

On the Indifferentiability of the Sponge Construction

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Introduction

- Sponge functions model
 - the **finite state** of iterated cryptographic functions
 - as in iterated hash functions, stream ciphers, etc.
- Random sponges can be used
 - as a reference for (hash function) design
 - as an inspiration for (hash function) design
- Sponges are **simple**

Outline

✓ Introduction

❑ Definitions

❑ Uses Examples

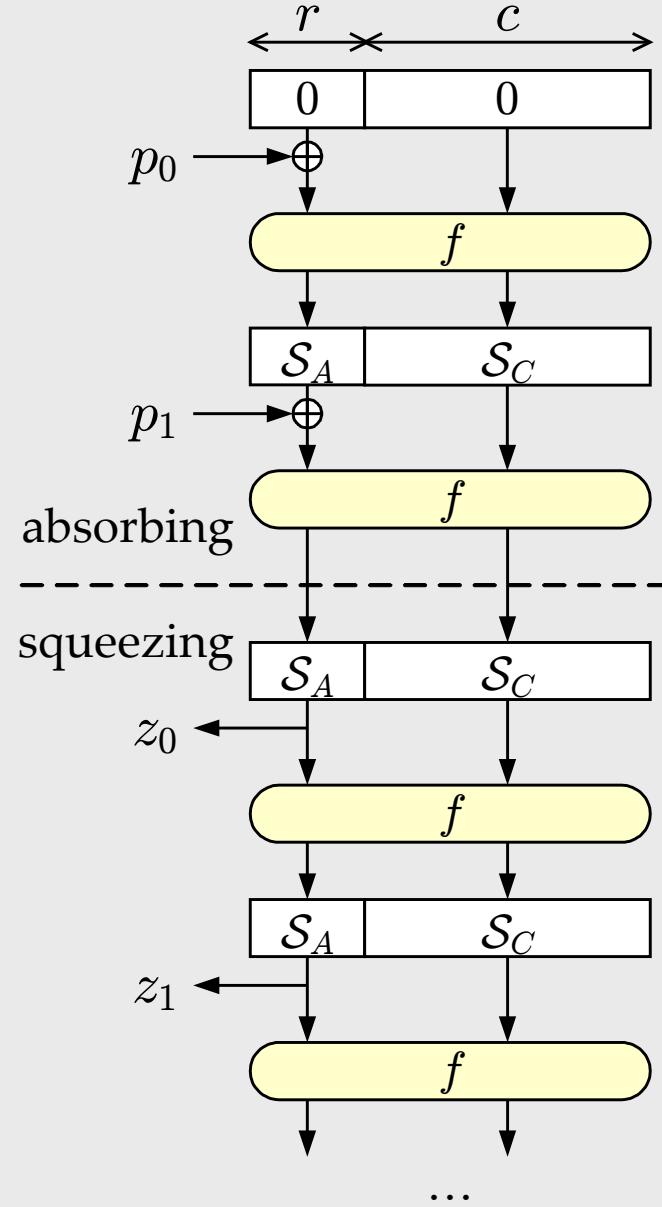
❑ Indifferentiability

❑ Constructing a sponge function

❑ Conclusion

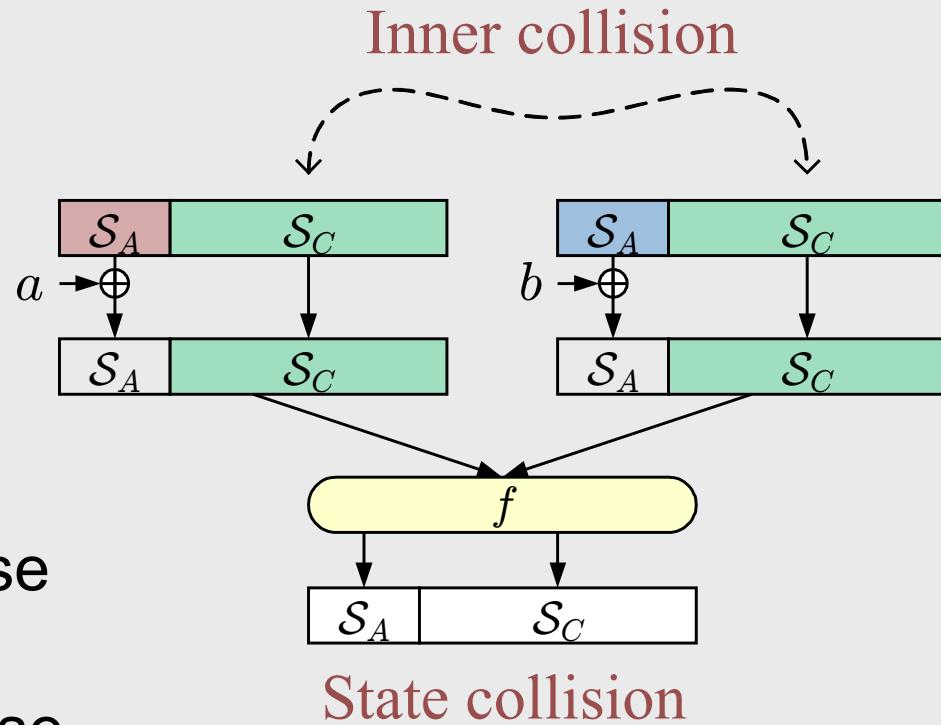
