

Valiant's Universal Circuit is Practical

Ágnes Kiss
Thomas Schneider

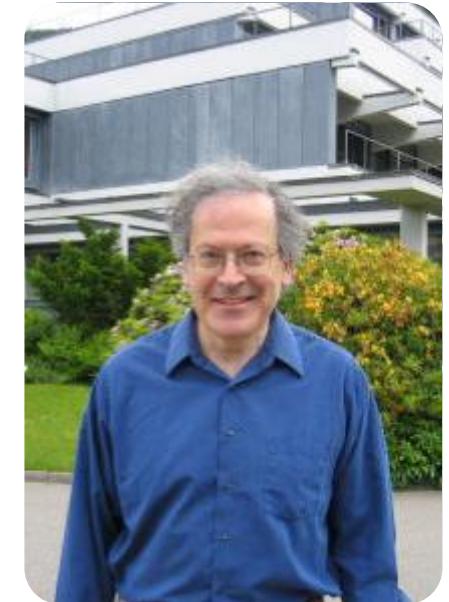
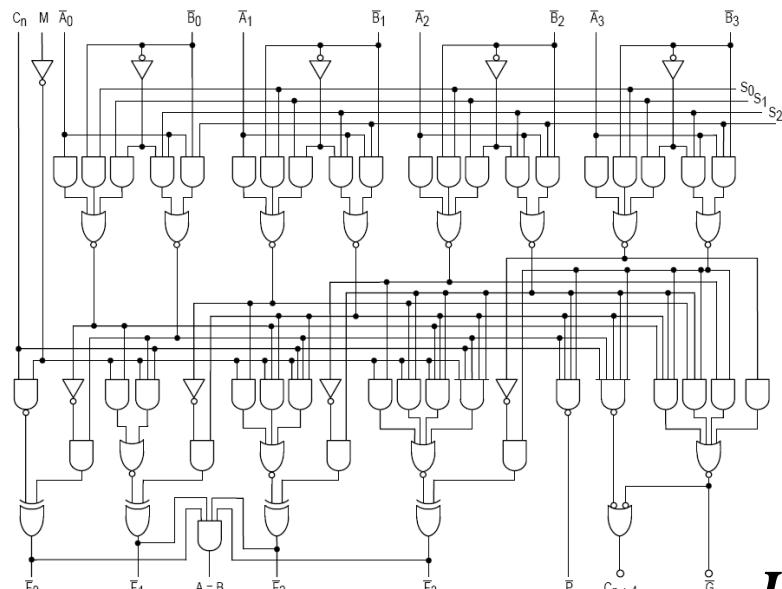
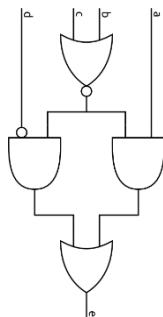
TU Darmstadt

Eurocrypt 2016
May 11, 2016



Universal Circuit (UC)

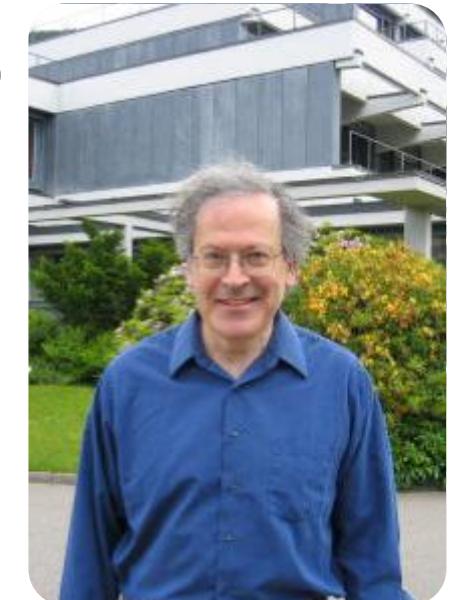
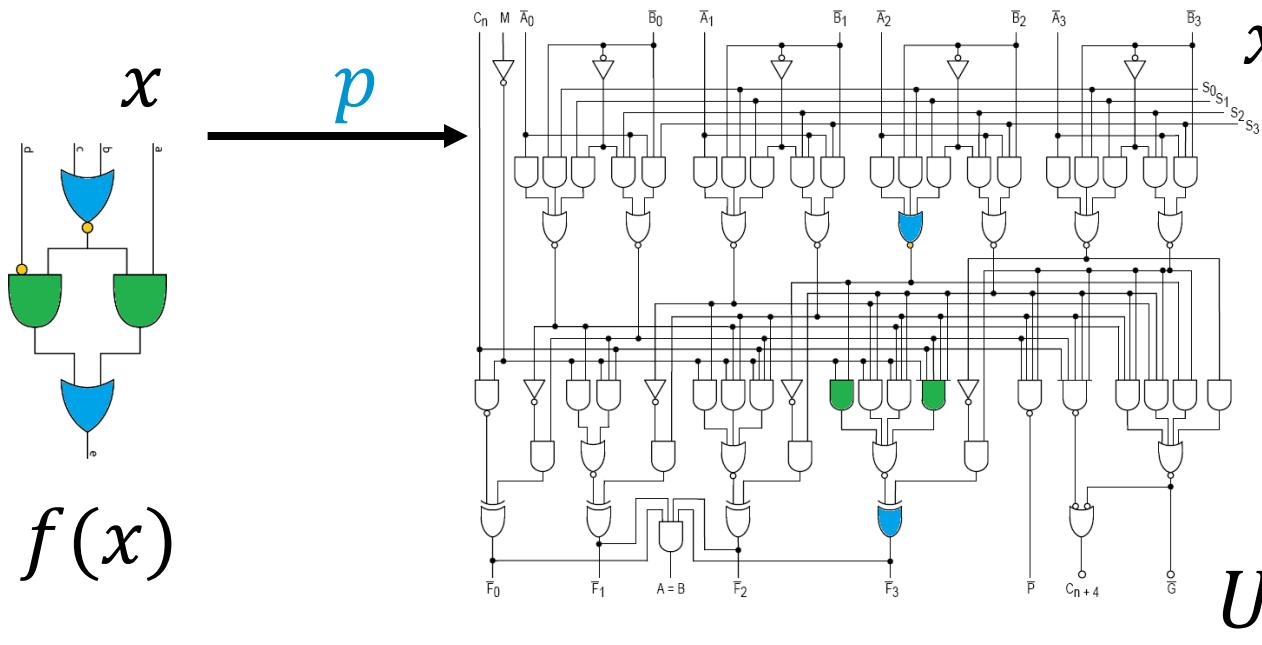
There is a Boolean circuit UC of size $O(n \log n)$ for which it holds that for any Boolean function f of size n UC can be made to compute f .



Leslie G. Valiant
1976

Universal Circuit (UC)

There is a Boolean circuit UC of size $O(n \log n)$ for which it holds that for any Boolean function f of size n there exists a programming p such that for any input x : $UC(p, x) = f(x)$.



