DPA Contest 2008 – 2009
Less than 50 traces allow to recover the key

Christophe Clavier [1] [2]

[1] Institut d'Ingénierie Informatique de Limoges (3iL)

[2] Université de Limoges – XLIM

Lausanne – September 7, 2009

Description of the method

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Given a consumption model (Hamming distance between L_i and R_i), we compute for each key guess k its *a posteriori* probability $Pr(k|traces)$

- Predicted value assuming k is evaluated for each trace
- Sum of squared differences between predictions and observations:
  - $\longrightarrow$ a posteriori probability of the traces given the key
  - $\longrightarrow$ a posteriori probability of the key given the traces (Bayes)

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Is this method new?

- Already mentionned by Bevan and Knudsen (ICISC'02)
- Major differences:
  - We guess the full 56-bit key (particularly suited to hardware DES)
  - We focus on two points of interest (end of first round & end of DES)

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Partial exploration of the key space:

- Oriented iterative walk (heuristic)
- Given a key candidate k_i
  - Search for a better one k_{i+1} in a neighbourhood of k_i
  - Repeat the process until $k_{i+1} = k_i$ (stability)
- Starting from a random k_0, the best key encountered may not be the correct one (particularly with few traces)
- Explore a largest key space portion by considering several initial key candidates (increase probability of success)
- Other heuristic methods are possible: genetic algorithms, simulated annealing,...

Our results

We posted three solutions to the *Representative Order* category

(average score on 100 runs with randomly chosen traces)

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Solution 1 (dpa_contest.representative.1.c)

- posted on August 18, 2009
- uses a bivariate known model with 3 points of interest
- key recovered with only 42.42 curves on average
- assume a strong adversary model
  - previous caraterization of the consumption function
  - need a device with fixed known key

Our results

Solution 2 (dpa_contest.representative.3.c)

- posted on August 30, 2009 (together with solution 3)
- uses a bivariate unknown model with 2 points of interest
- key recovered with 46.06 curves on average
- do not assume a strong adversary model!
  - model parameters are infered on-the-fly by linear regression

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Solution 3 (dpa_contest.representative.4.c)

- same as solution 2 with a univariate model
- key recovered with 53.42 curves on average

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Conclusion

- Maximum likelihood method combined with full-key guessing strategy showed to be efficient to tackle the *DPA contest* challenge
- Further details about the method available in the source comments

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