Sponge Construction

*The last absorbed block
must not be zero.*



Inner Collisions, State Collisions

- State collision
 - Absorbing phase
 - Hash collision
 - Squeezing phase
 - Output periodicity



Random Sponges

- Random **T**-sponge
 - Randomly chosen in $(2^{c+r})^{2^{c+r}}$ **transformations** f
- Random **P**-sponge
 - Randomly chosen in $(2^{c+r})!$ **permutations** f

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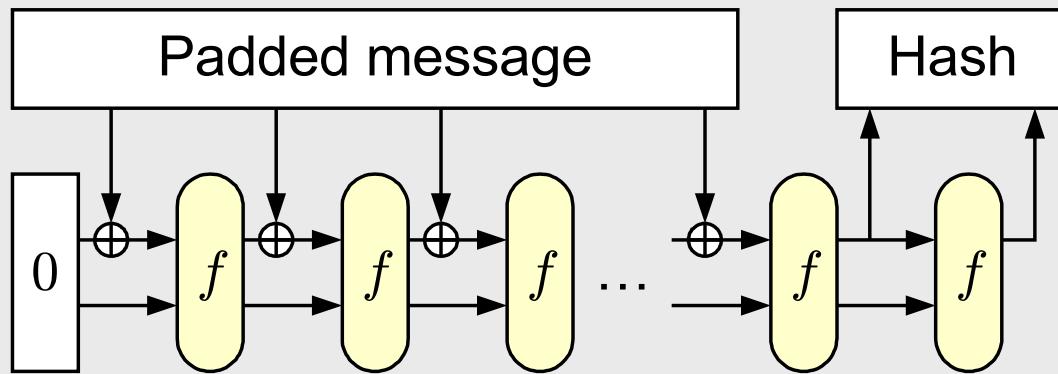
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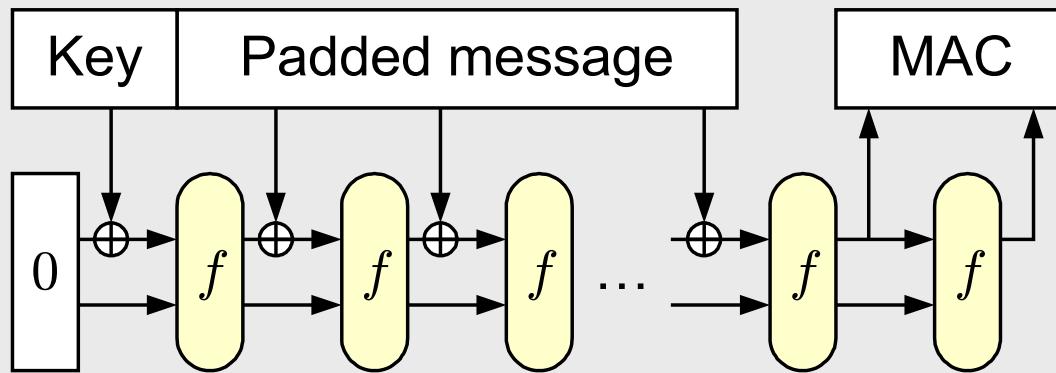
Uses Examples (1/5)