Leslie G. Valiant
1976

UC Applications



Verifiable
computation



Program obfuscation

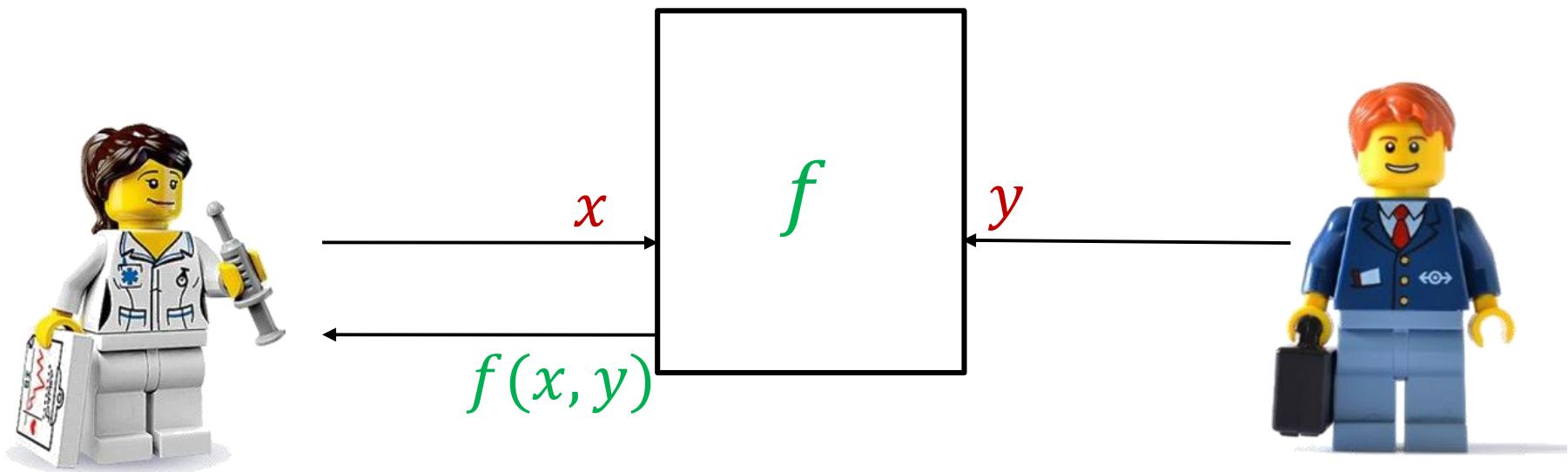


Attribute-based
encryption

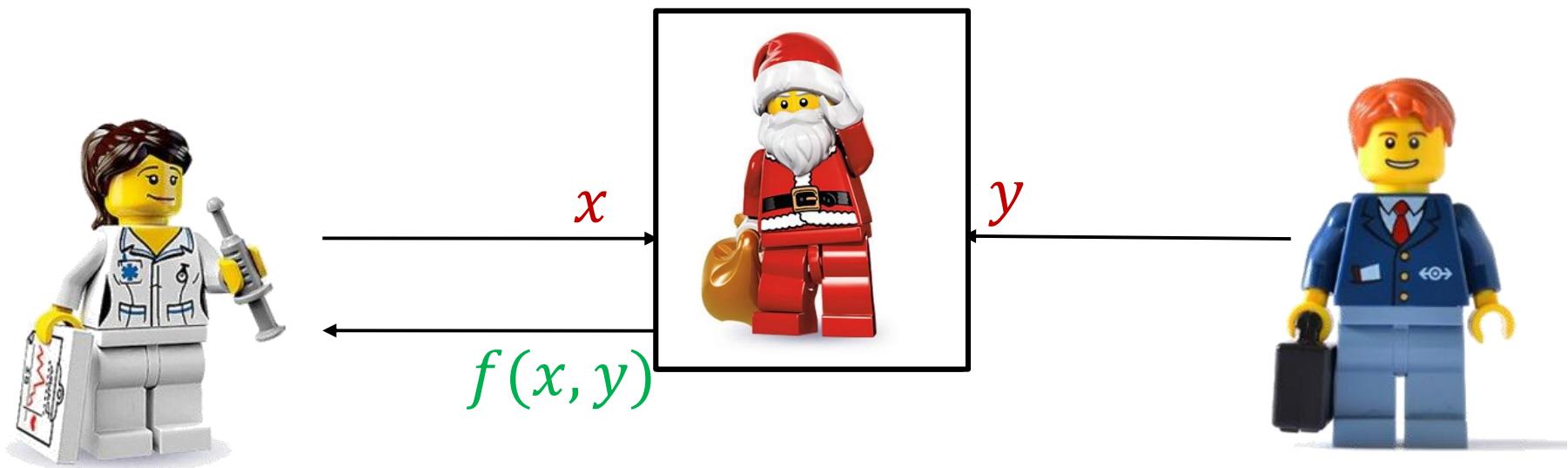


Private function
evaluation

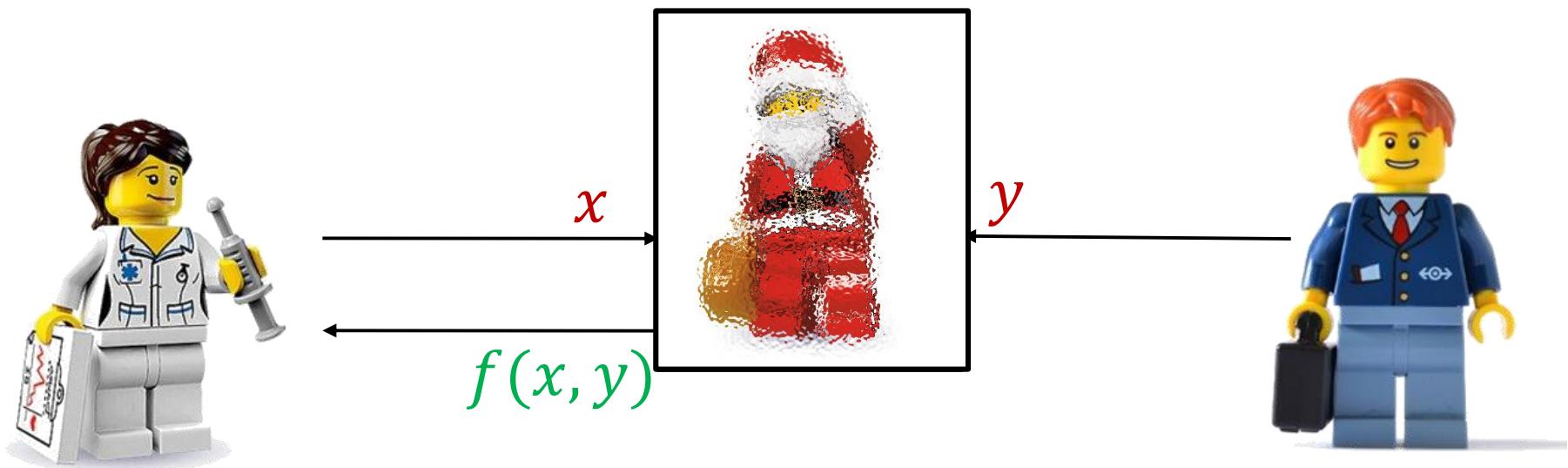
Secure Function Evaluation



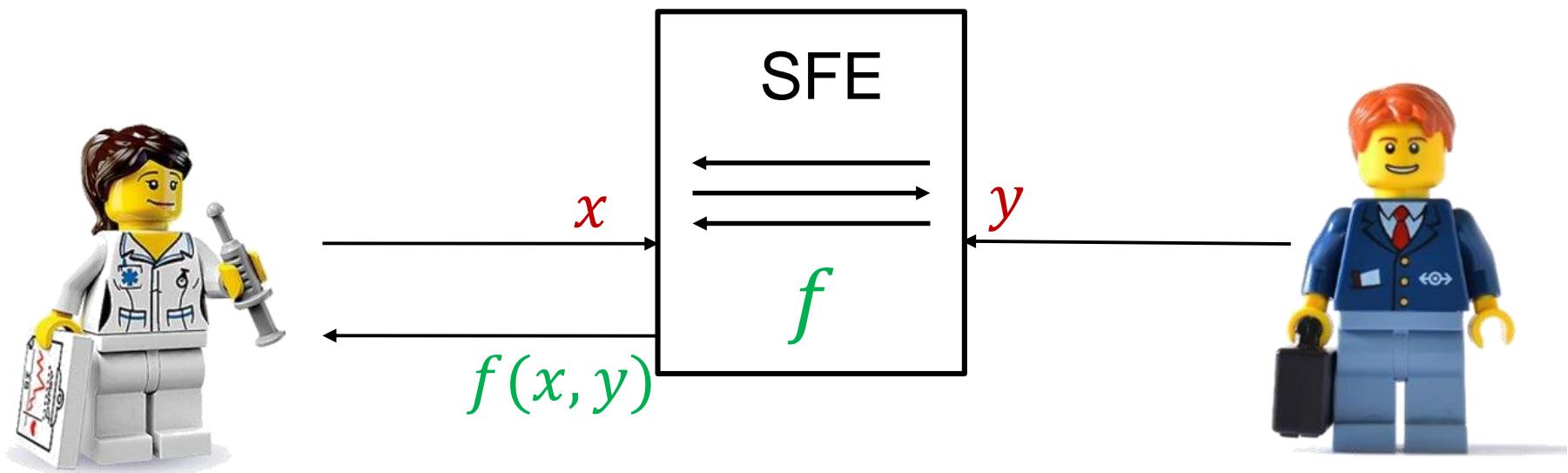
Secure Function Evaluation



Secure Function Evaluation

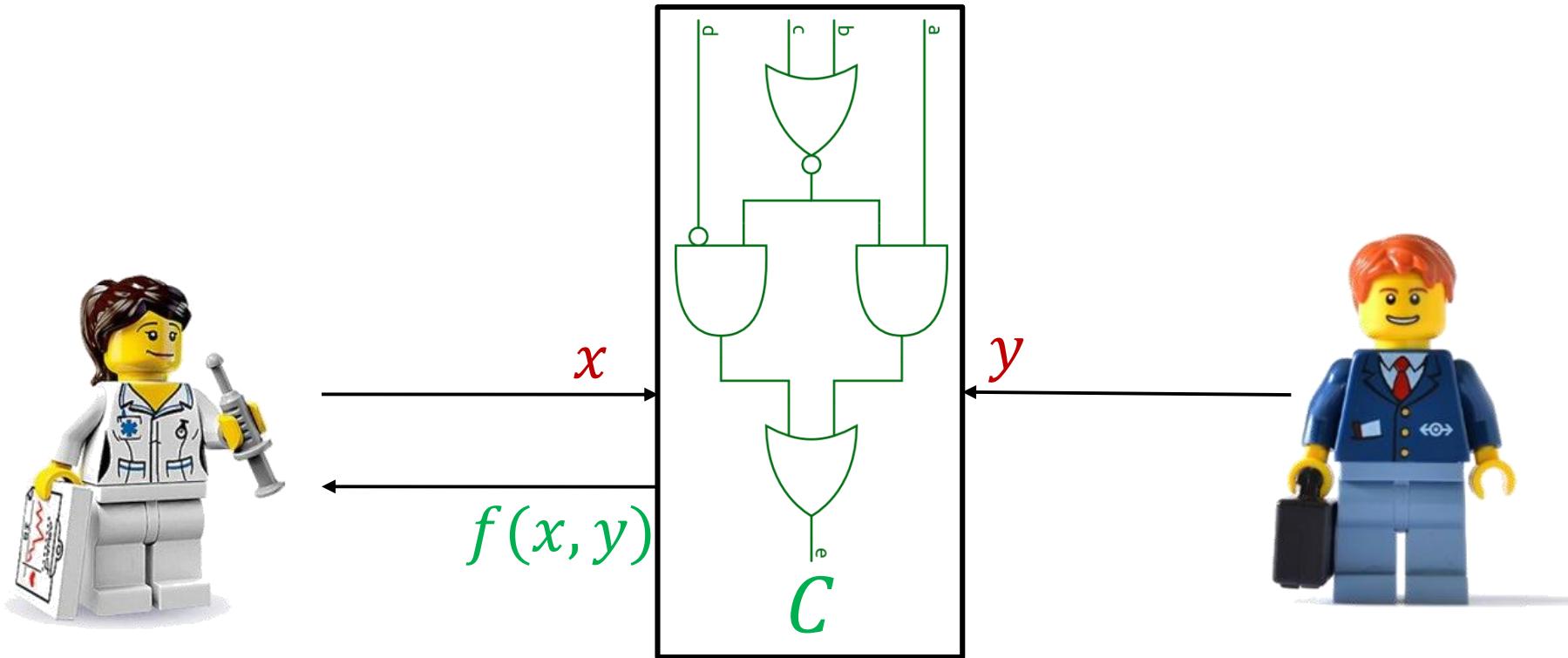


Secure Function Evaluation



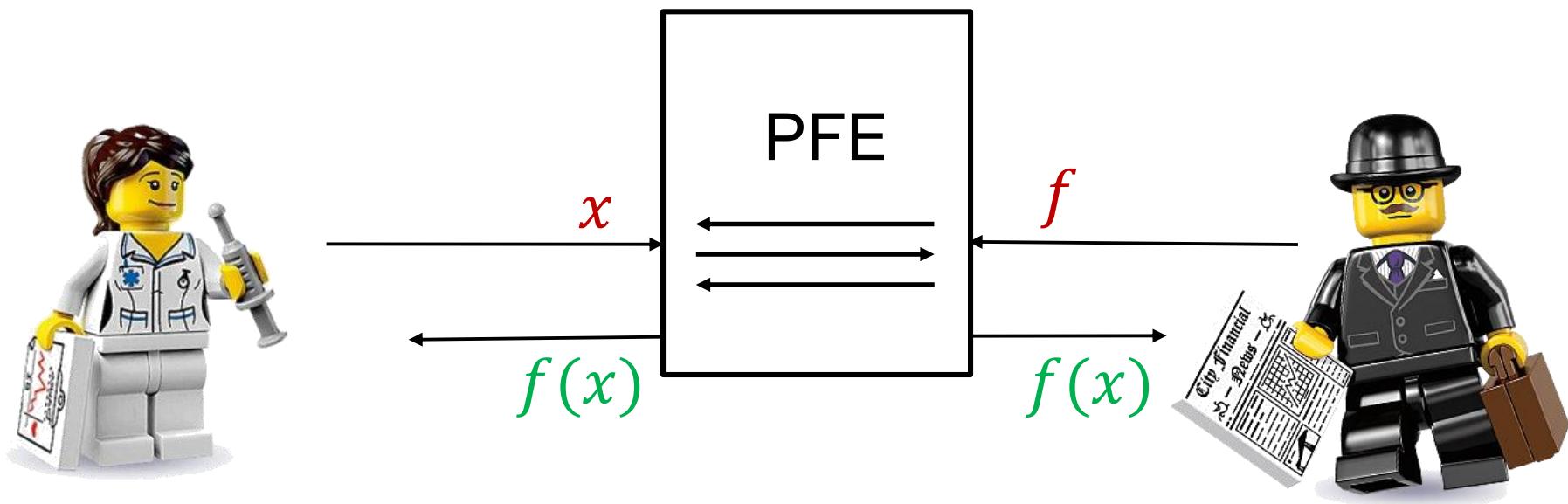
Secure Function Evaluation

Boolean circuit

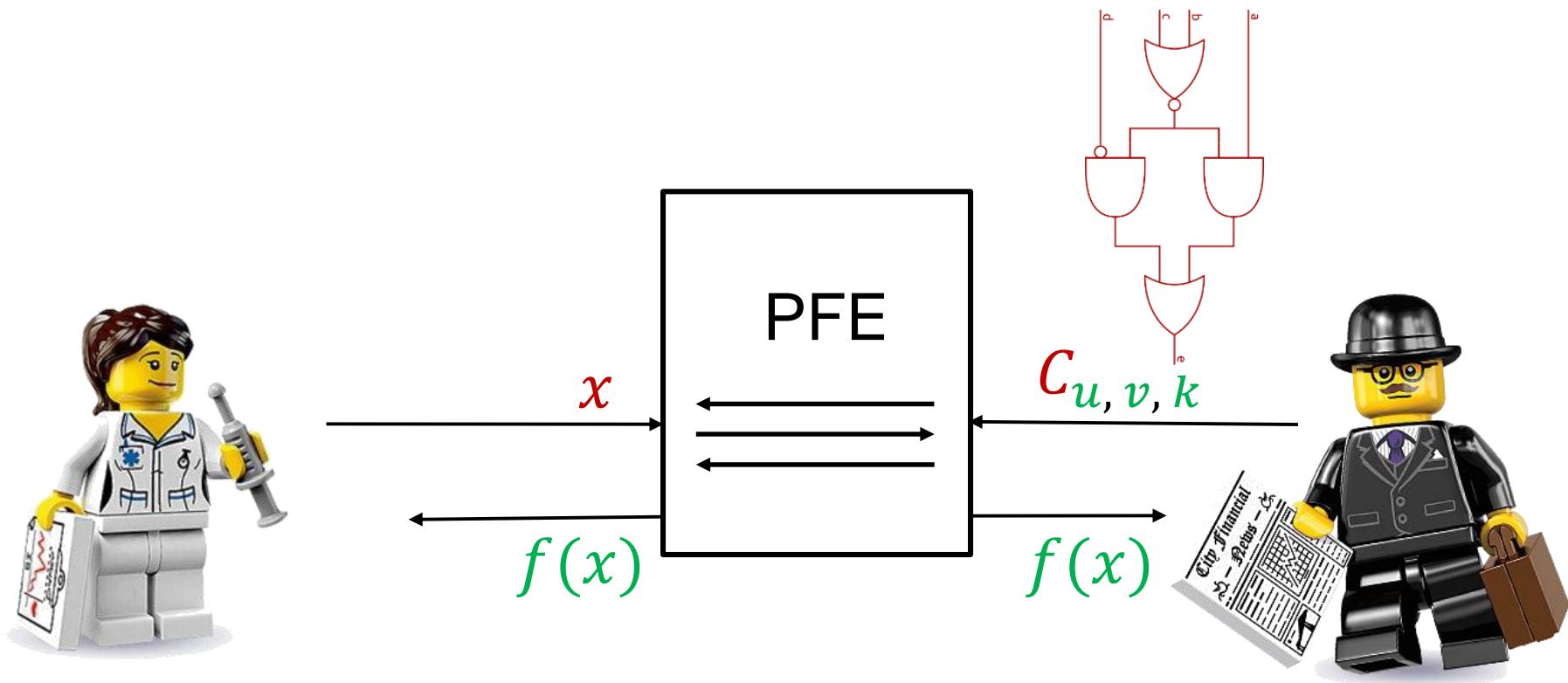


- ⇒ Yao's Garbled Circuit Protocol
- ⇒ Goldreich-Micali-Wigderson Protocol

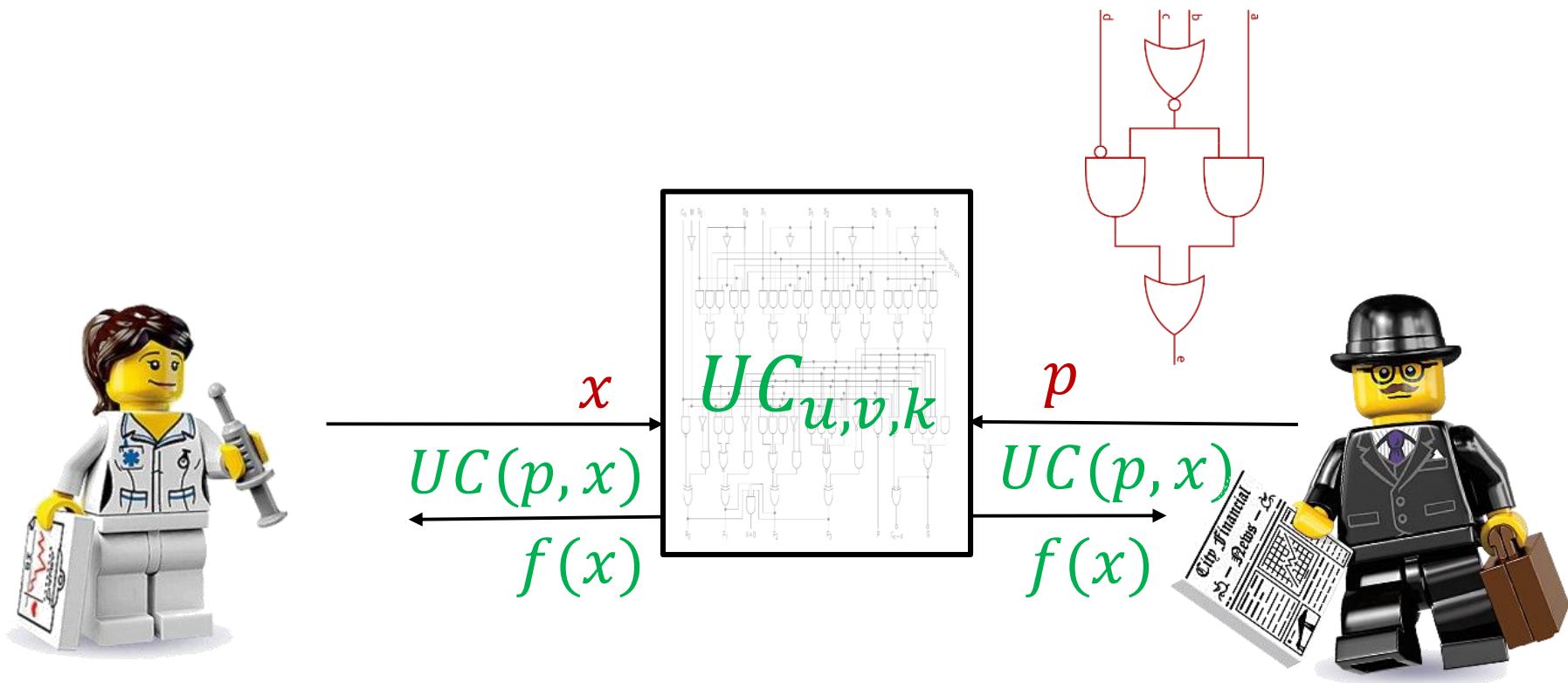
Private Function Evaluation



Private Function Evaluation



Private Function Evaluation



PFE Applications



Software diagnostics



Medical diagnostics



Private databases



Private search
queries

UC Construction

C (size: $n = u + v + k$)

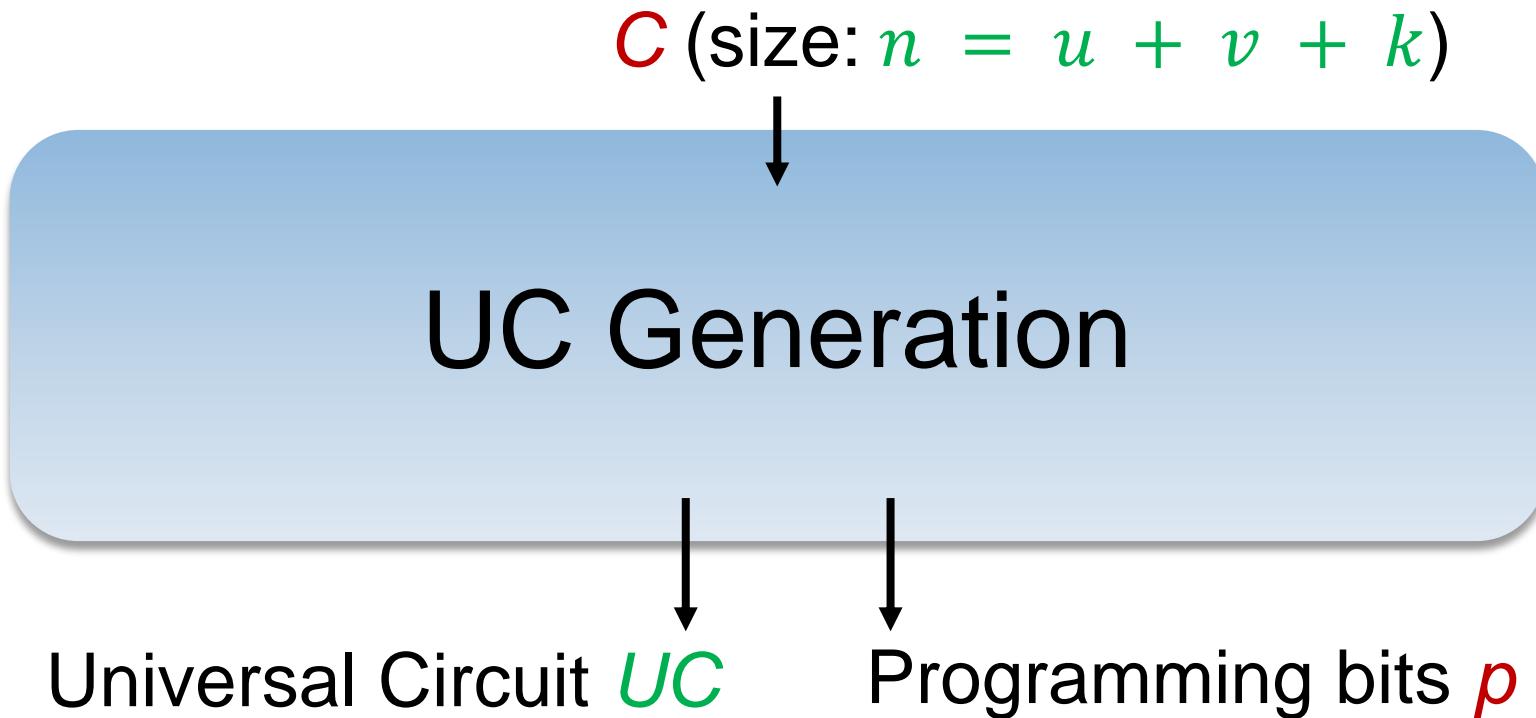
UC Construction

C (size: $n = u + v + k$)



UC Generation

UC Construction



Existing UC Constructions

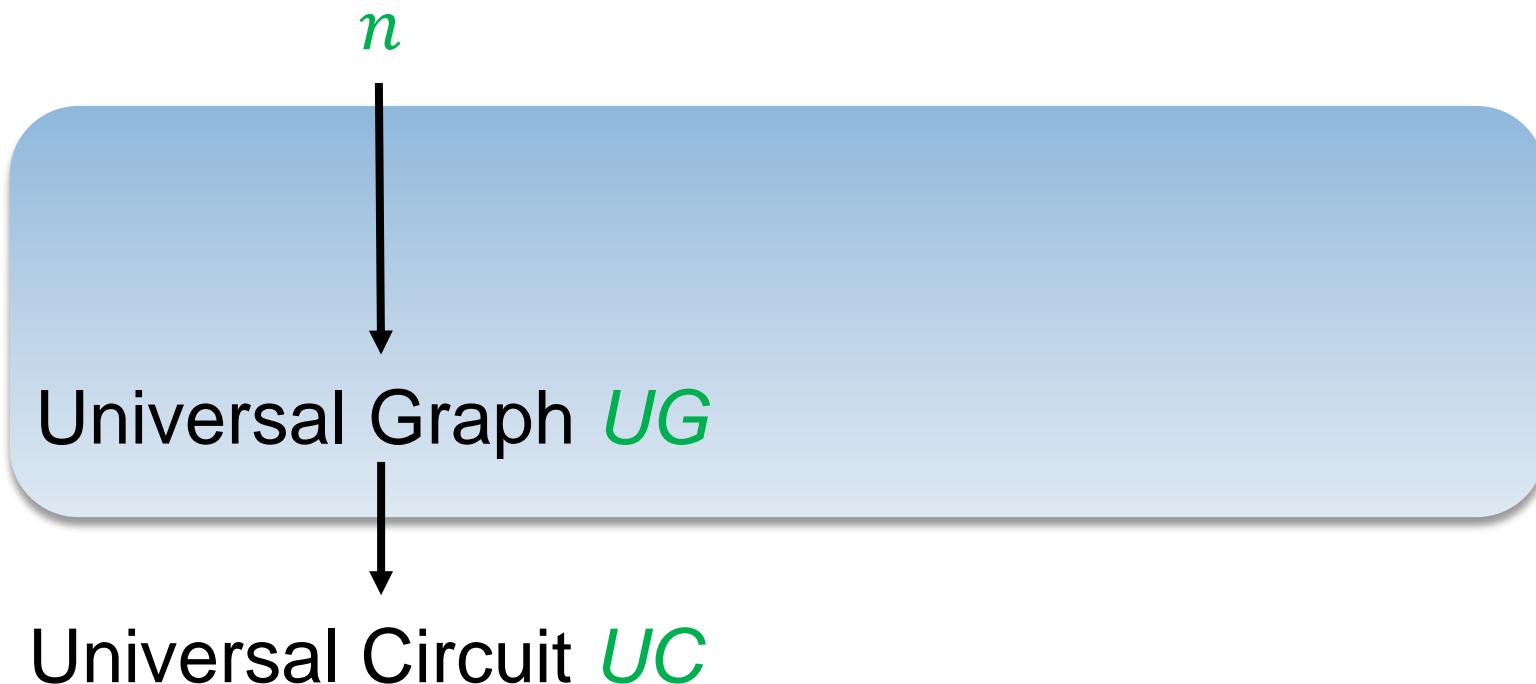
	[Val76]	[KS08]
Size	$O(n \log n)$	$O(n \log^2 n)$
Depth	$O(n)$	$O(n \log n)$
Implemented	✗	✓

[Val76] L. G. Valiant: Universal circuits (preliminary report). In *STOC 1976*.

[KS08] V. Kolesnikov, T. Schneider: A practical universal circuit construction and secure evaluation of private functions. In *FC 2008*.

Valiant's UC Construction

GENERATION



[Val76] L. G. Valiant: Universal circuits
(preliminary report). In STOC 1976.

Valiant's UC Construction

GENERATION

n



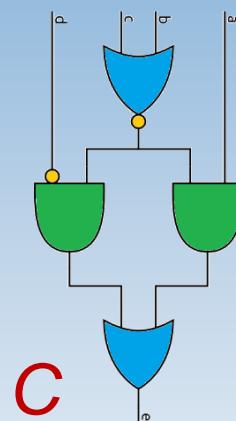
Universal Graph UG



Universal Circuit UC

C size $\leq n$

p c q e



[Val76] L. G. Valiant: Universal circuits

(preliminary report). In STOC 1976.

PROGRAMMING

Valiant's UC Construction

GENERATION

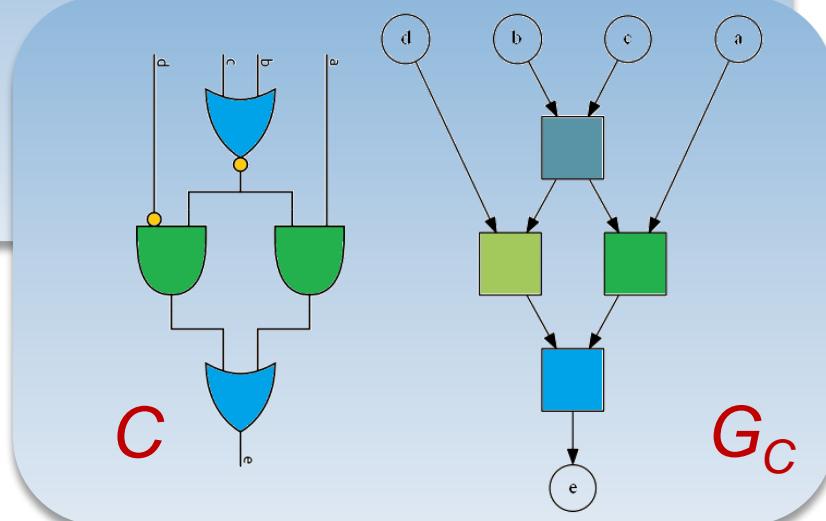
n

C size $\leq n$

Universal Graph UG

Graph G_C

Universal Circuit UC



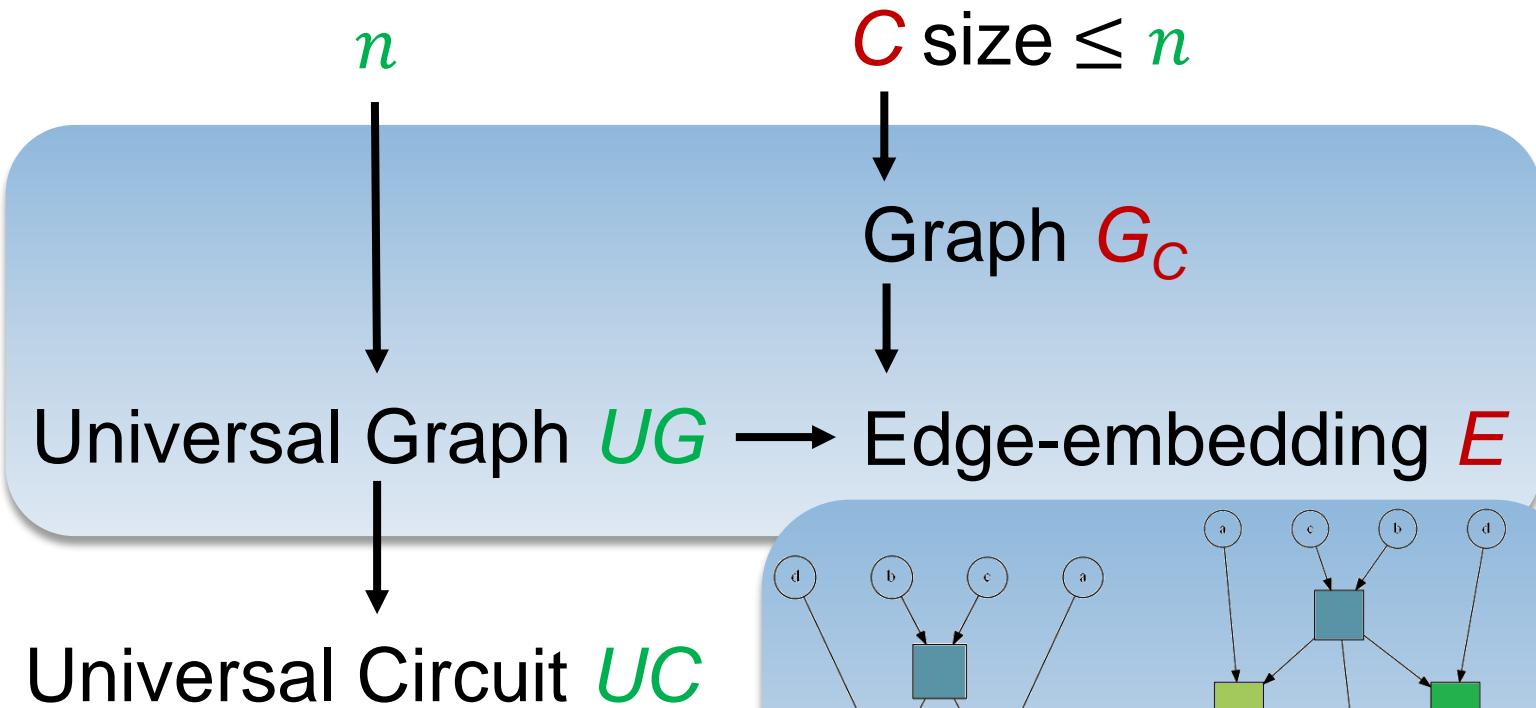
[Val76] L. G. Valiant: Universal circuits

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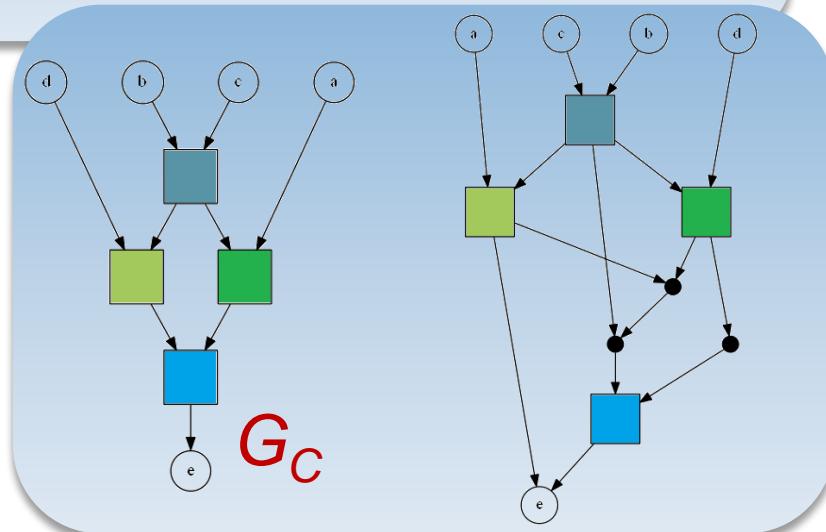
PROGRAMMING

