#### McBits:

fast constant-time

code-based cryptography

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# **Objectives**

# Set new speed records for public-key cryptography.

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... all of the above *at once*.

### The track record

1978 McEliece proposed public-key code-based crypto.

Has held up well after extensive optimization of attack algorithms: 1962 Prange. 1981 Omura.

- 1988 Lee-Brickell. 1988 Leon.
- 1989 Krouk. 1989 Stern.
- 1989 Dumer.
- 1990 Coffey–Goodman.
- 1990 van Tilburg. 1991 Dumer.
- 1991 Coffey–Goodman–Farrell.
- 1993 Chabanne–Courteau.
- 1993 Chabaud.

1994 van Tilburg.

- 1994 Canteaut–Chabanne.
- 1998 Canteaut-Chabaud.
- 1998 Canteaut–Sendrier.
- 2008 Bernstein-Lange-Peters.
- 2009 Bernstein–Lange–
- Peters-van Tilborg.
- 2009 Bernstein (post-quantum).
- 2009 Finiasz-Sendrier.
- 2010 Bernstein-Lange-Peters.
- 2011 May–Meurer–Thomae.
- 2011 Becker–Coron–Joux.
- 2012 Becker–Joux–May–Meurer.
- 2013 Bernstein–Jeffery–Lange–

Meurer (post-quantum).

### Examples of the competition

Some cycle counts on h9ivy (Intel Core i5-3210M, Ivy Bridge) from bench.cr.yp.to:

mceliece encrypt 61440(2008 Biswas–Sendrier,  $\approx 2^{80}$ ) gls254 DH 77468 (binary elliptic curve; CHES 2013) kumfp127g DH 116944 (hyperelliptic; Eurocrypt 2013) curve25519 DH 182632 (conservative elliptic curve) mceliece decrypt 1219344 ronald1024 decrypt 1340040

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All load/store addresses and all branch conditions are public. Eliminates cache-timing attacks etc.

Similar improvements for CFS.

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"How can this be competitive in speed? Are you really simulating field multiplication with hundreds of bit operations instead of simple log tables?" Yes, we are.

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Low-end smartphone CPU: 128-bit XOR every cycle.

Ivy Bridge: 256-bit XOR every cycle, or three 128-bit XORs. Not immediately obvious that this "bitslicing" saves time for, e.g., multiplication in  $\mathbf{F}_{2^{12}}$ . Not immediately obvious that this "bitslicing" saves time for, e.g., multiplication in  $\mathbf{F}_{2^{12}}$ .

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Typical decoding algorithms have add, mult roughly balanced.

Coming next: how to save many adds and *most* mults. Nice synergy with bitslicing.

### <u>The additive FFT</u>

Fix  $n = 4096 = 2^{12}$ , t = 41.

Big final decoding step is to find all roots in  $\mathbf{F}_{2^{12}}$ of  $f = c_{41}x^{41} + \cdots + c_0x^0$ . For each  $\alpha \in \mathbf{F}_{2^{12}}$ , compute  $f(\alpha)$  by Horner's rule: 41 adds, 41 mults.

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Our cost: 6.01 adds, 2.09 mults.

Asymptotics: normally  $t \in \Theta(n/\lg n)$ , so Horner's rule costs  $\Theta(nt) = \Theta(n^2/\lg n)$ . Asymptotics: normally  $t \in \Theta(n/\lg n)$ , so Horner's rule costs  $\Theta(nt) = \Theta(n^2/\lg n)$ .

Wait a minute. Didn't we learn in school that FFT evaluates an *n*-coeff polynomial at *n* points using  $n^{1+o(1)}$  operations? Isn't this better than  $n^2/\lg n$ ?

#### Standard radix-2 FFT:

Want to evaluate  $f = c_0 + c_1 x + \dots + c_{n-1} x^{n-1}$  at all the *n*th roots of 1.

Write f as  $f_0(x^2) + x f_1(x^2)$ . Observe big overlap between  $f(\alpha) = f_0(\alpha^2) + \alpha f_1(\alpha^2)$ ,  $f(-\alpha) = f_0(\alpha^2) - \alpha f_1(\alpha^2)$ .

 $f_0$  has n/2 coeffs; evaluate at (n/2)nd roots of 1 by same idea recursively. Similarly  $f_1$ . Useless in char 2:  $\alpha = -\alpha$ . Standard workarounds are painful. FFT considered impractical.

1988 Wang–Zhu, independently 1989 Cantor: "additive FFT" in char 2. Still quite expensive.

1996 von zur Gathen–Gerhard: some improvements.

2010 Gao–Mateer: much better additive FFT.

We use Gao–Mateer, plus some new improvements. Gao and Mateer evaluate  $f = c_0 + c_1 x + \cdots + c_{n-1} x^{n-1}$ on a size-*n* **F**<sub>2</sub>-linear space.

Their main idea: Write f as  $f_0(x^2 + x) + x f_1(x^2 + x)$ .

Big overlap between  $f(\alpha) = f_0(\alpha^2 + \alpha) + \alpha f_1(\alpha^2 + \alpha)$ and  $f(\alpha + 1) = f_0(\alpha^2 + \alpha) + (\alpha + 1)f_1(\alpha^2 + \alpha)$ .

"Twist" to ensure  $1 \in$  space. Then  $\{\alpha^2 + \alpha\}$  is a size-(n/2)  $\mathbf{F}_2$ -linear space. Apply same idea recursively.

#### <u>Results</u>

60493 Ivy Bridge cycles:

8622 for permutation.

20846 for syndrome.

7714 for BM.

14794 for roots.

8520 for permutation.

Code will be public domain. We're still speeding it up.

Also  $10 \times$  speedup for CFS.

More information:

cr.yp.to/papers.html#mcbits

What you find in paper:

Cryptosystem specification.

Our speedups to additive FFT. (We now have more speedups; ongoing joint work with Lange.)

Fast syndrome computation without big precomputed matrix. Important for lightweight!

Fast secret permutation using bit operations: sorting networks, permutation networks.