- Hash function



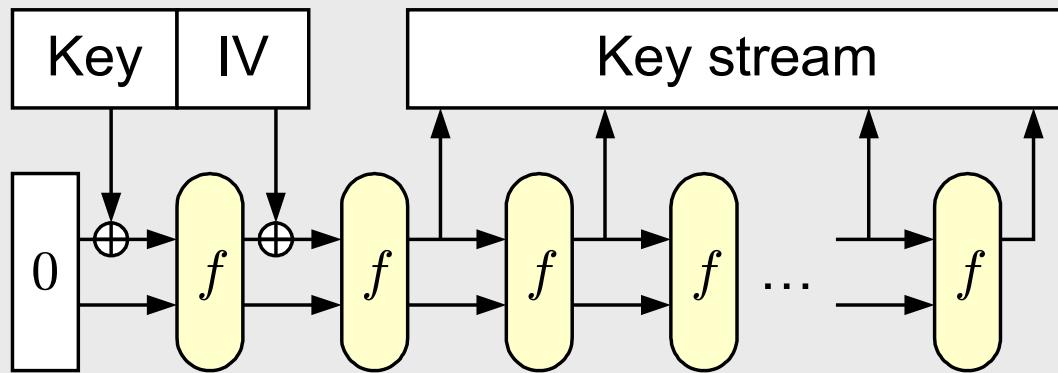
Uses Examples (2/5)

- Message authentication code



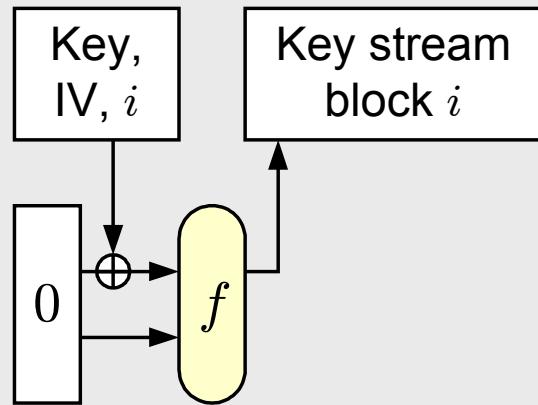
Uses Examples (3/5)

- Stream cipher



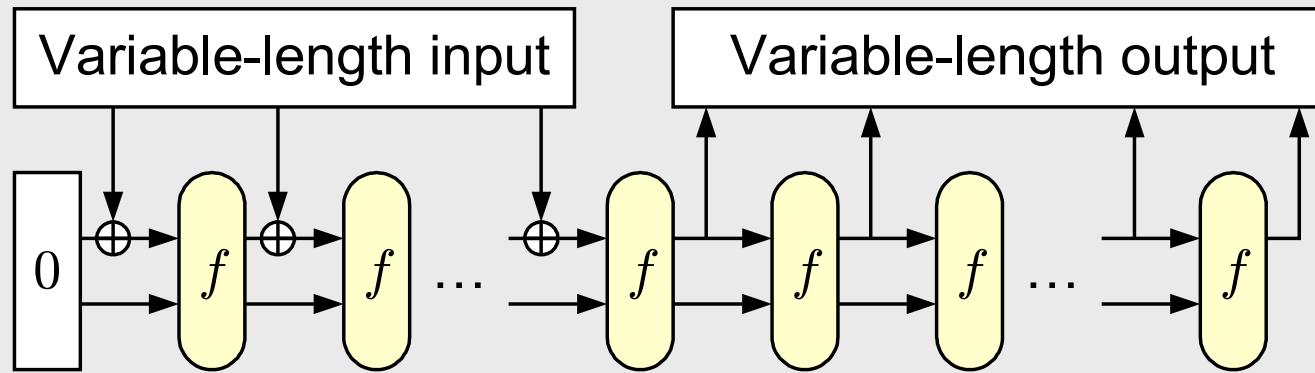
Uses Examples (4/5)

- Random-access stream cipher



Uses Examples (5/5)