Valiant's UC Construction

GENERATION



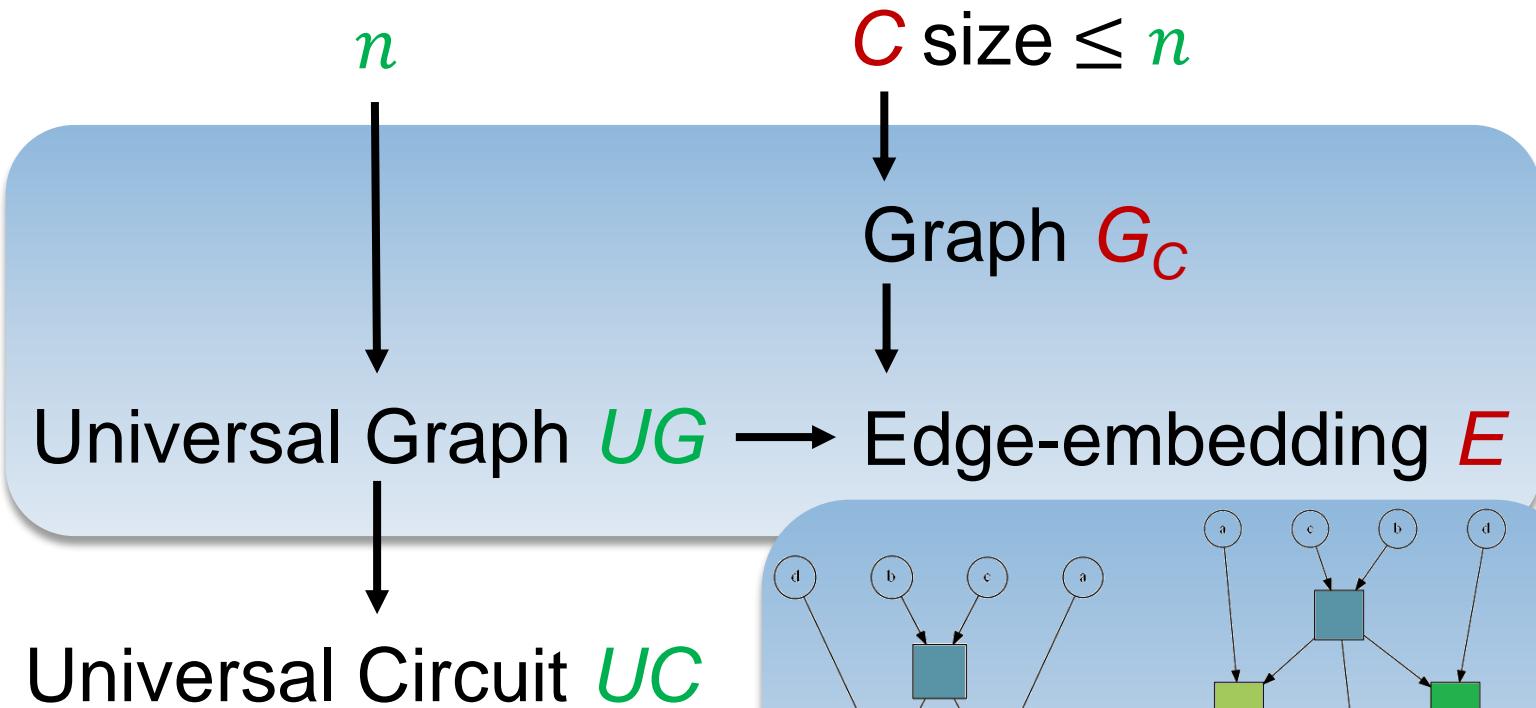
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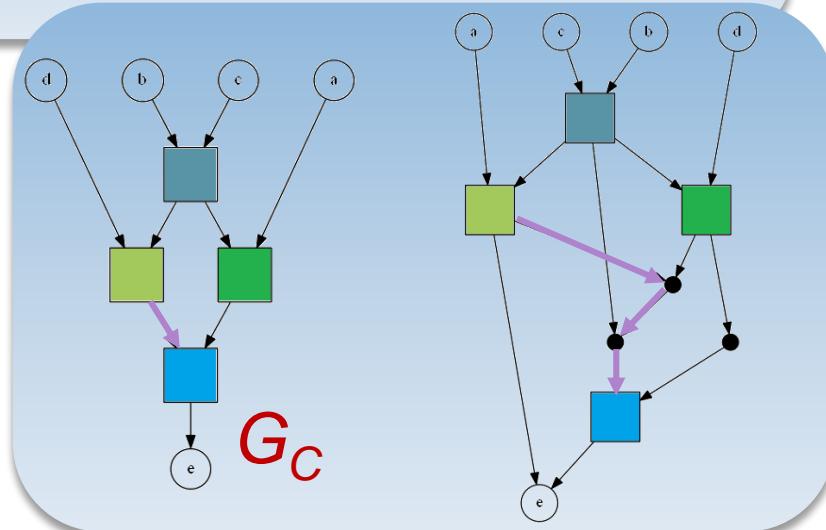
PROGRAMMING

Valiant's UC Construction

GENERATION



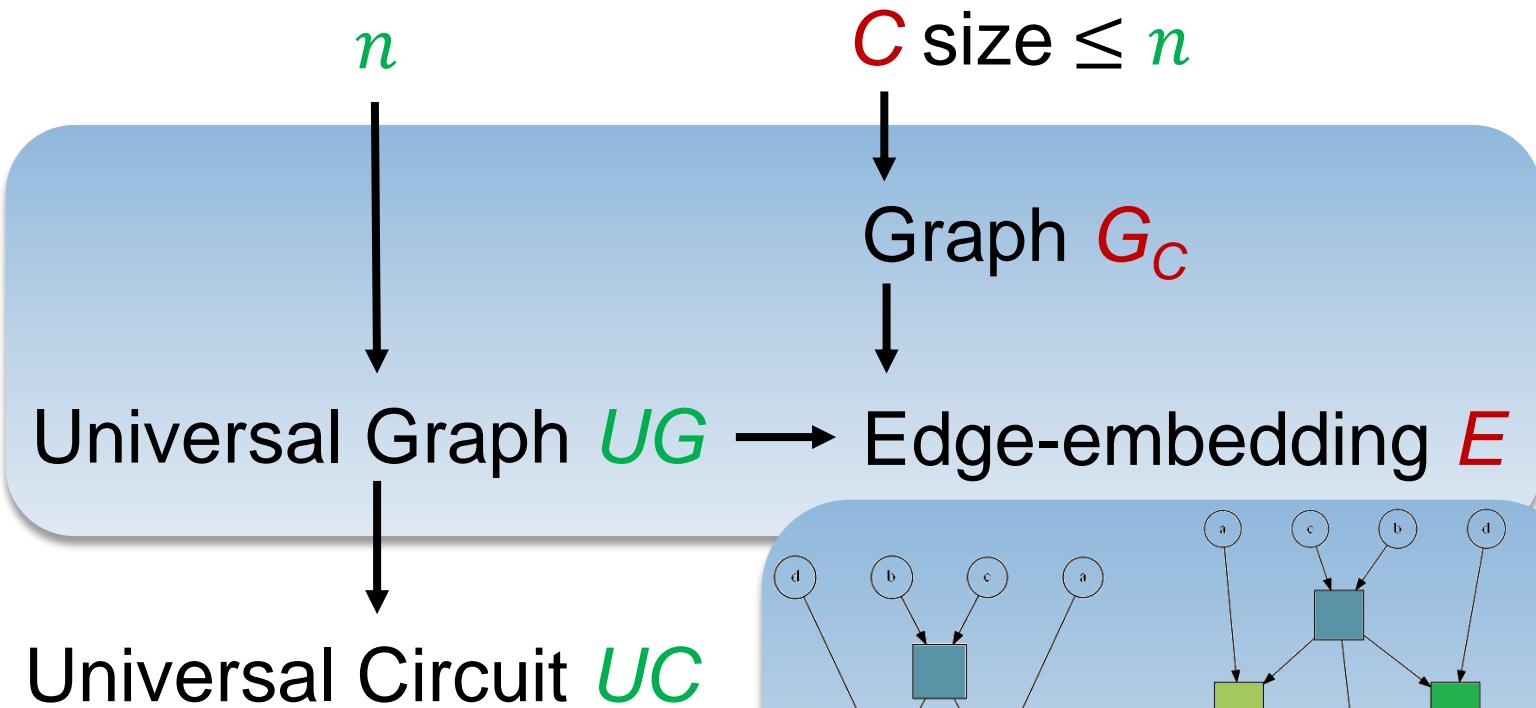
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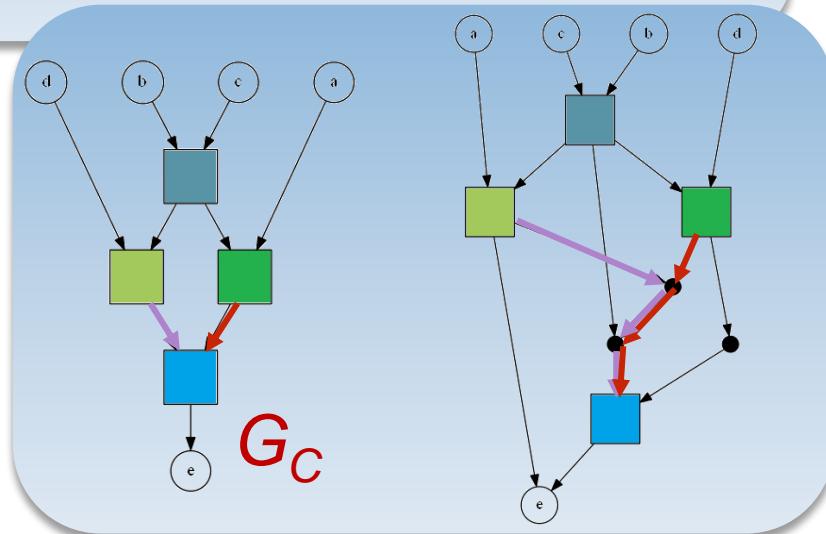
PROGRAMMING

Valiant's UC Construction

GENERATION



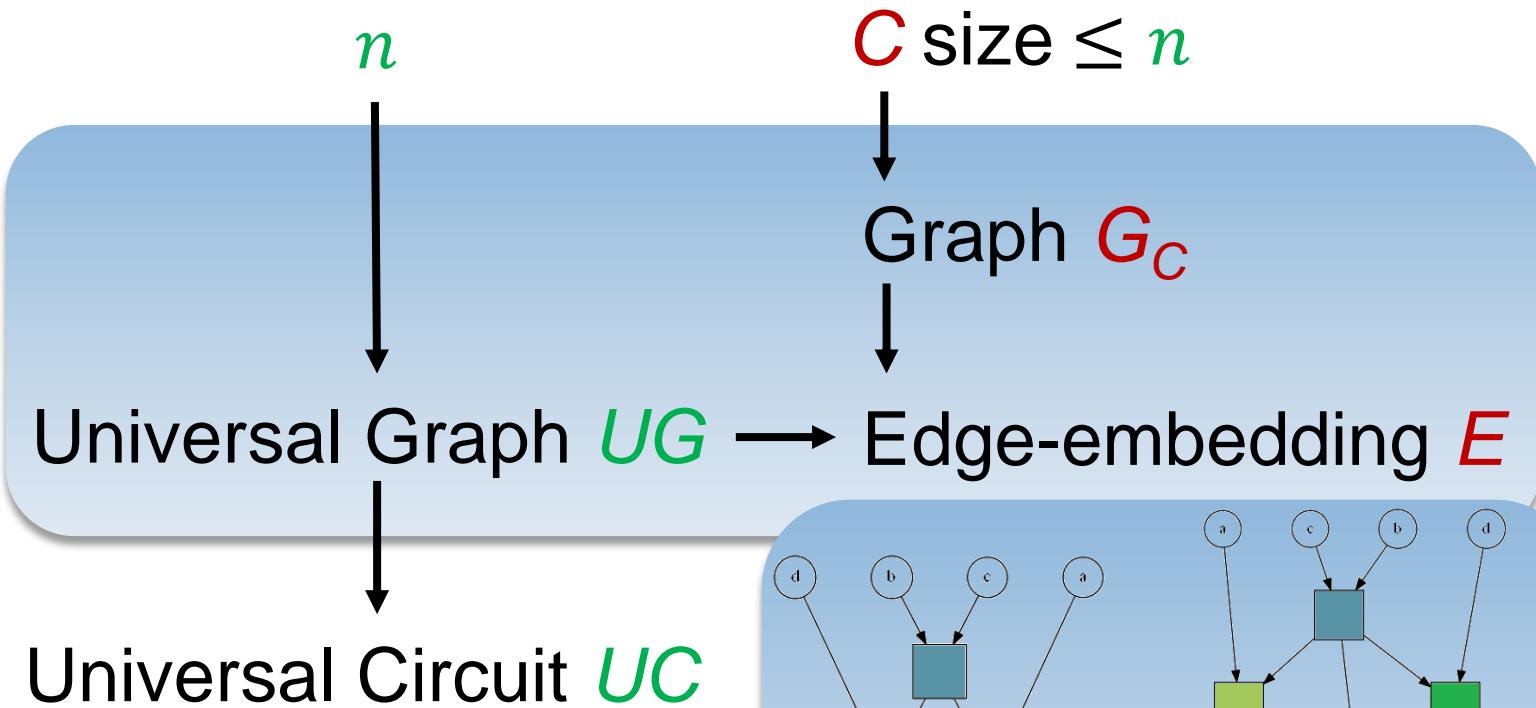
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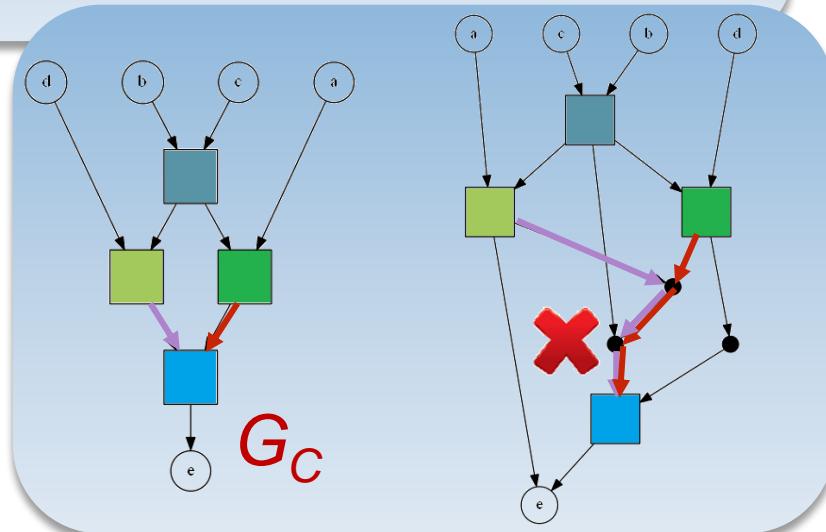
PROGRAMMING

Valiant's UC Construction

GENERATION



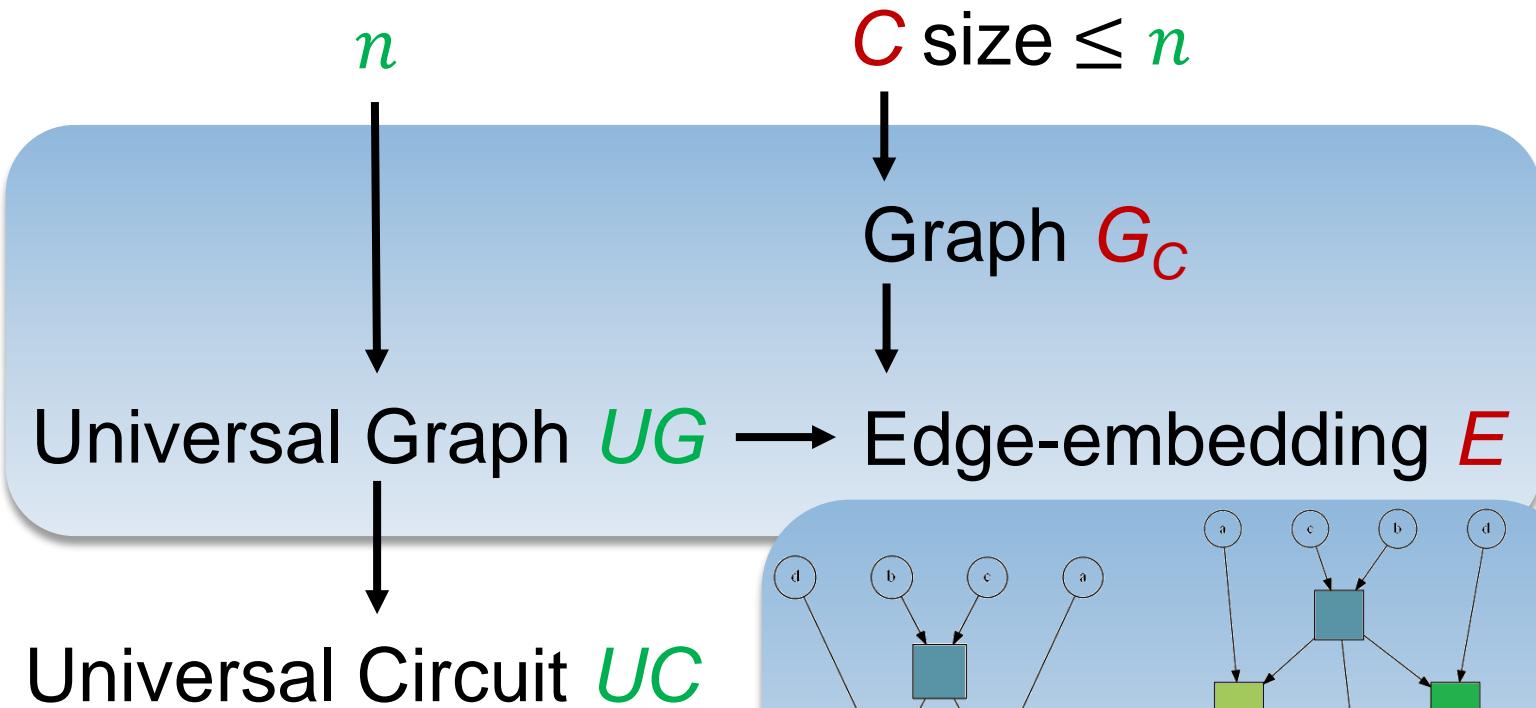
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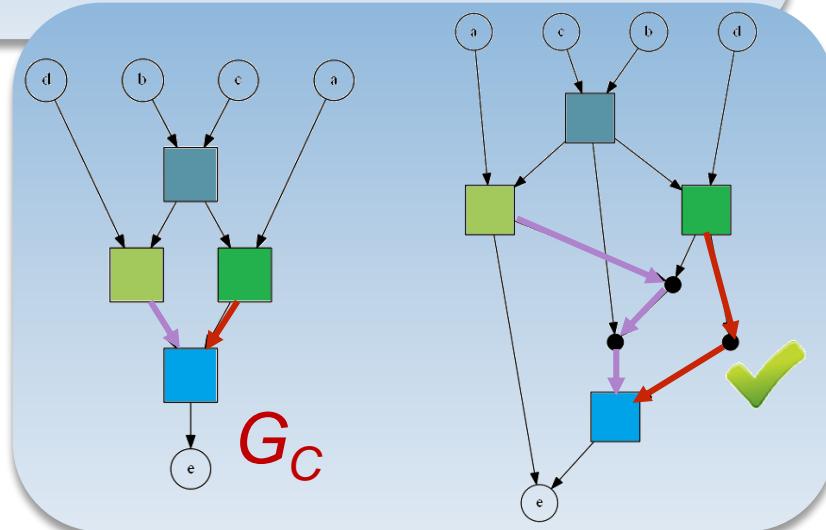
PROGRAMMING

Valiant's UC Construction

GENERATION



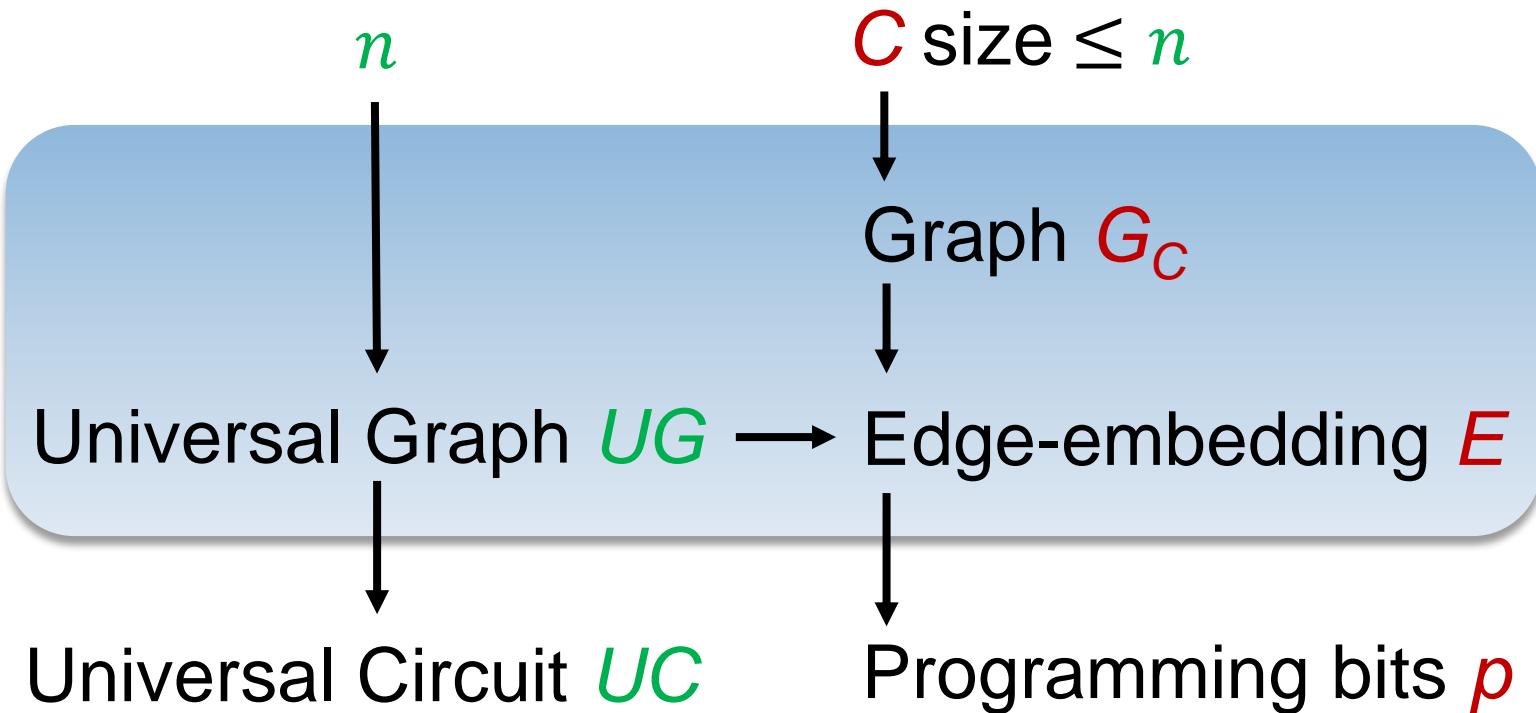
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PROGRAMMING

Valiant's UC Construction

GENERATION

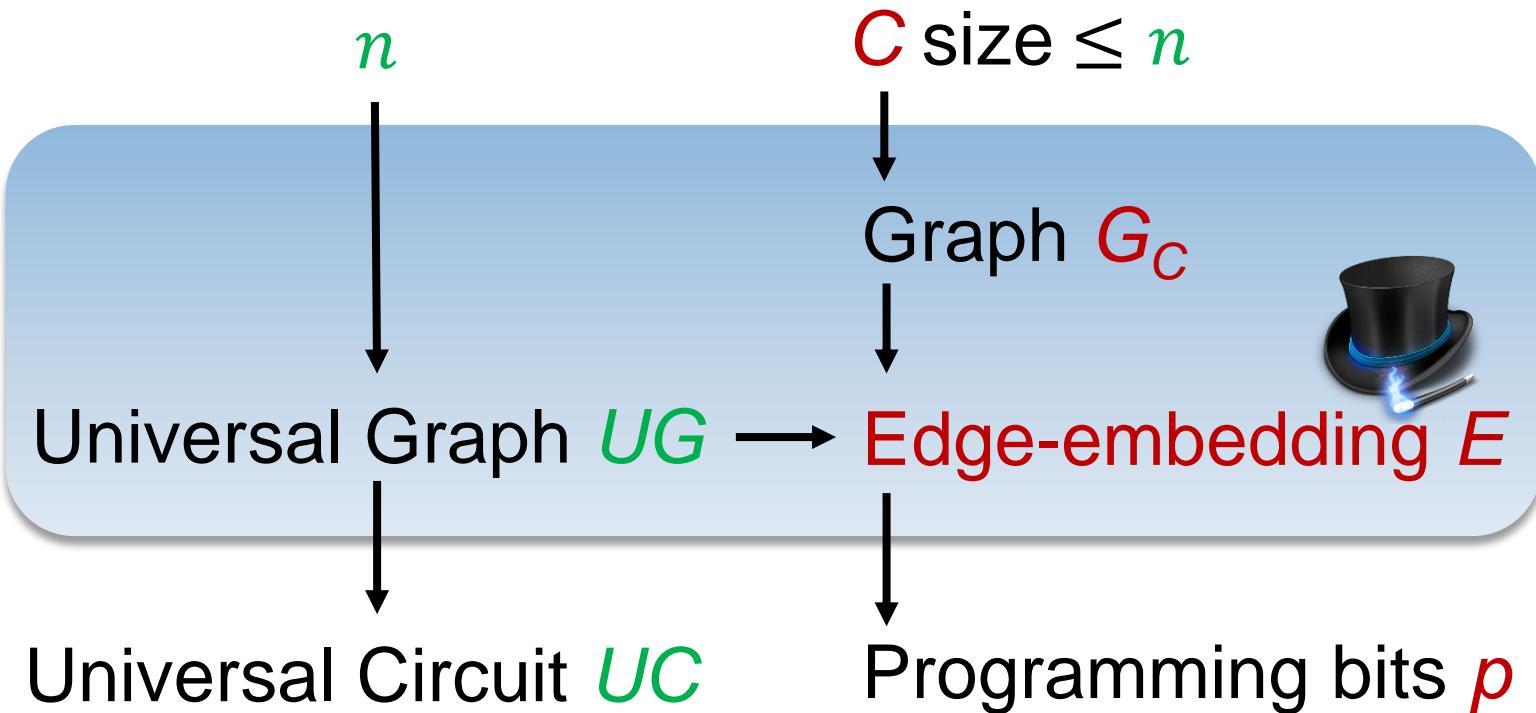


PROGRAMMING

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Valiant's UC Construction

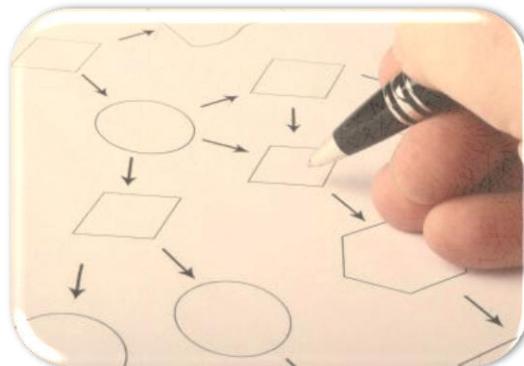
GENERATION



[Val76] L. G. Valiant: Universal circuits
(preliminary report). In STOC 1976.

Our Contributions

Valiant's universal circuit is practical.



**Embedding
algorithm**



Refined size of
construction



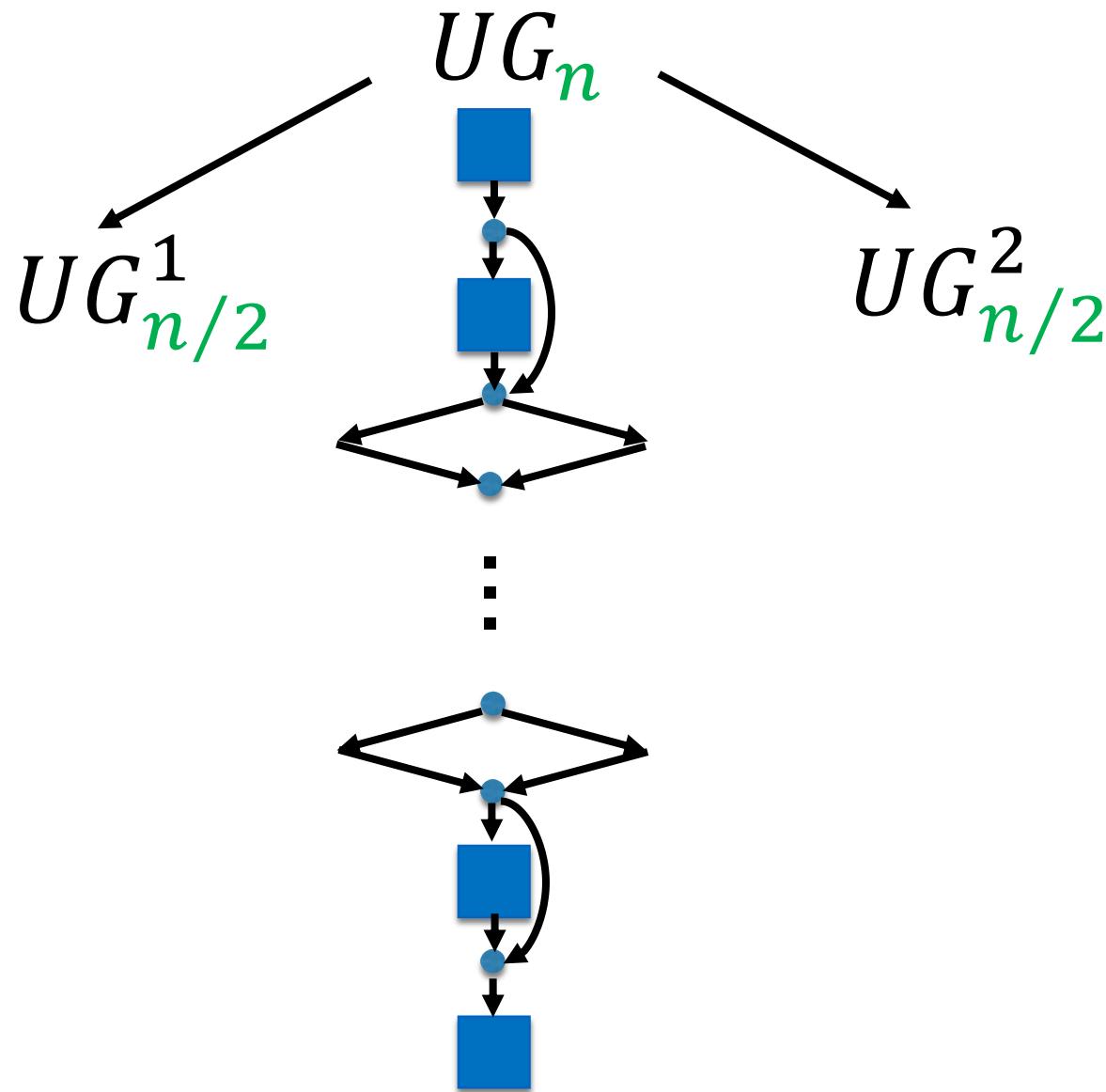
UC compiler

UG Embedding Algorithm

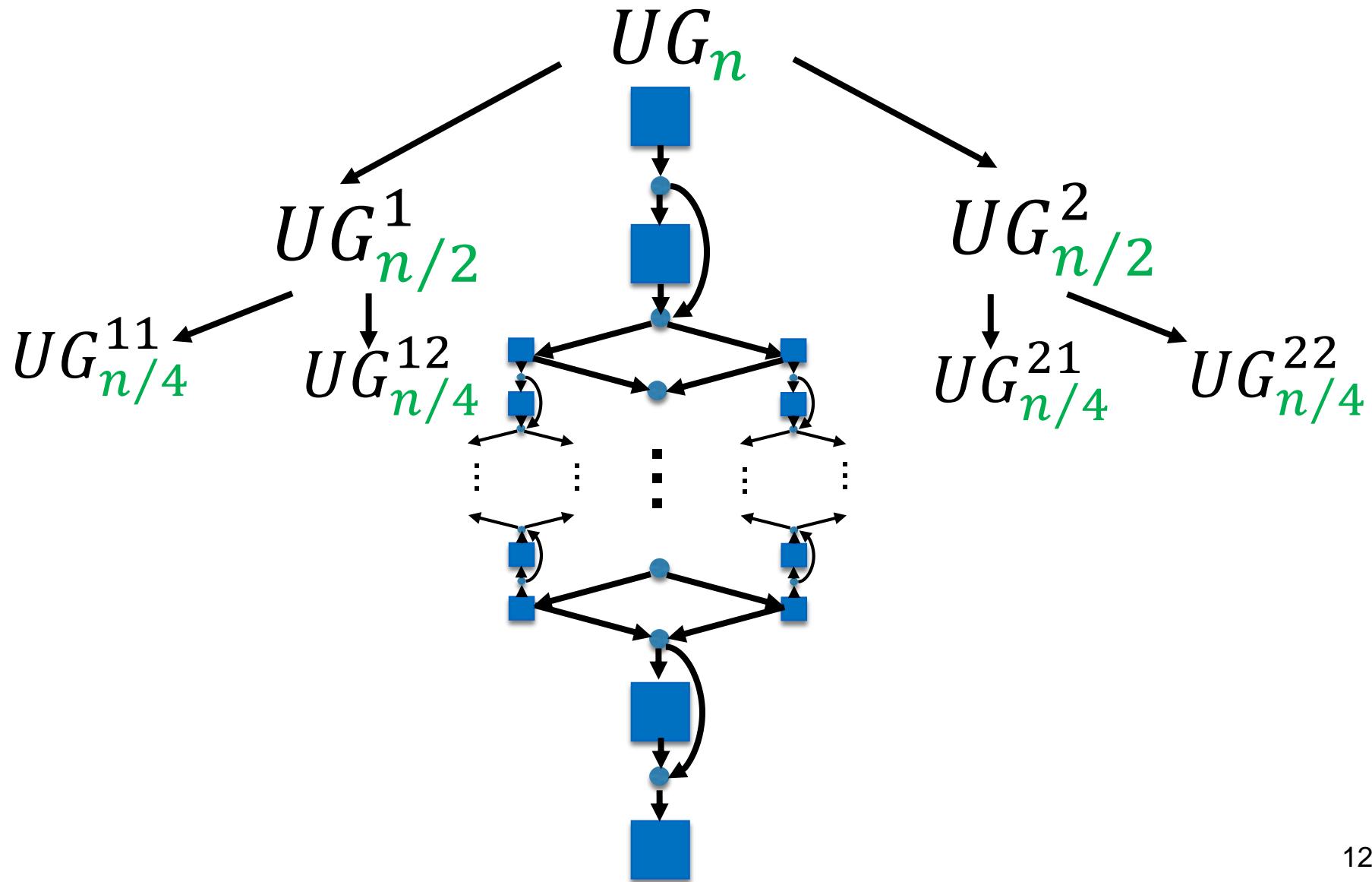
Universal Graph $UG \rightarrow$ Graph G_C
Edge-embedding E