- Mask generating functions, key derivation



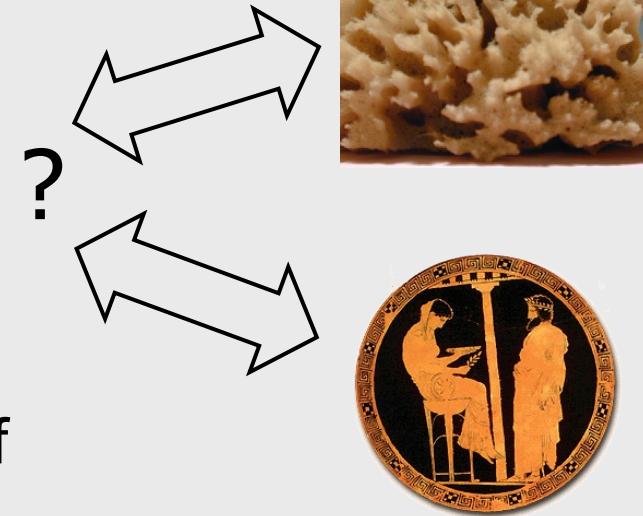
- See PKCS#1 and IEEE Std 1363a

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Distinguishing Random Sponges

- Adversary queries a **black box**, either RS or RO
 - Budget of N input and output blocks
- **Theorem:** A random sponge can only be distinguished from a random oracle by the presence of **inner collisions**.
 - When $N \ll 2^{c/2}$, inner collisions are unlikely

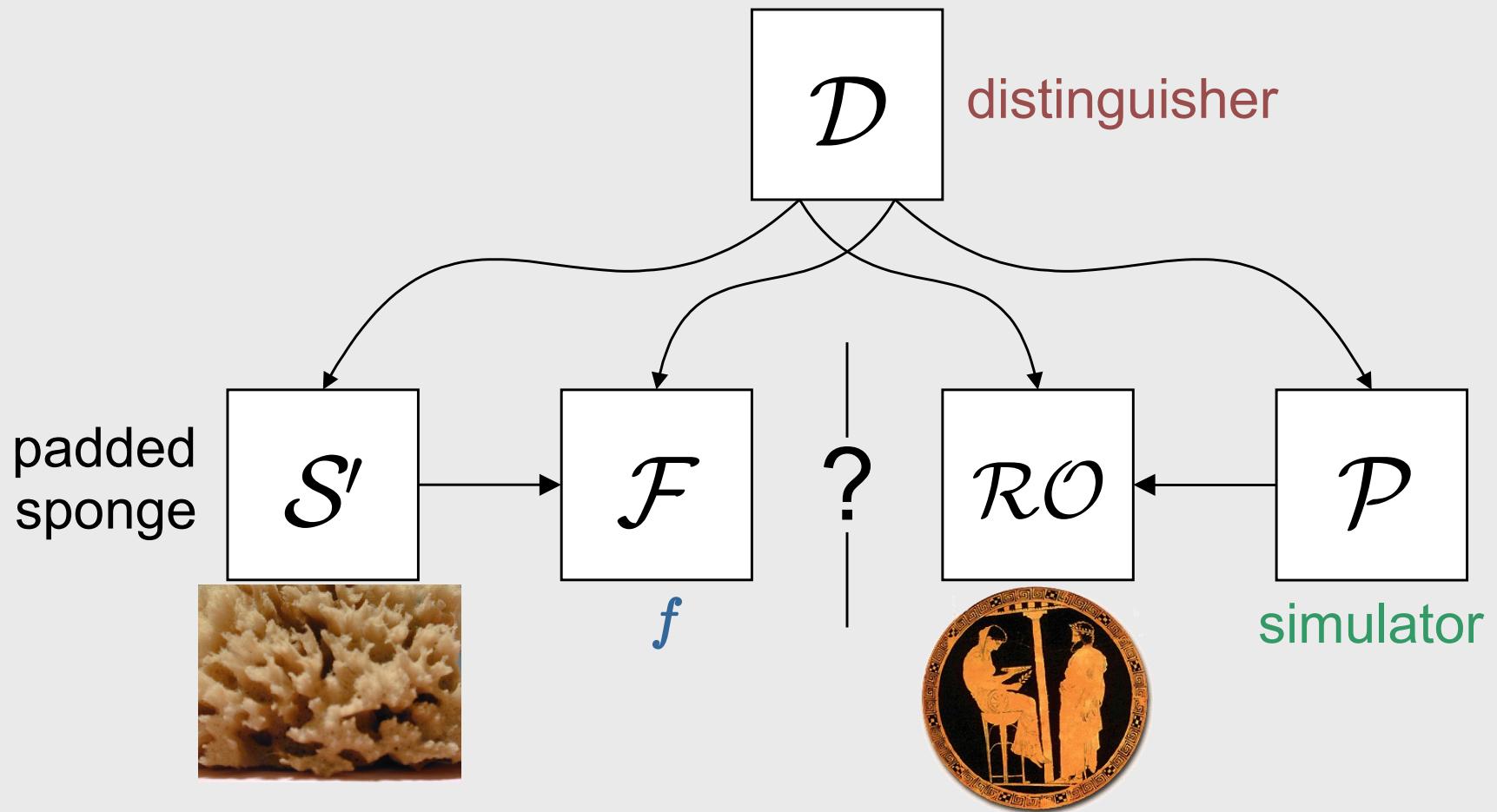


Only gives an upper bound.