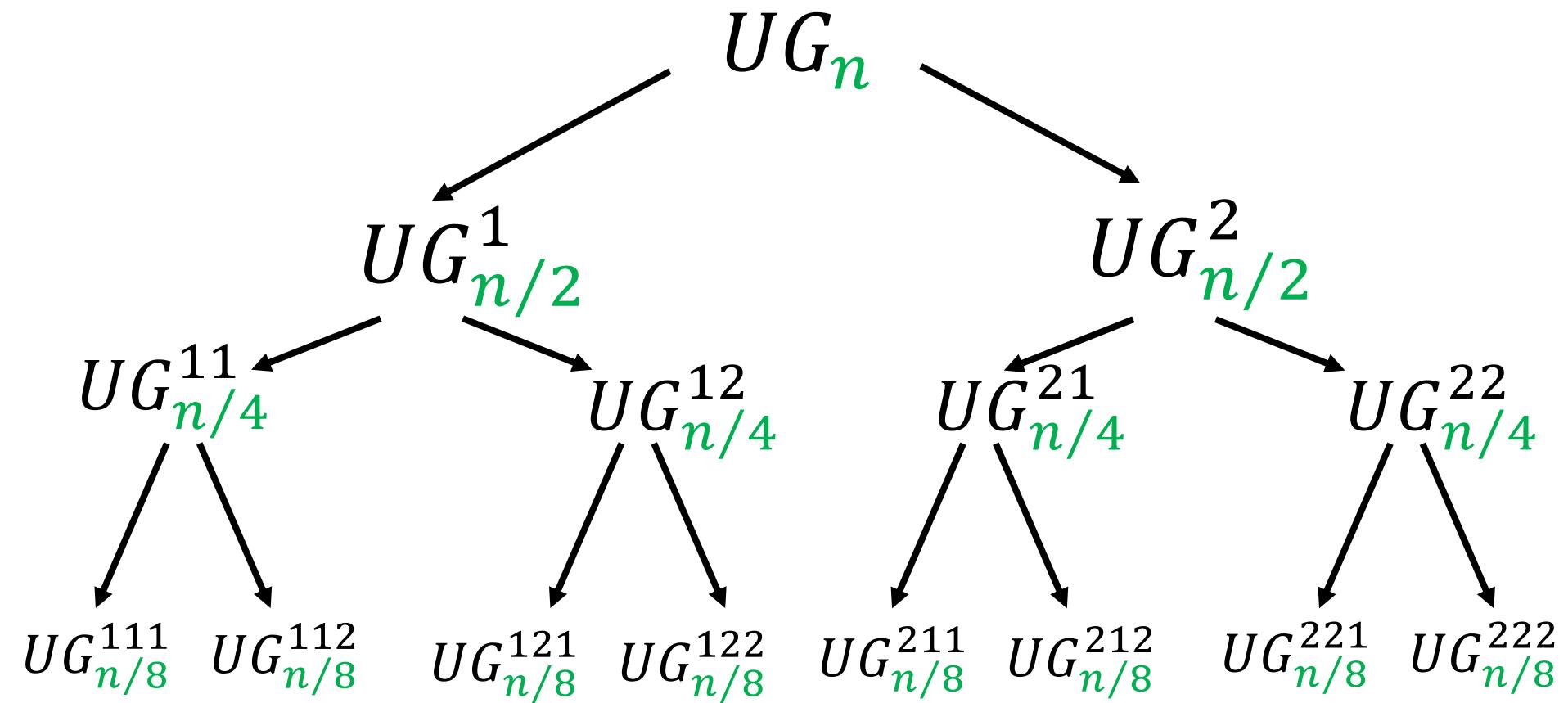
Recursive UG Construction



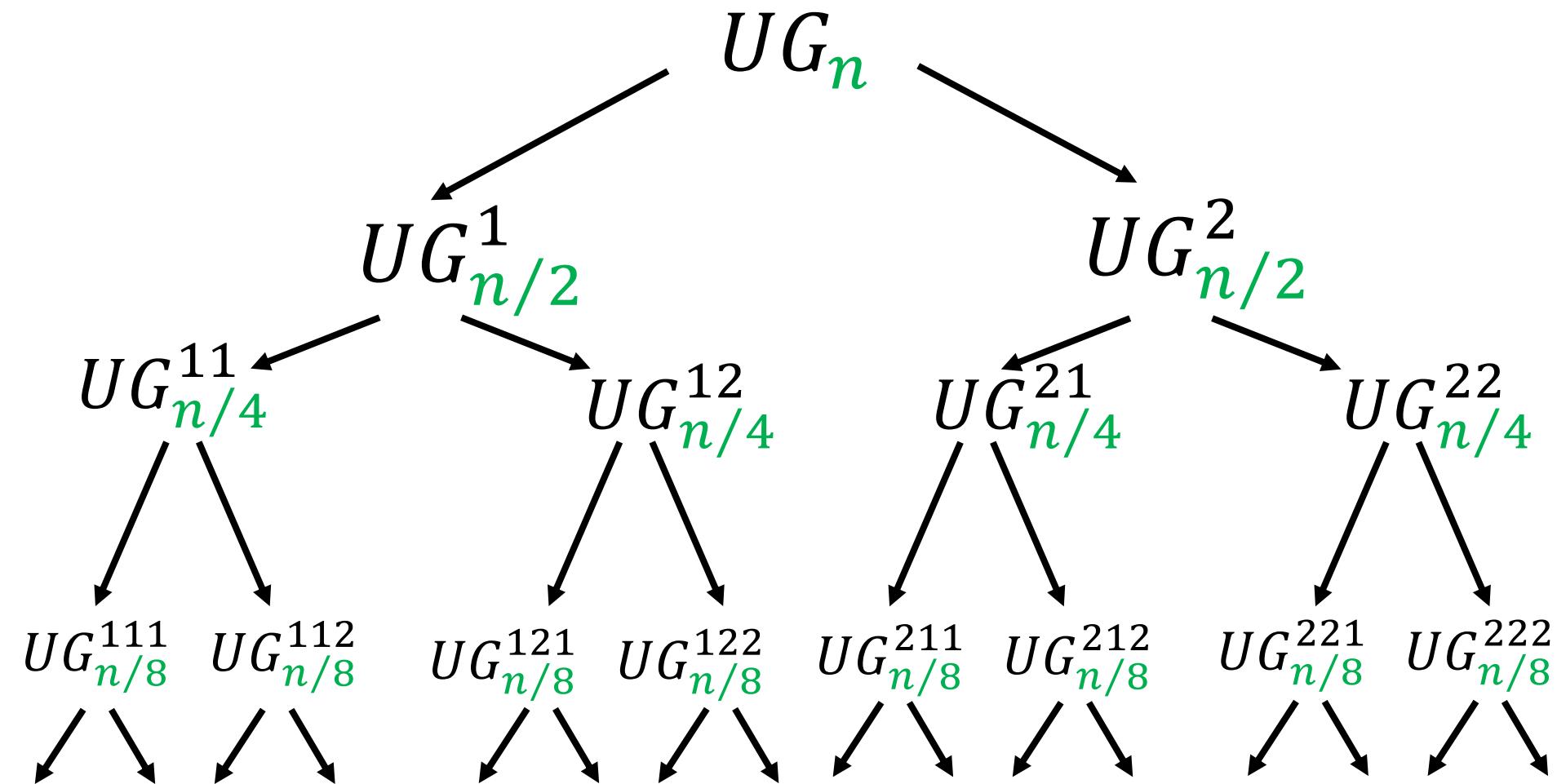
Recursive UG Construction



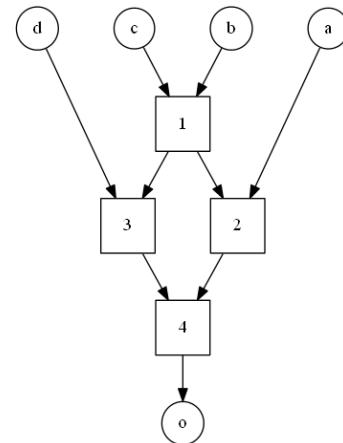
Recursive UG Construction



Recursive UG Construction

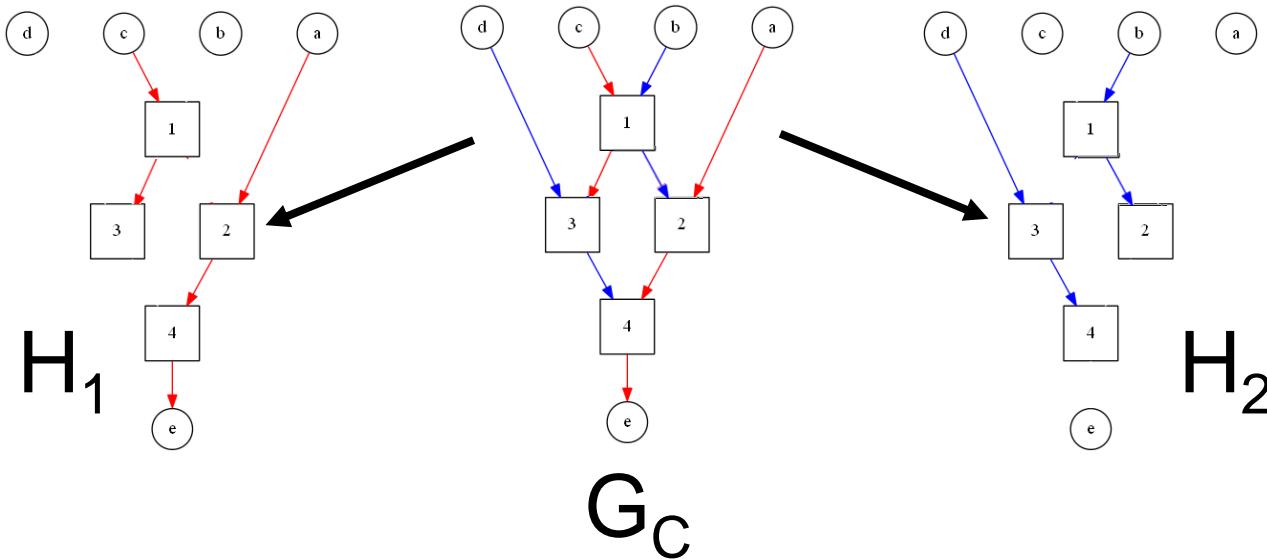


Edge-Embedding

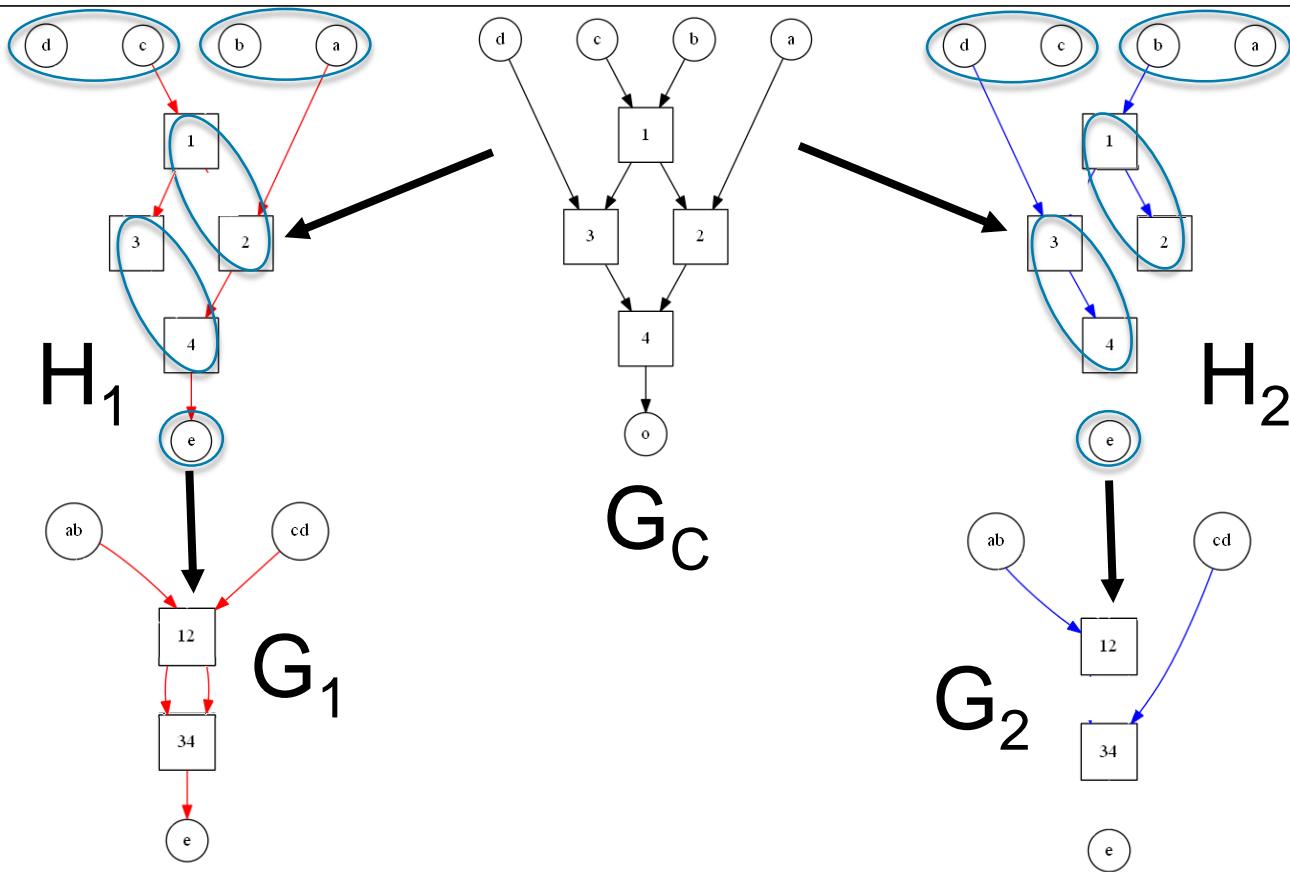


G_C

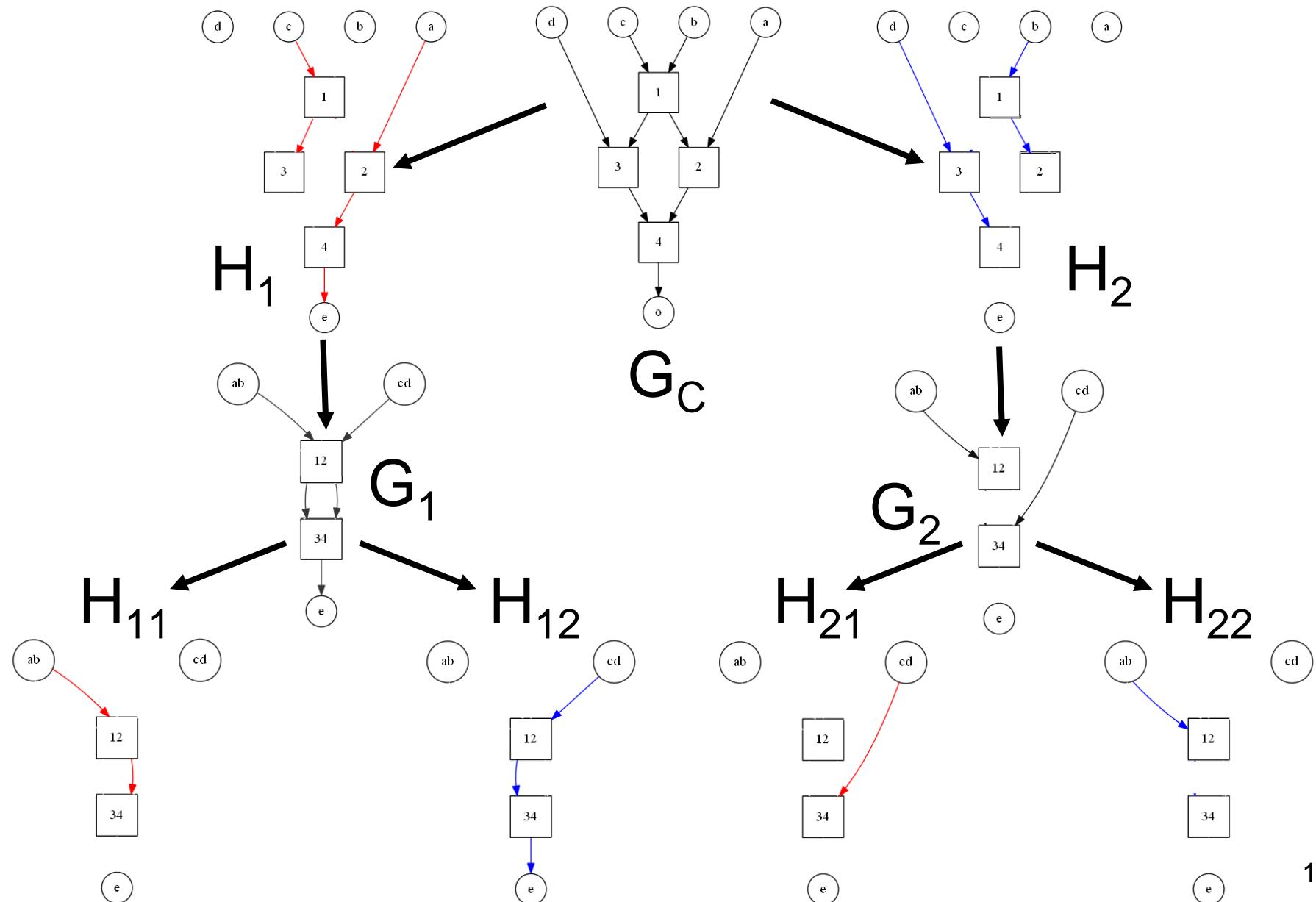
Edge-Embedding



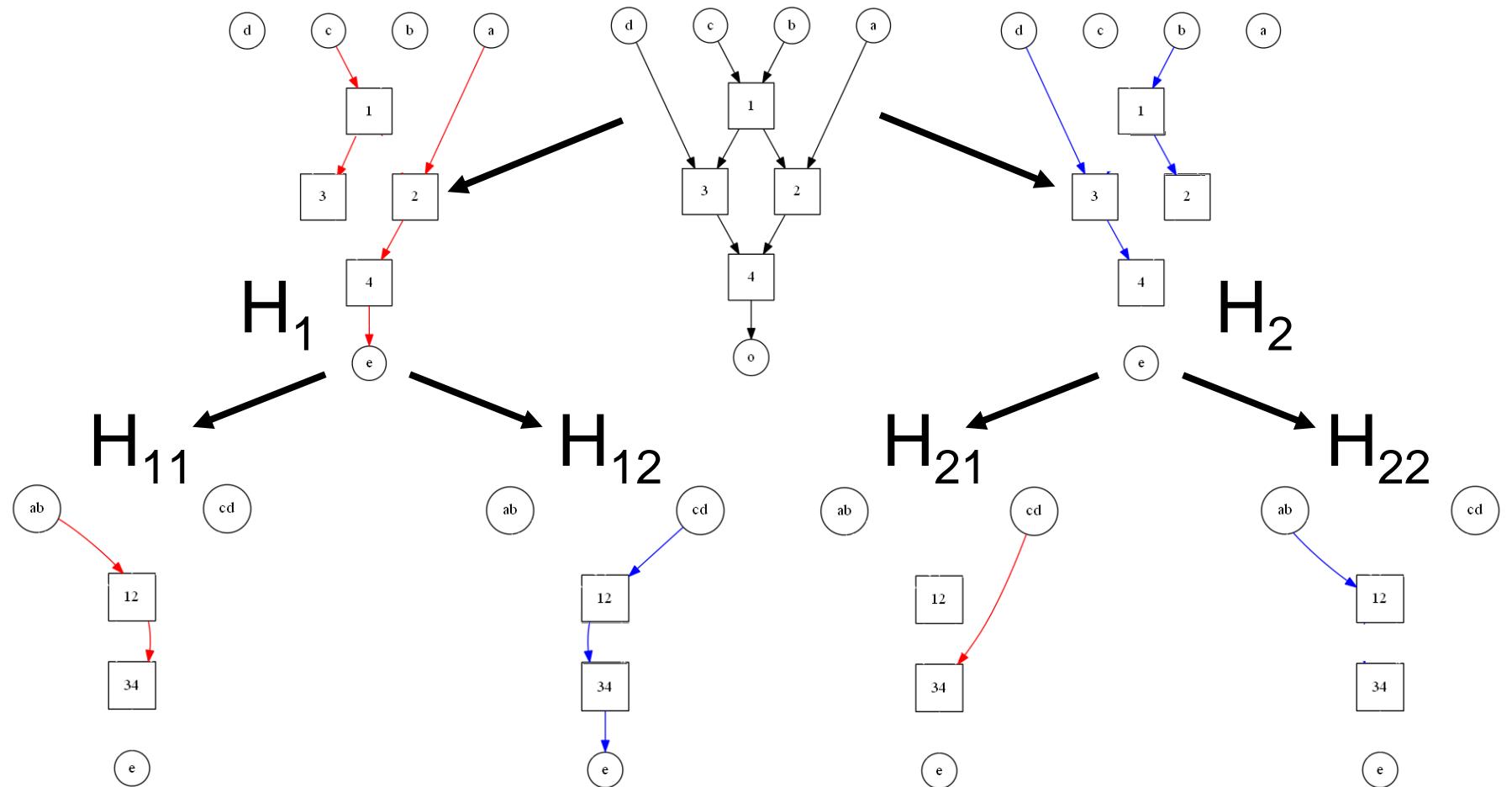
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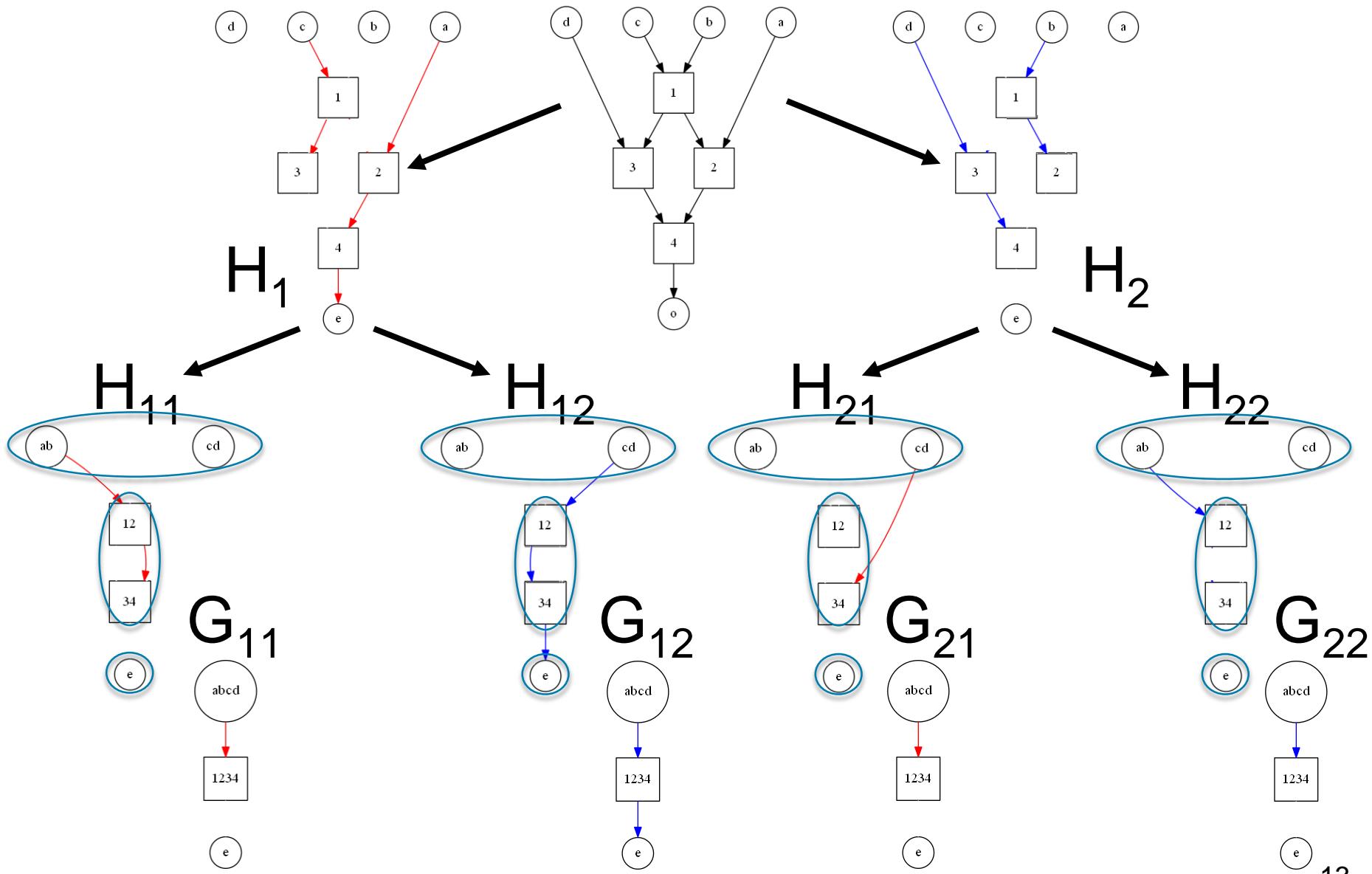
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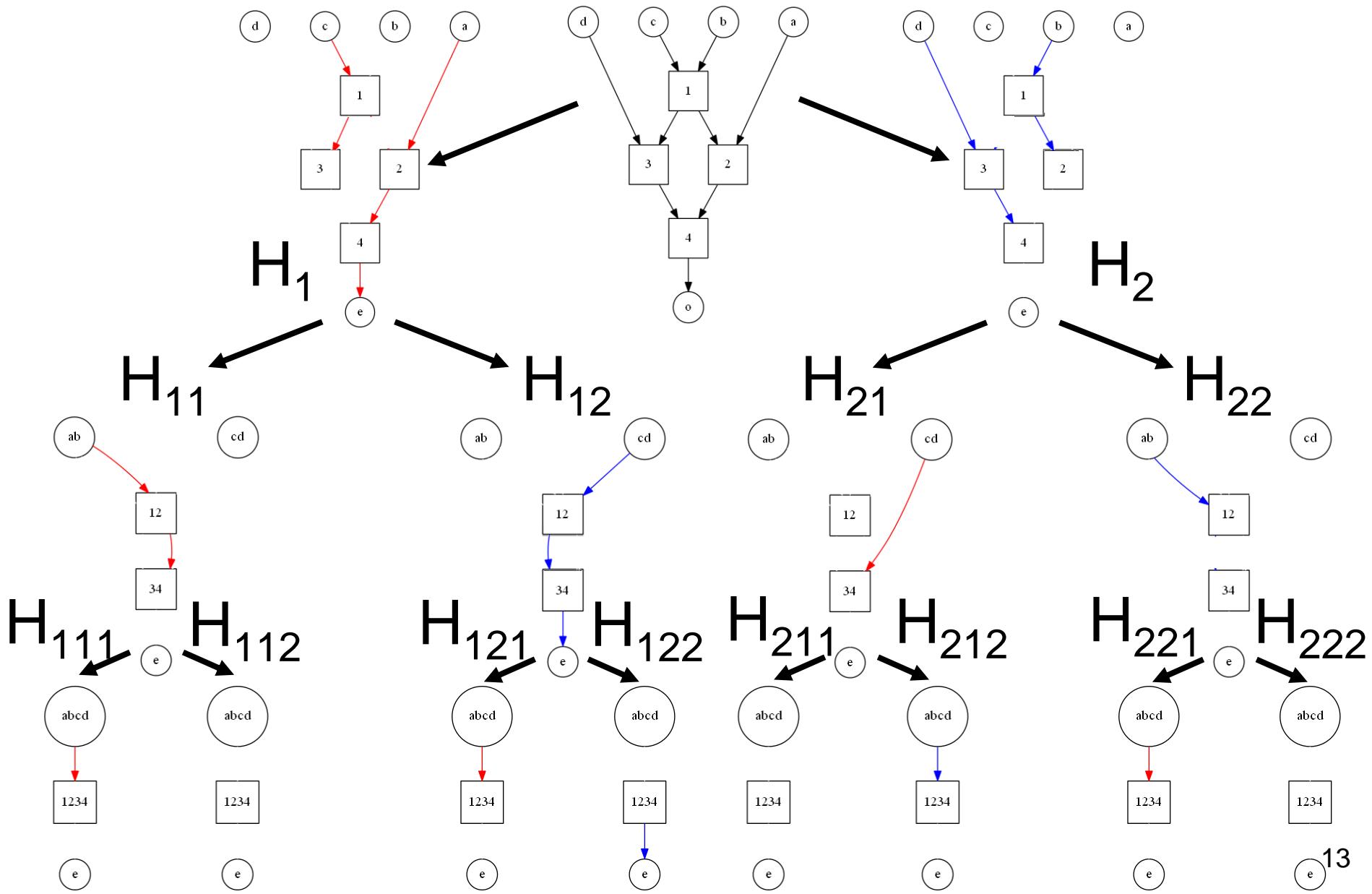
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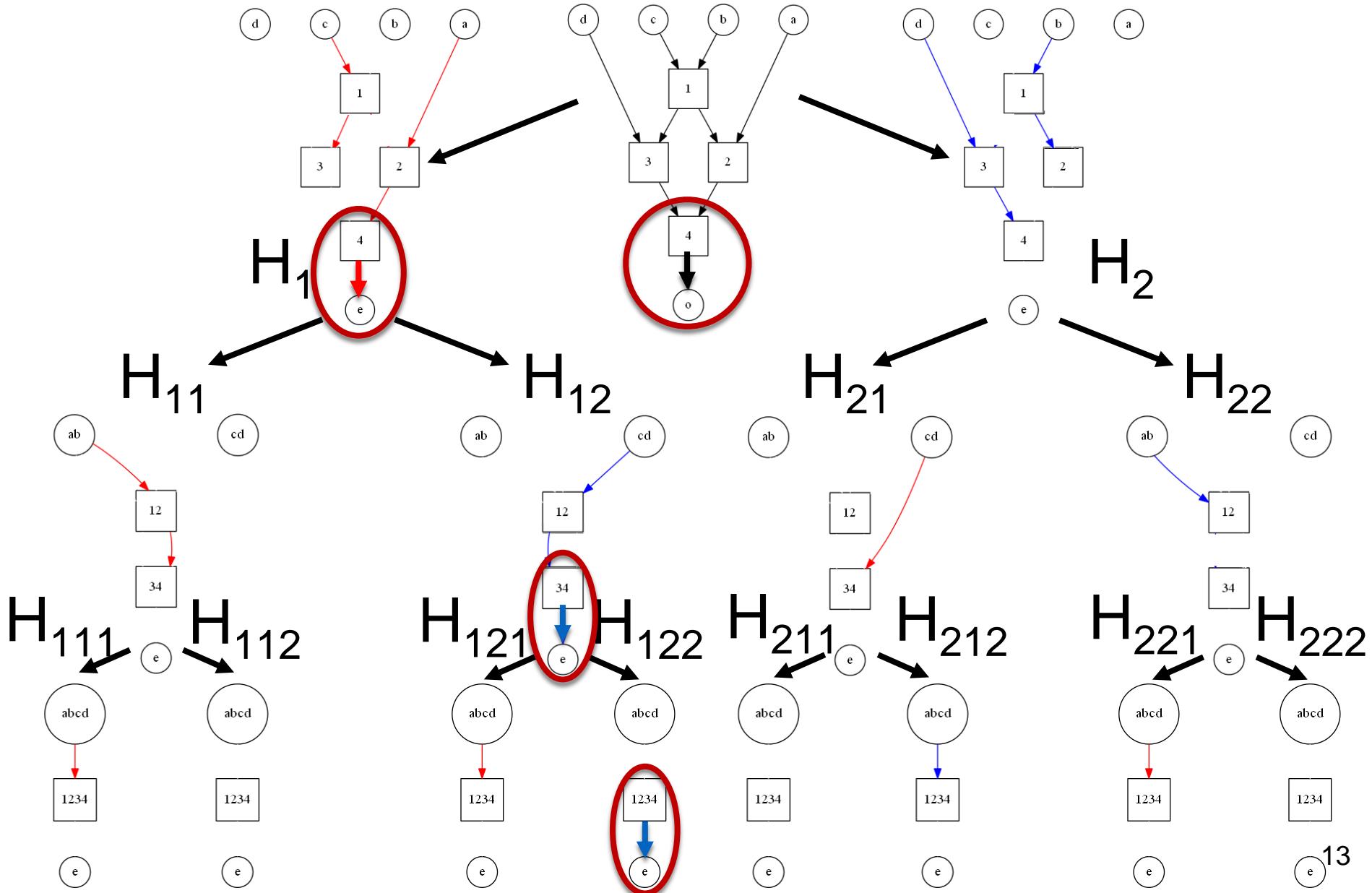
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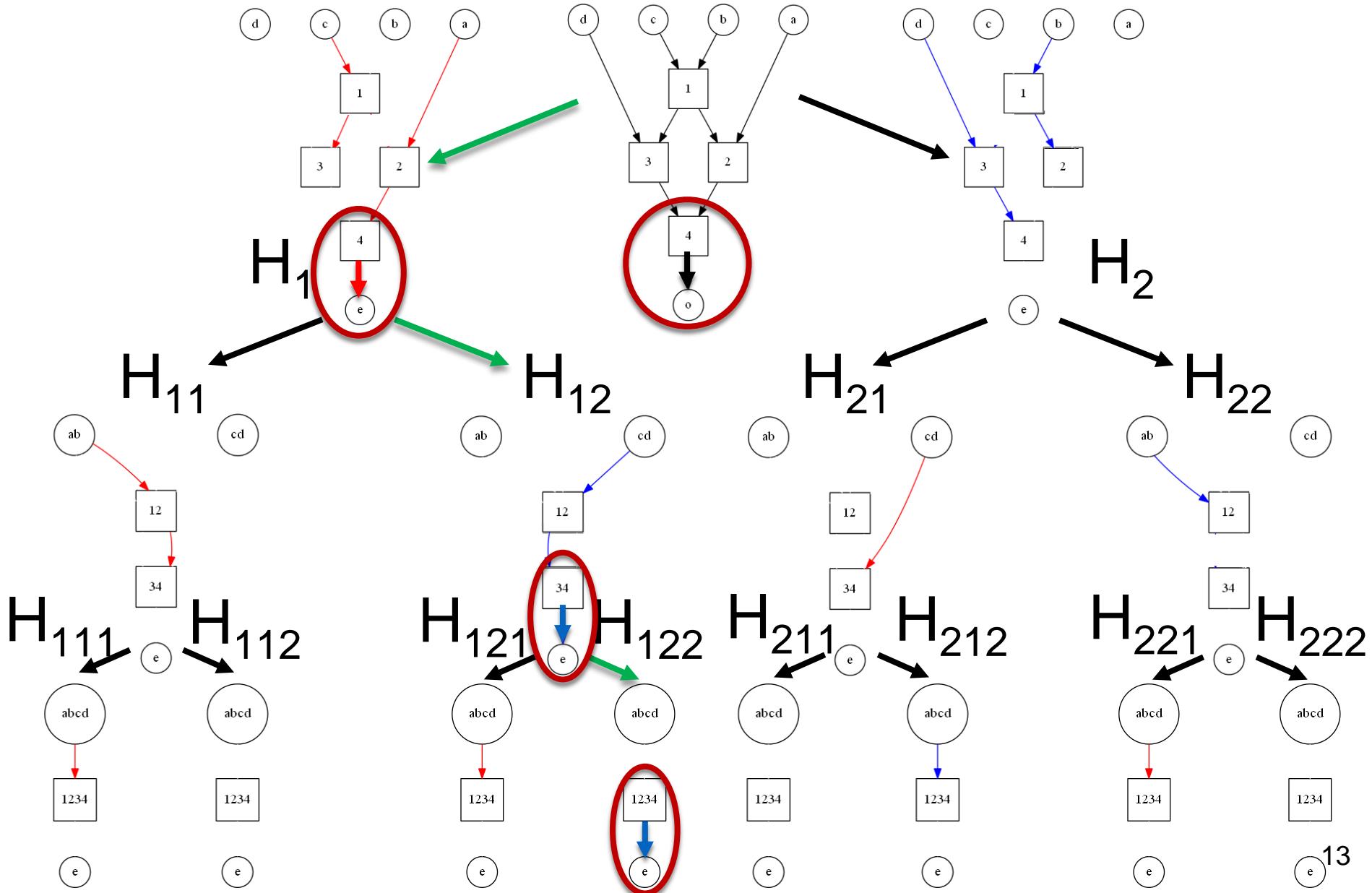
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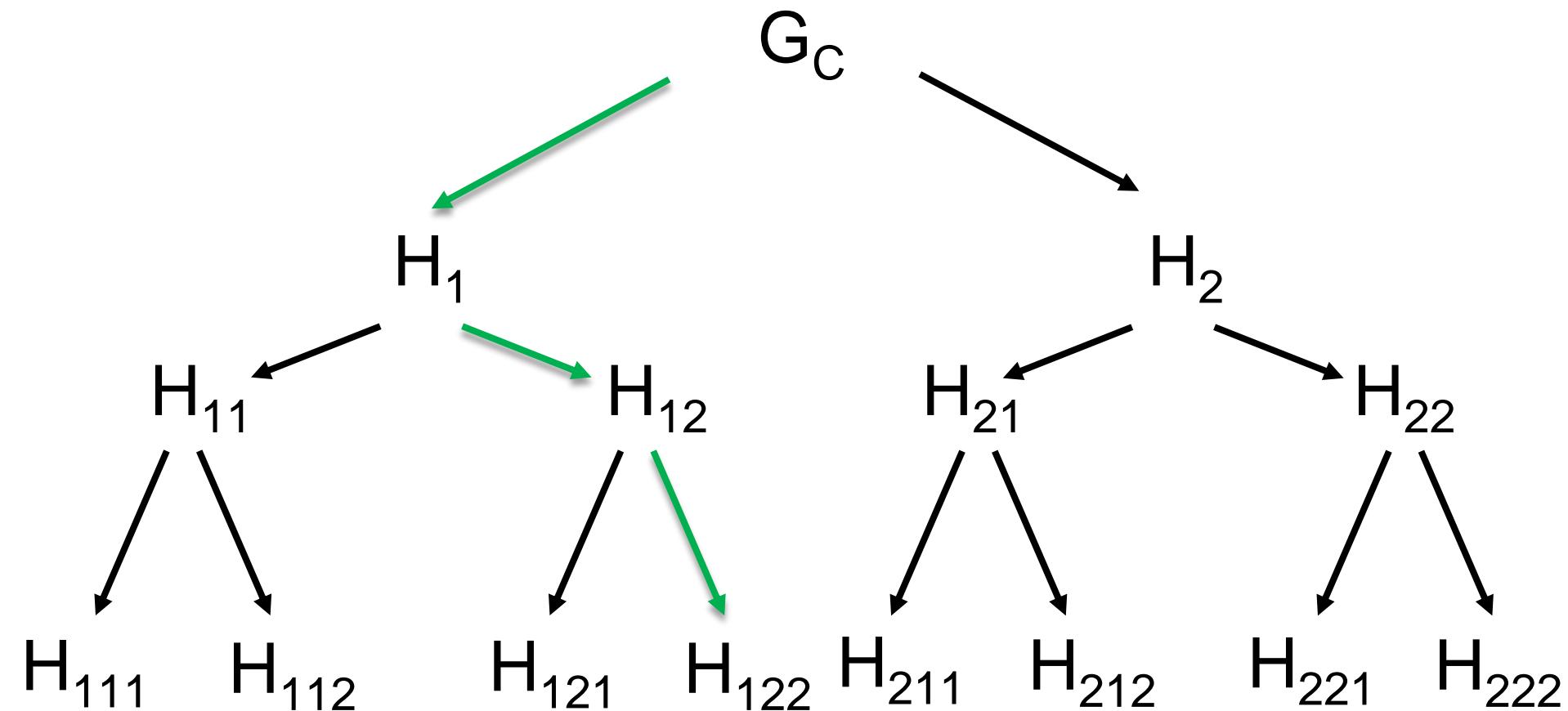
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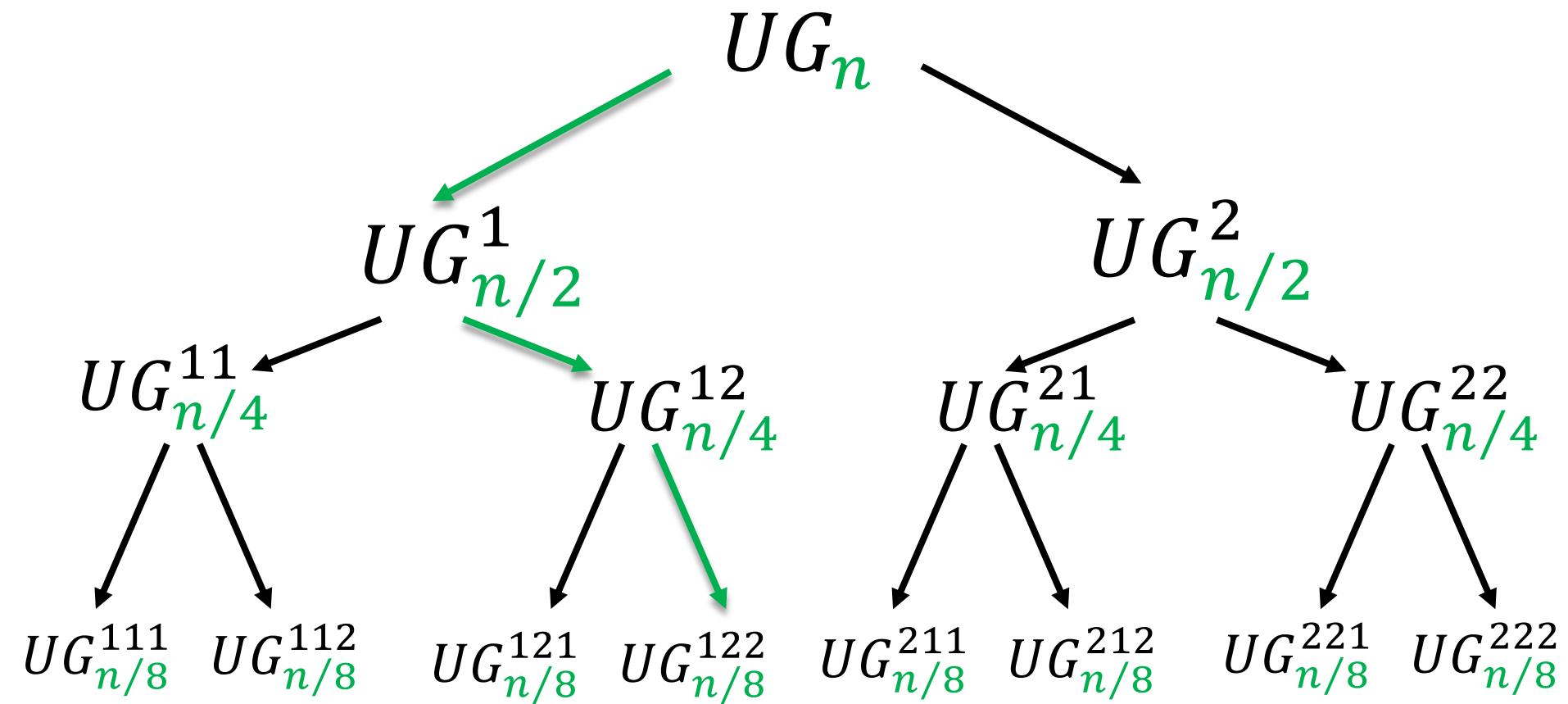
Edge-Embedding



Edge-Embedding



Recursive UG Construction



Our Contributions

Valiant's universal circuit is practical.