Indifferentiability Framework

- Goal: obtain **lower bound** on generic attacks
- Distinguisher has to differentiate between:
 - the ideal system (Random Oracle), and
 - the construction (here, the Sponge),
 - **with access** to publicly-known function or parameter (here, the transformation f)
- If indifferentiable
 - cryptosystem using construction as strong as cryptosystem using ideal system
- Maurer et al., TCC 2004; Coron et al., CRYPTO 2005

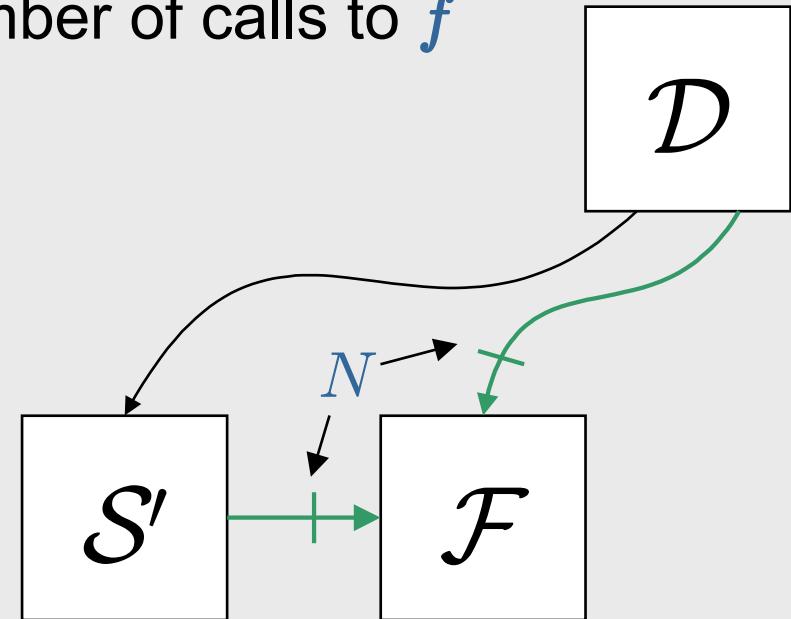
Differentiating Random Sponges



Differentiating Random Sponges

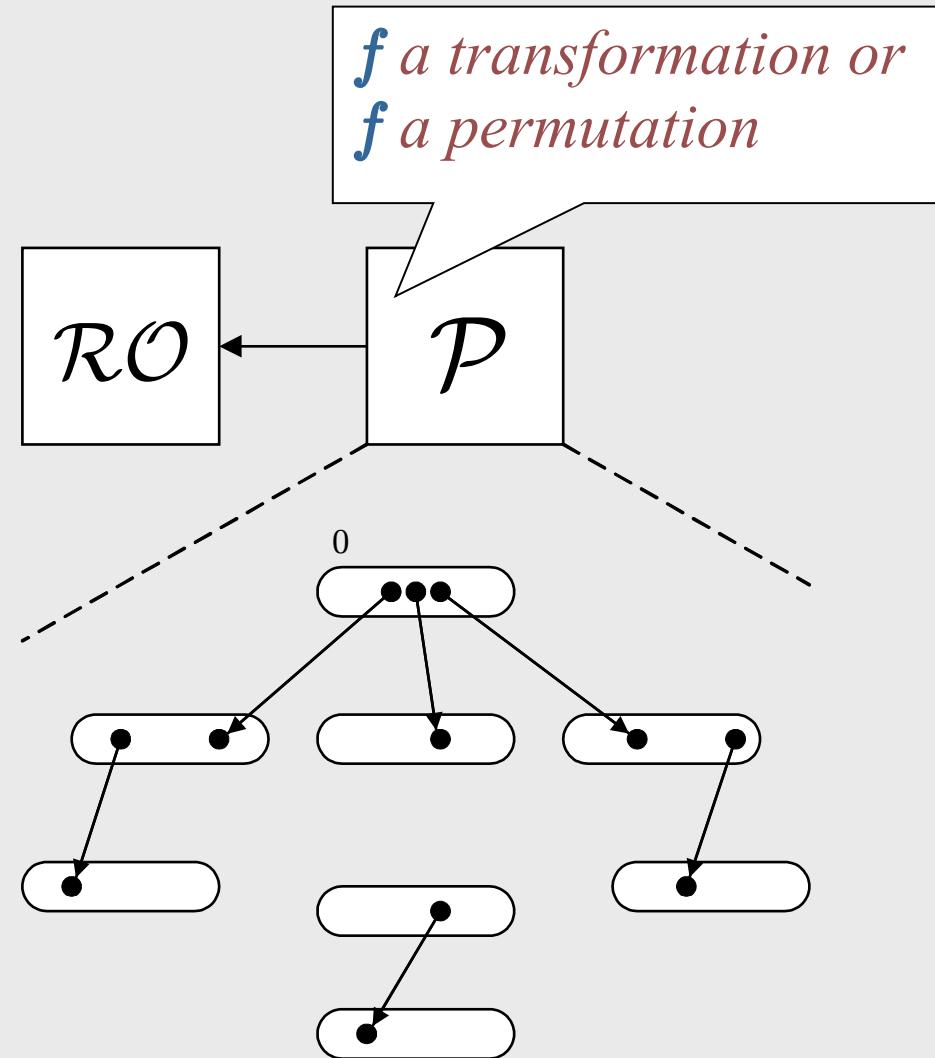
- **Theorem:** a random sponge can be differentiated from a random oracle only with probability $\approx N(N+1)/2^{c+1}$, with $N < 2^c$.
 - Here N is the **total** number of calls to f

*Generic attacks
require $2^{c/2}$.*



Proving the Indifferentiability

- Simulating f
 - Keeps memory of (input, output) pairs in a graph
- Properties
 - **Sponge-consistence** with what RO says
 - Similar **output distribution**
- Can be differentiated
 - By different distribution of simulator and random f

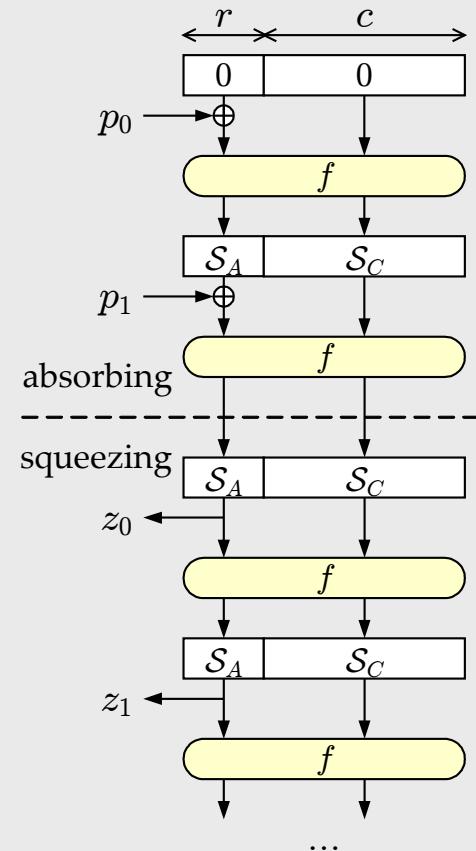


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- ☐ Constructing a sponge function**
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Constructing a Sponge Function

- Choose c, r
 - No generic attacks below $2^{c/2}$
 - Transformation or permutation over $c+r$ bits
- Construct a *random^(!)* transformation?
- Construct a *random^(!)* permutation!
 - It shall not have any special properties^(!)
 - except its compact description
 - Other constructions build upon permutations:
see also Snelru, FFT-Hash, SMASH, ...



Advantages of the Sponge Construction

- Relative simplicity in design
 - Permutation similar to block cipher design
 - E.g., block cipher without key schedule
- Flexibility
 - One permutation can accommodate for several (c,r) pairs
- Efficiency
- Simplicity
 - Simple model, simple proofs
 - Suitable for many applications
 - Variable-length output

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Conclusion

- Sponges are a simple model
 - to model the finite state of iterated primitives
- Sponges are a simple tool
 - for building hash functions and stream ciphers
 - for expressing compact security claims
- Sponges are fun!

<http://sponge.noekeon.org/>