Embedding
algorithm

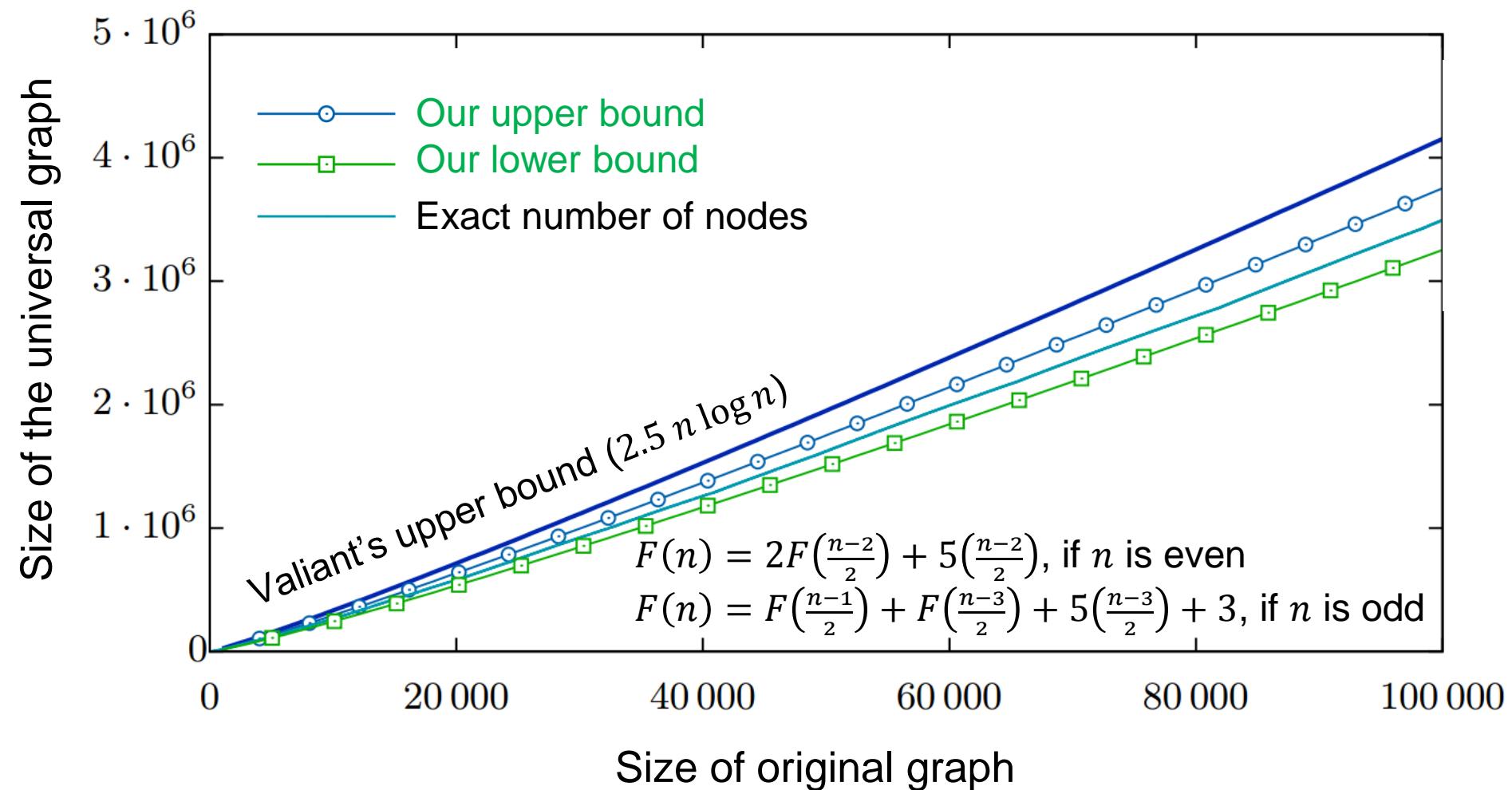


**Refined size of
construction**

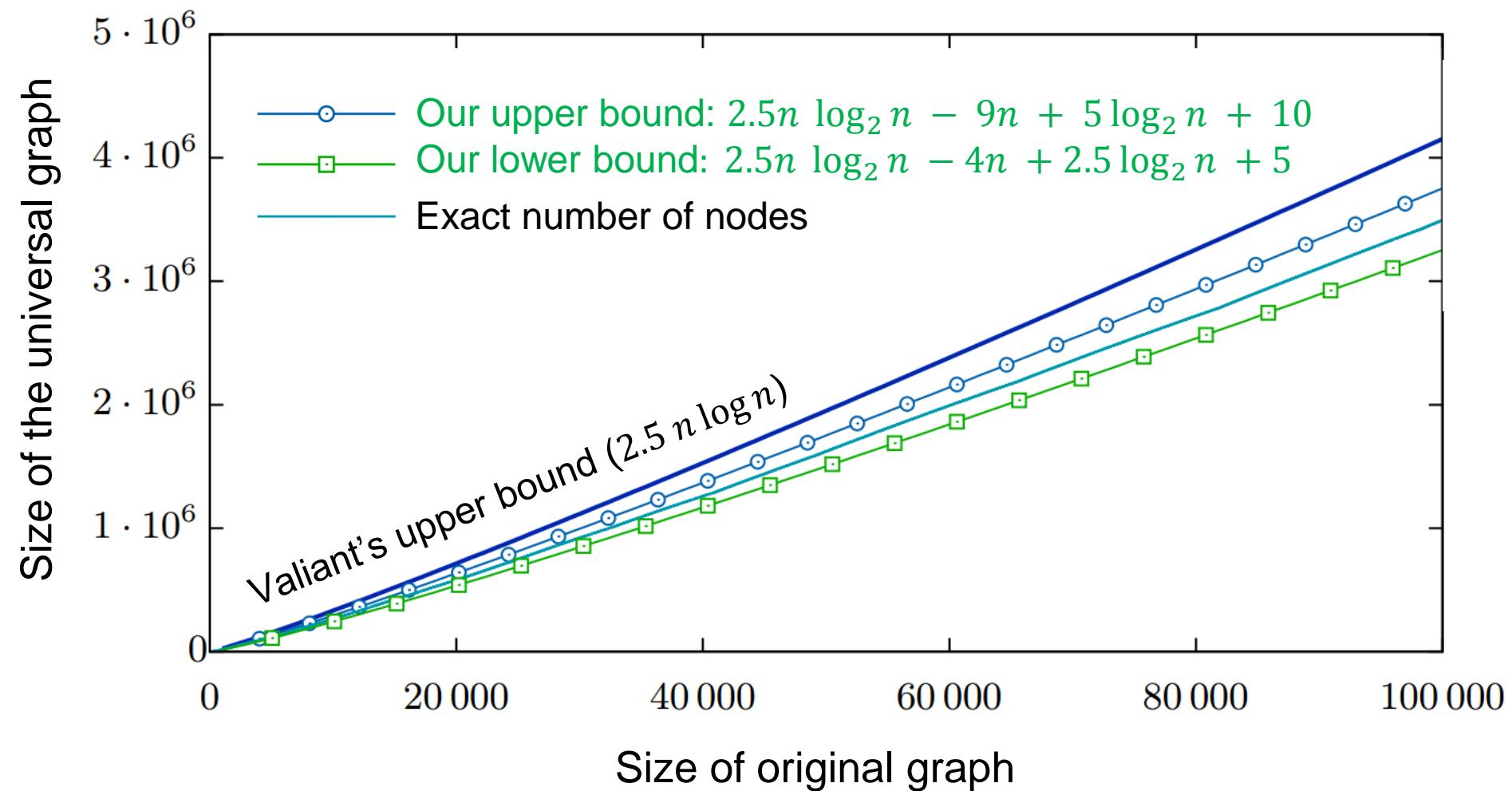


UC compiler

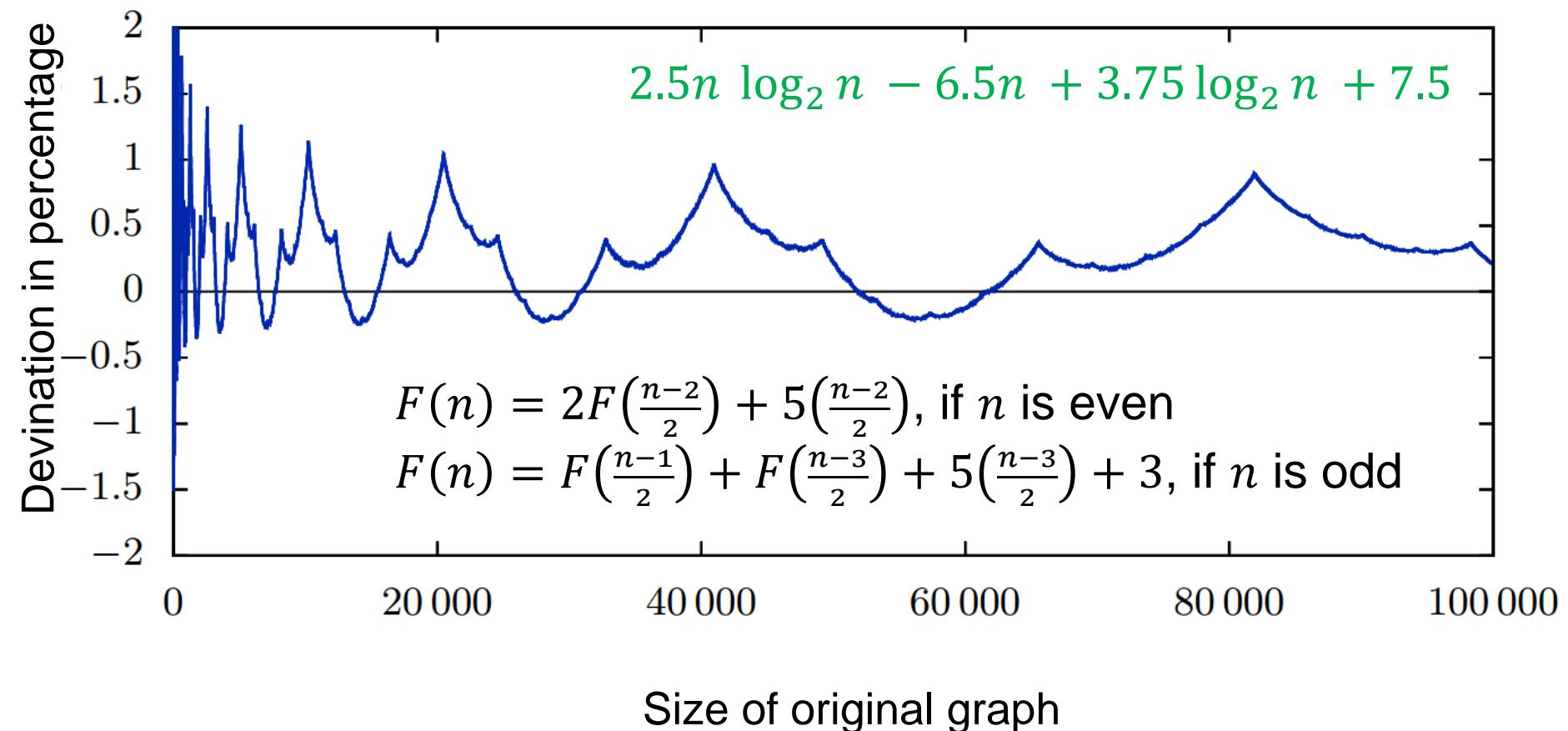
Size of Universal Graph



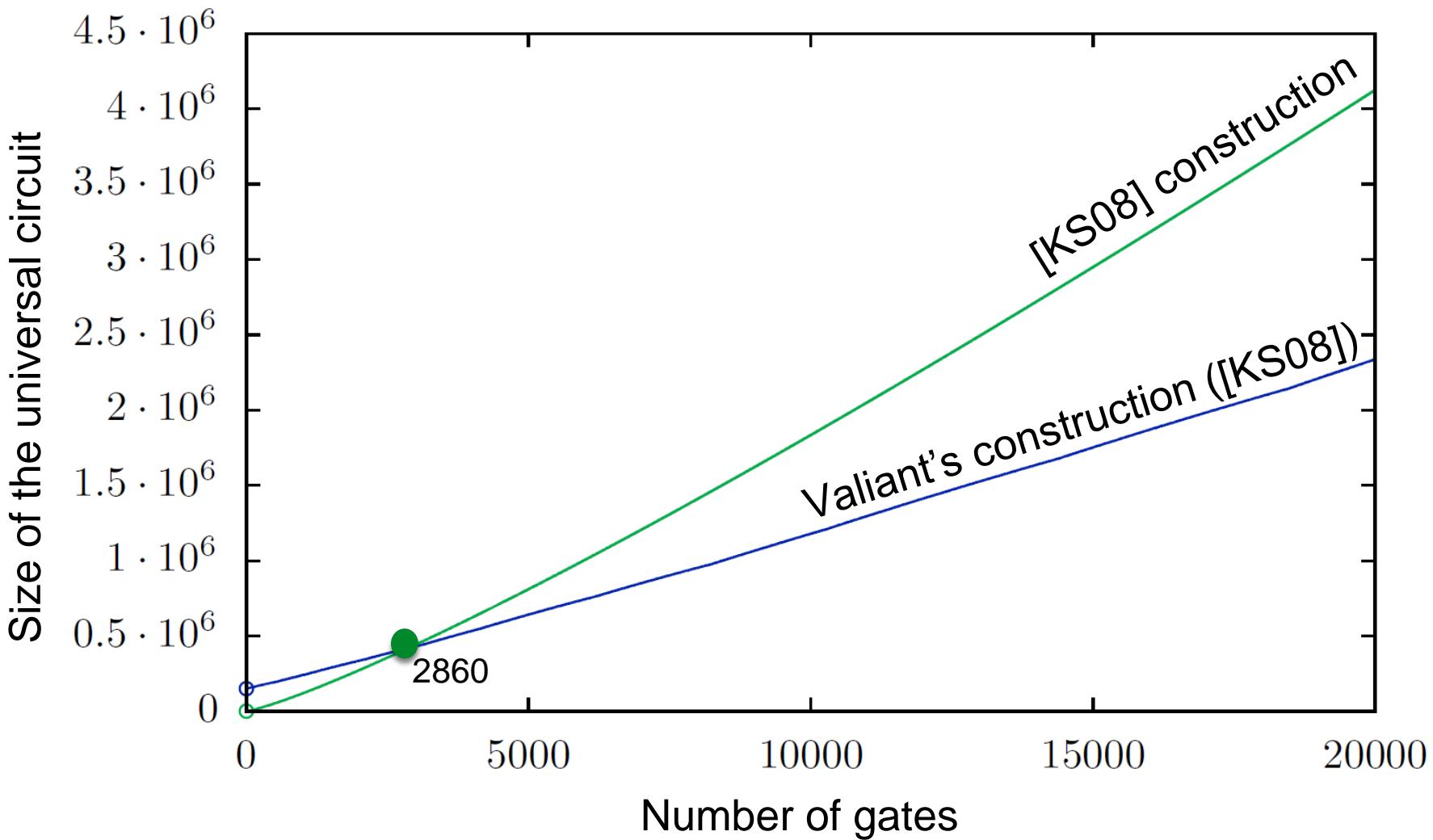
Size of Universal Graph



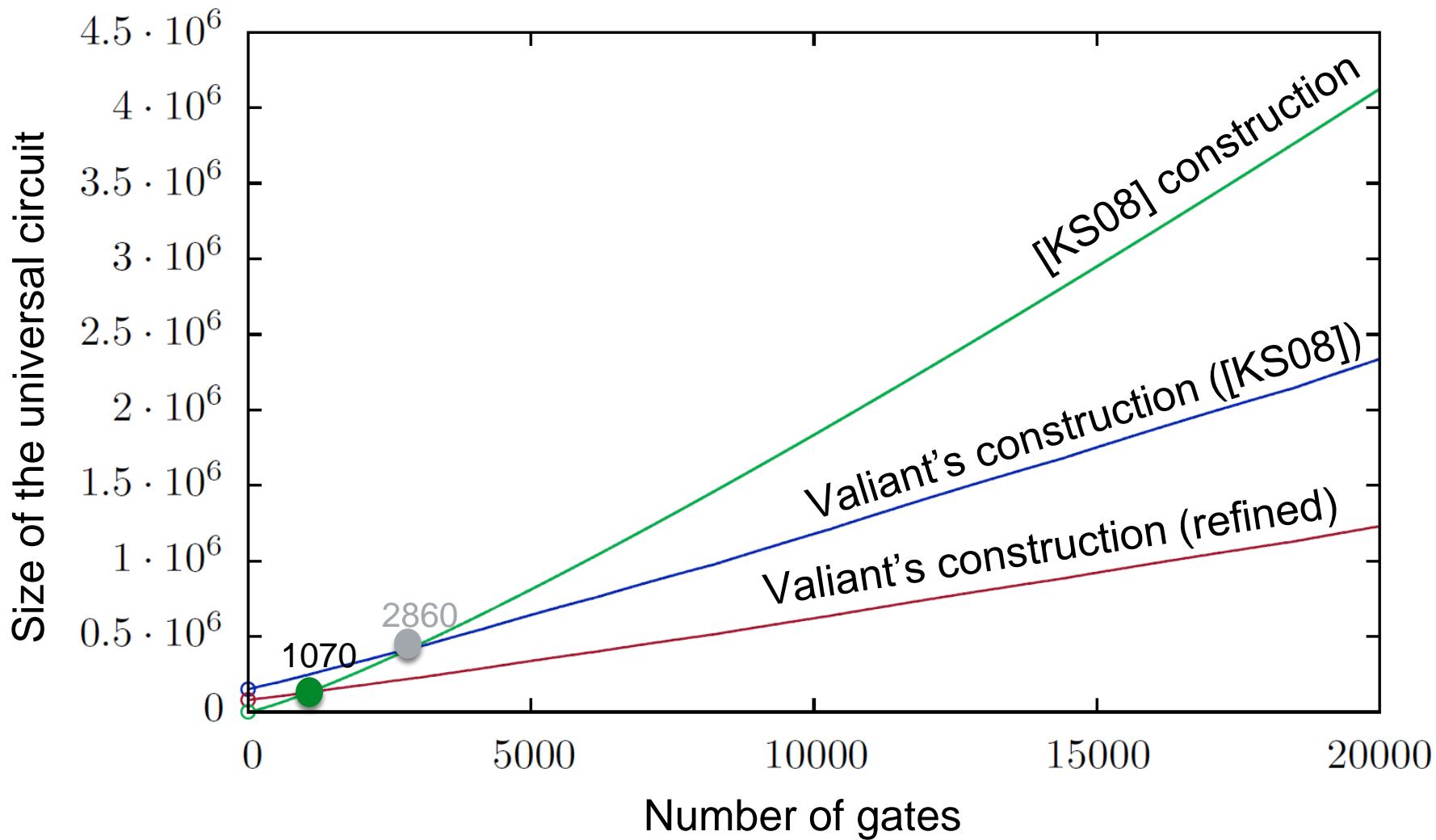
Deviation of Estimated Size and Exact Size



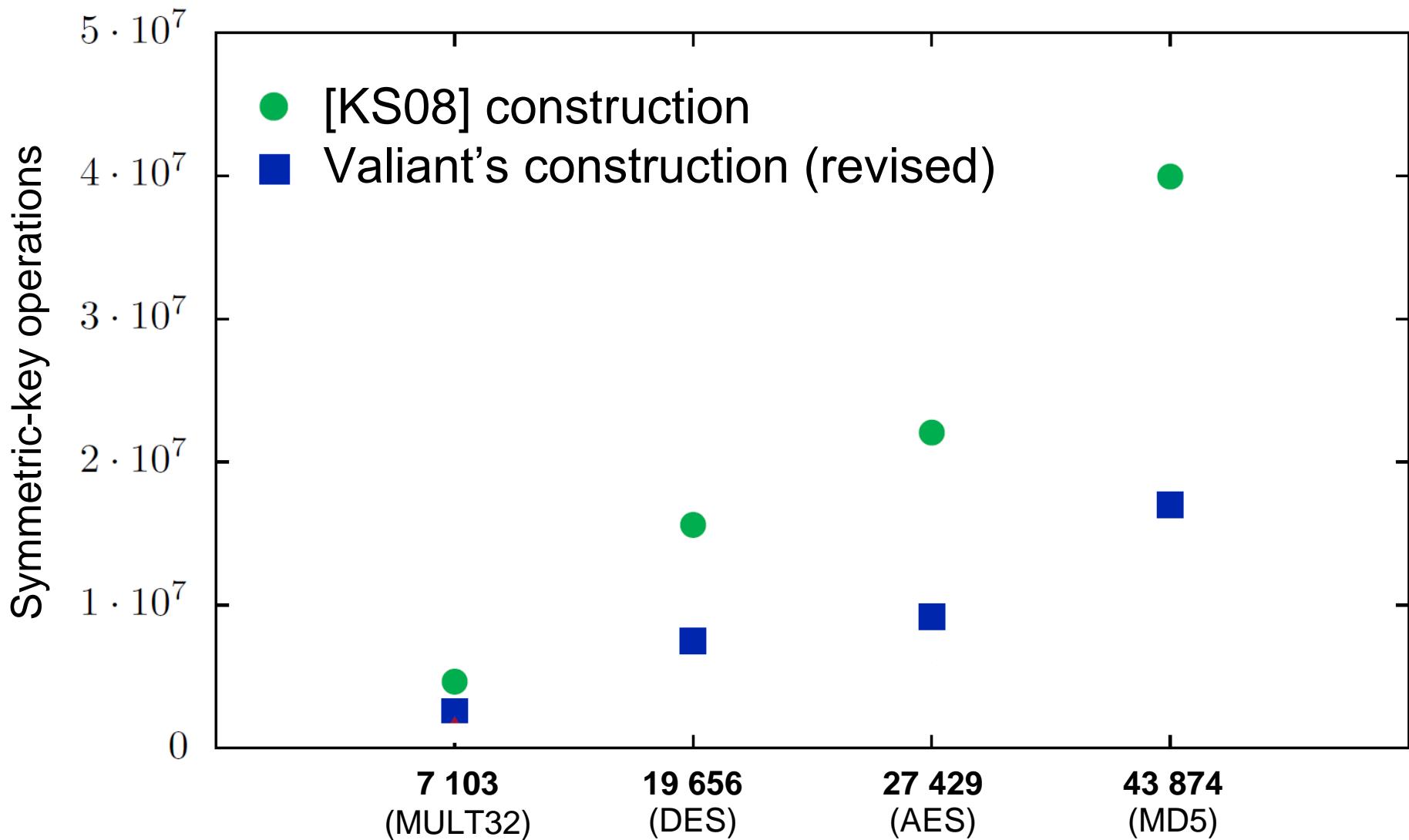
Size of the UC Constructions [KS08]



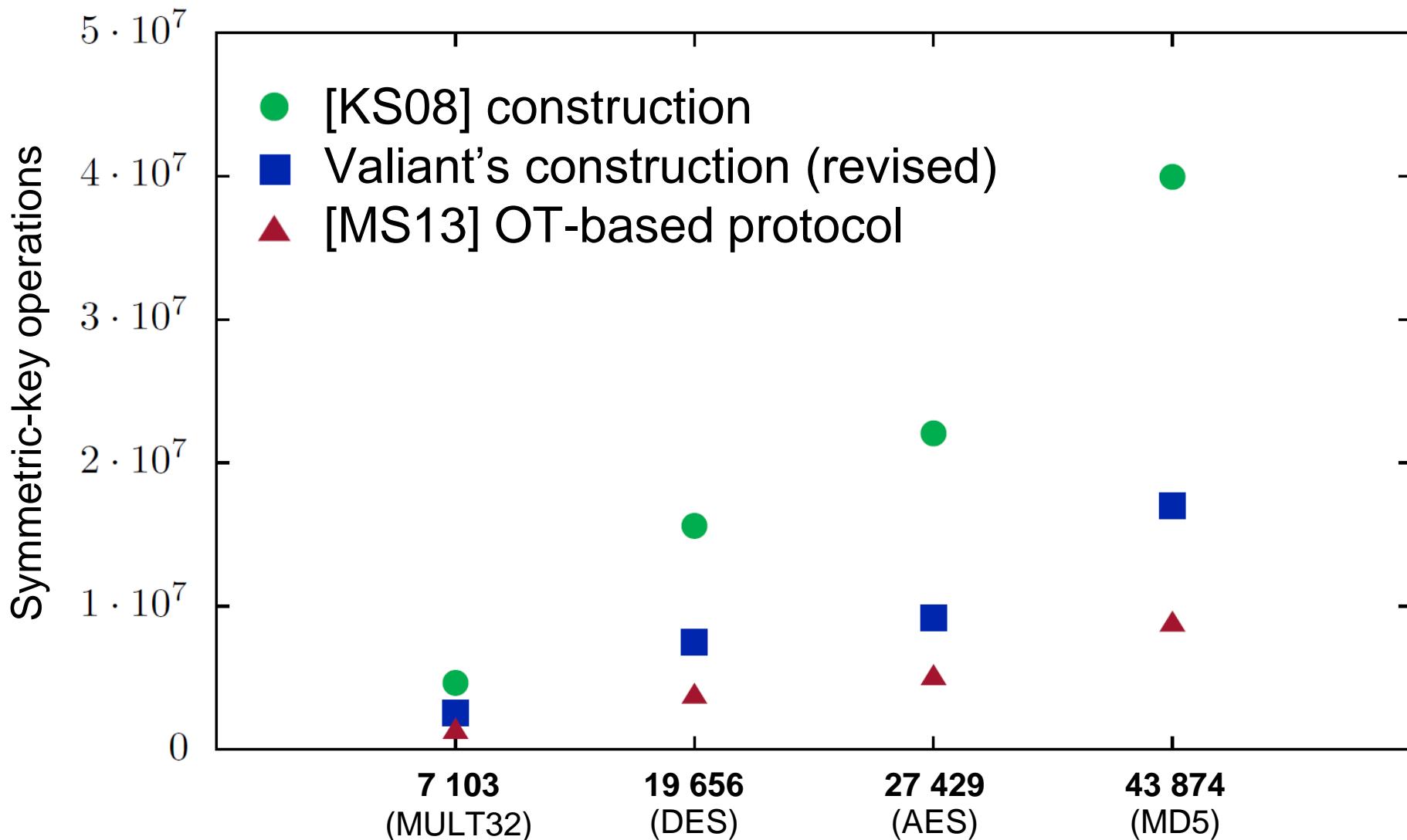
Revised size of the UC Constructions



PFE Comparison – Symmetric-Key Operations



PFE Comparison – Symmetric-Key Operations



[MS13]: P. Mohassel, S. S. Sadegian. How to hide circuits in MPC an efficient framework for private function evaluation. In *Eurocrypt 2013*.

Our Contributions

Valiant's universal circuit is practical.



Embedding
algorithm



Refined size of
construction



UC compiler

UC Implementation

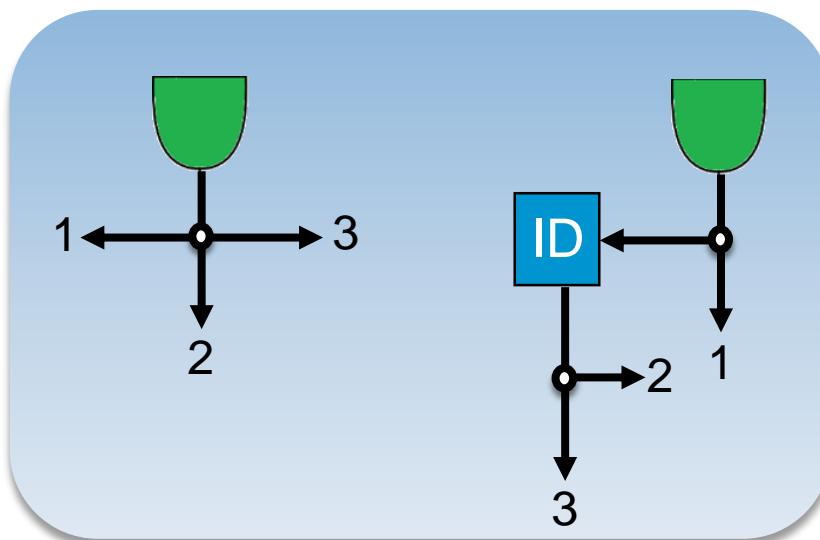
SHDL

$$C_0 \leftarrow f$$

[MNPS04] D. Malkhi, N. Nisan, B. Pinkas, Y. Sella. Fairplay-Secure Two-Party Computation System. In *USENIX Security Symposium* 2004.

UC Implementation

$$C \text{ size} \leq n \leftarrow C_0 \leftarrow f$$

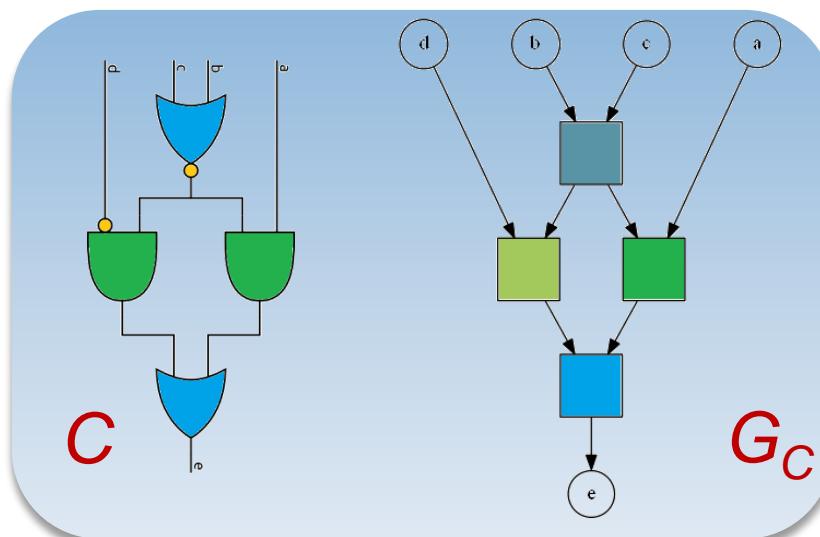


UC Implementation

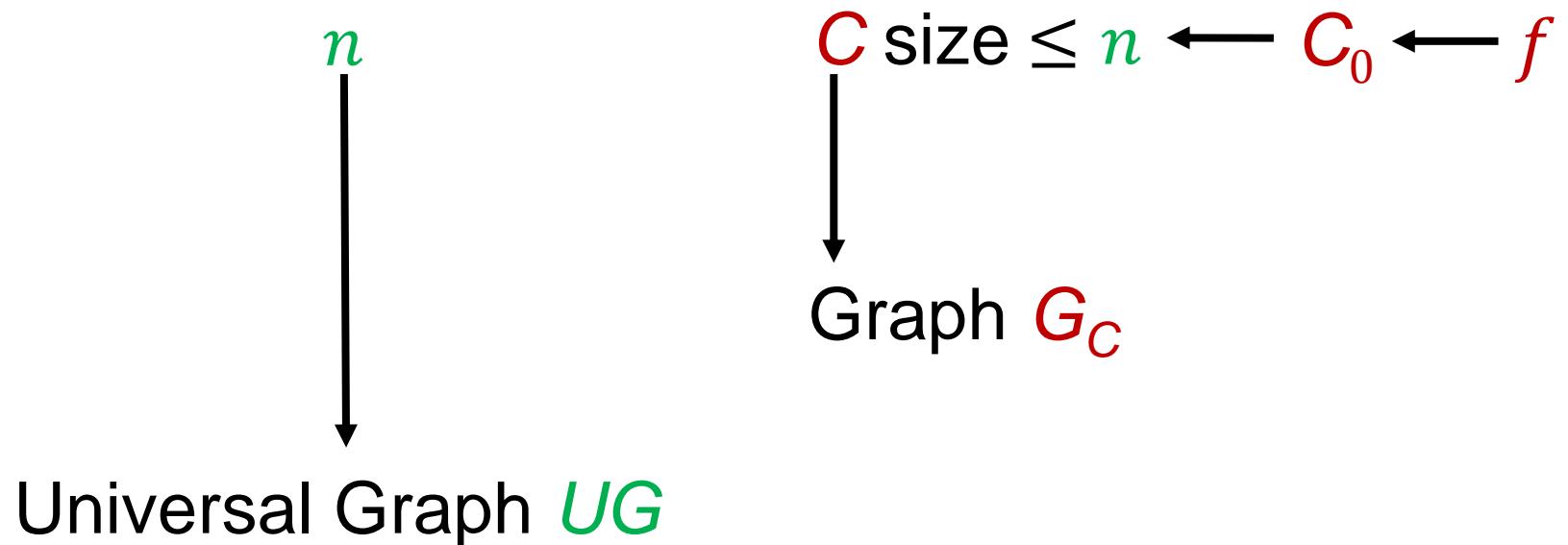
$C \text{ size} \leq n \leftarrow C_0 \leftarrow f$

↓

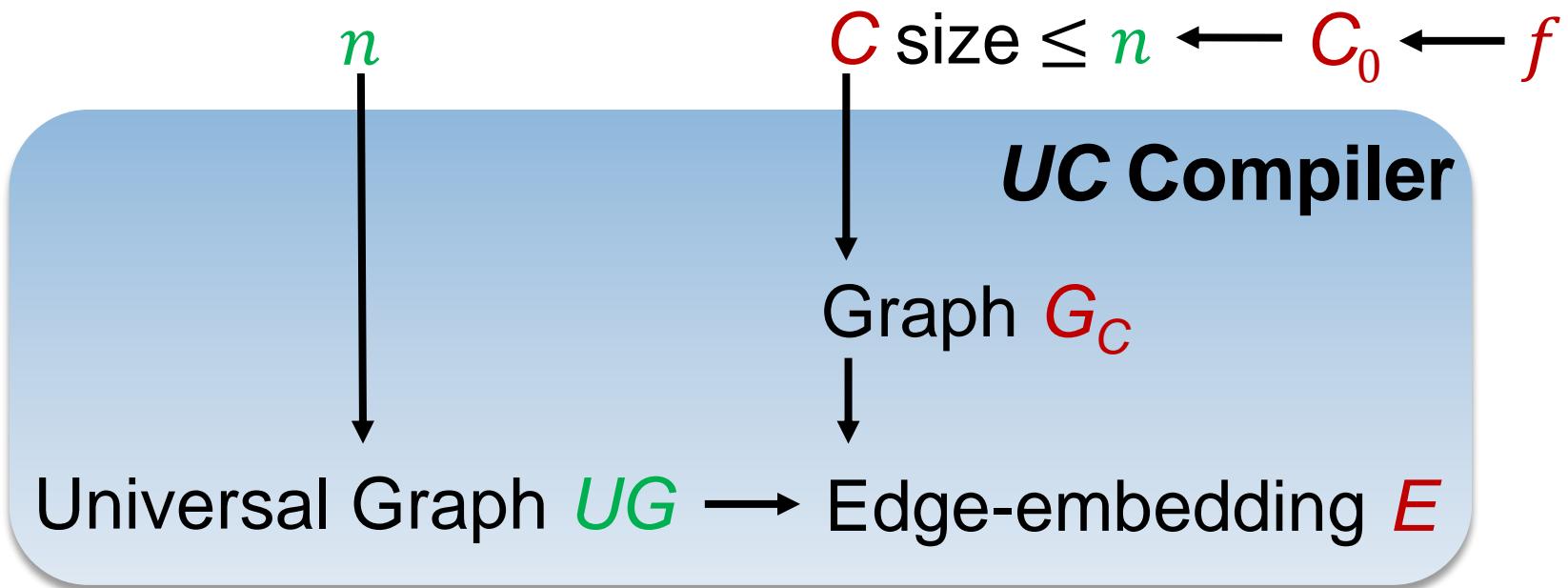
Graph G_C



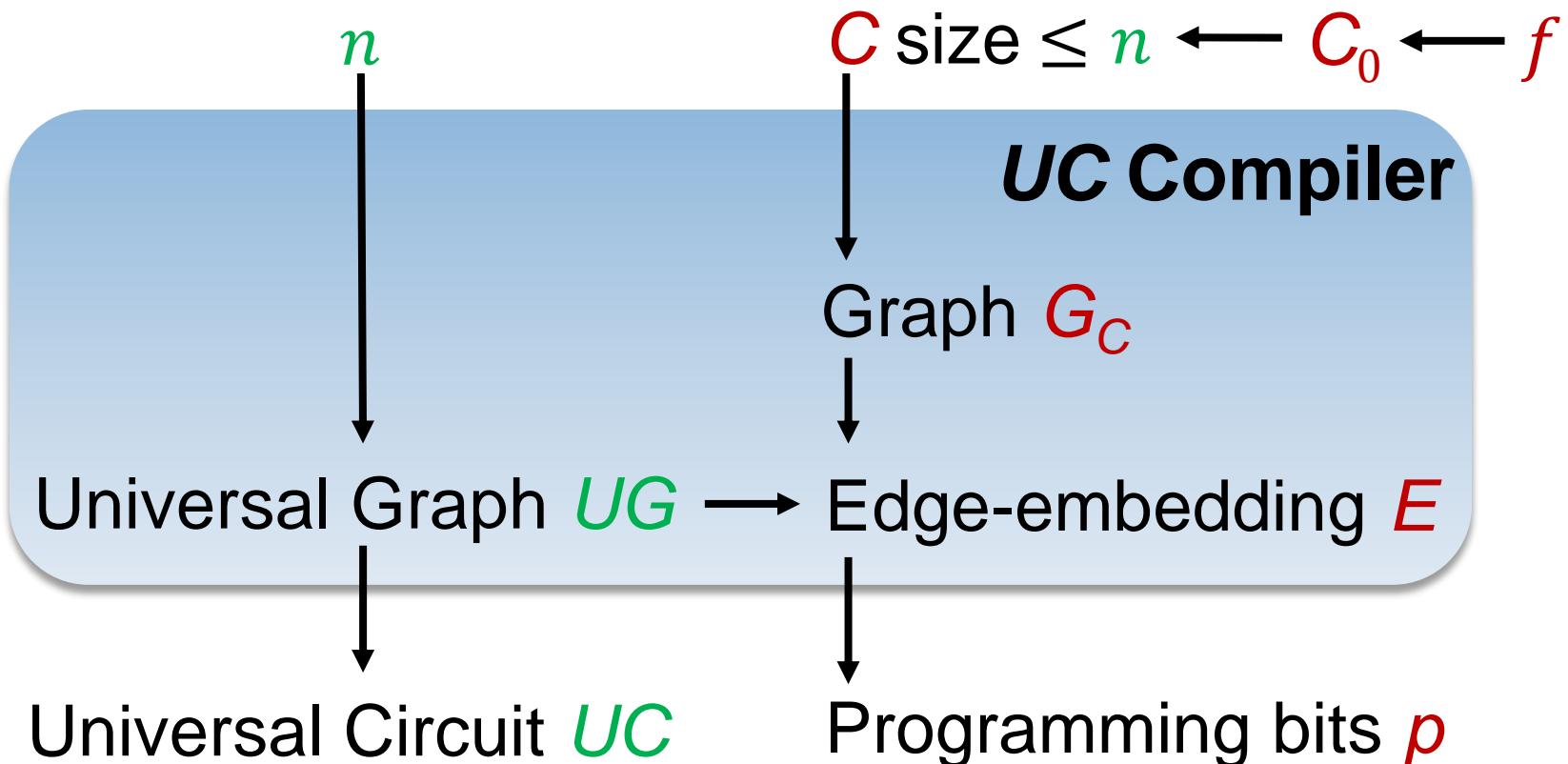
UC Implementation



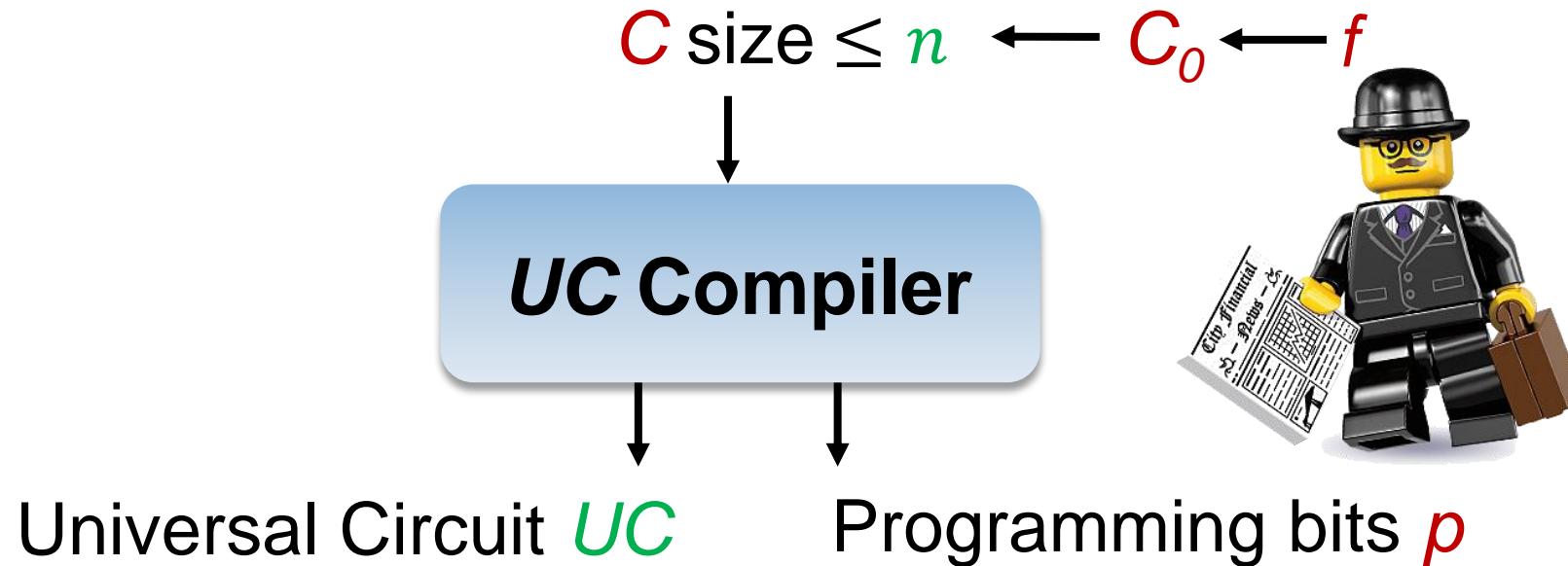
UC Implementation



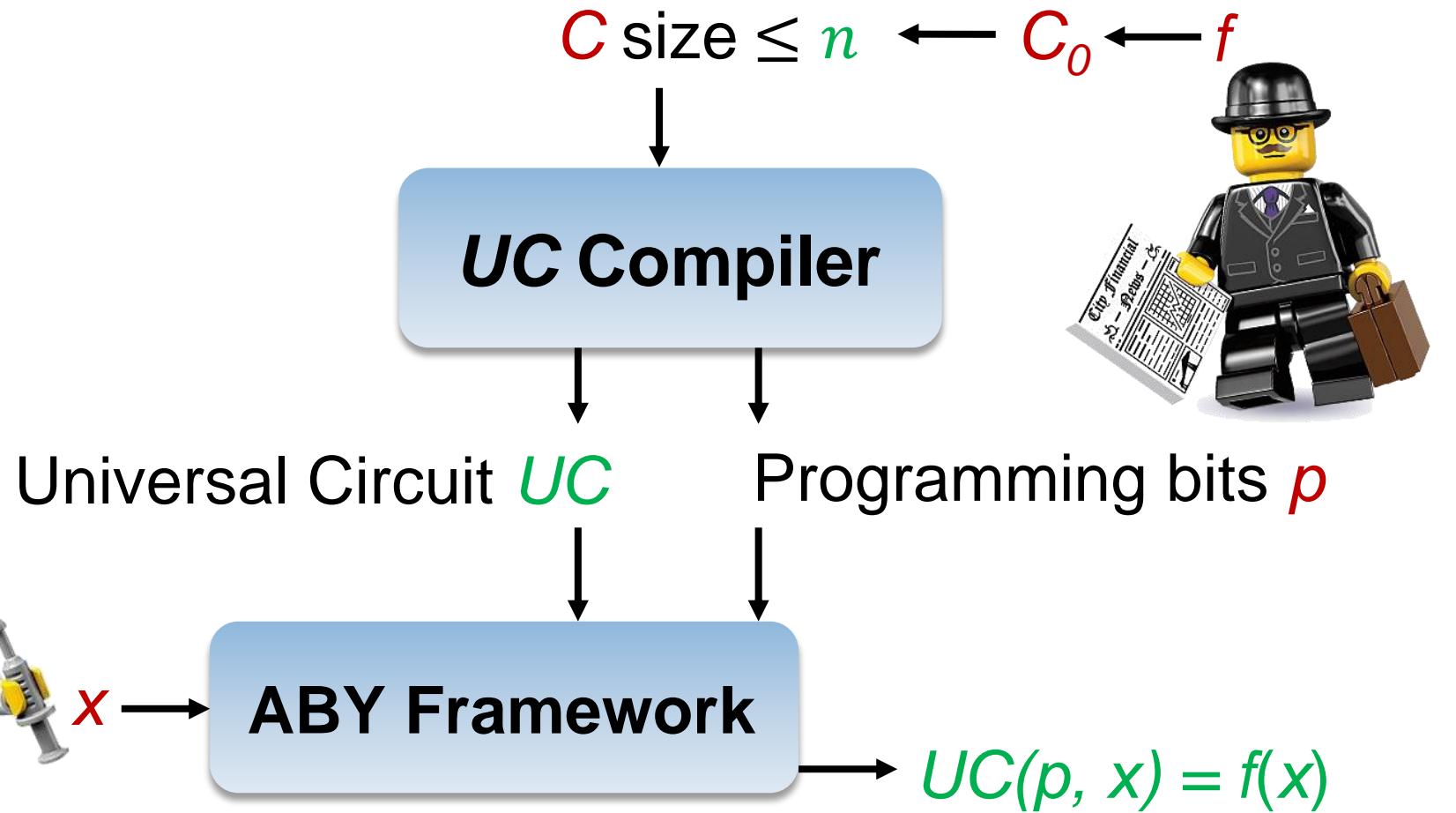
UC Implementation



PFE Implementation



PFE Implementation



[DSZ15] D. Demmler, T. Schneider, M. Zohner.

ABY—a framework for efficient mixed-protocol secure two-party computation. In NDSS 2015. 23

Experimental Results – UC Compiler

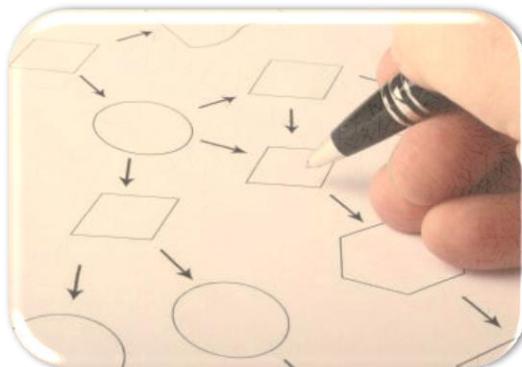
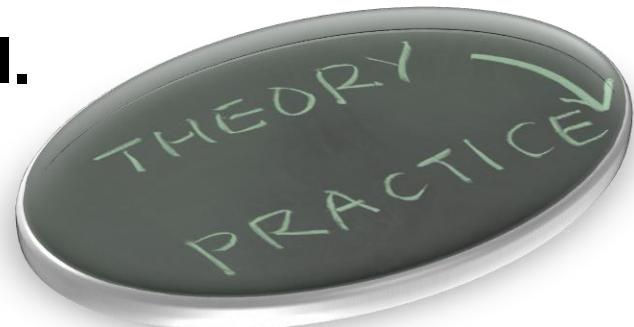
UC Compiler

ABY Framework

Private function (circuit size)	UC Compile (ms)	UC I/O (ms)	PFE (GMW) (ms)	PFE (Yao) (ms)
MULT32 7 103	329	1443	1092	540
DES 19 656	1596	4174	2695	1311
AES 27 429	2104	5064	5522	2349
MD5 43 874	4043	8785	7041	3548

Conclusion

Valiant's universal circuit is practical.



Embedding
algorithm



Refined size of
construction

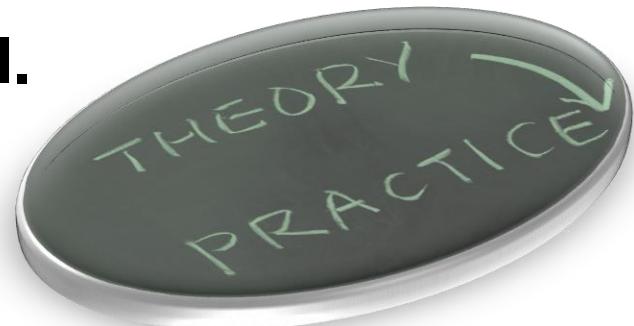


UC compiler

Conclusion

Valiant's universal circuit is practical.

Thank you for your attention!



Embedding
algorithm



Refined size of
construction



UC compiler

References

- [Val76] L. G. Valiant: Universal circuits (preliminary report). In *STOC 1976*.
- [KS08] V. Kolesnikov, T. Schneider: A practical universal circuit construction and secure evaluation of private functions. In *FC 2008*.
- [MNPS04] D. Malkhi, N. Nisan, B. Pinkas, Y. Sella. Fairplay-Secure Two-Party Computation System. In *USENIX Security Symposium 2004*.
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