

Concurrently Composable Security With Shielded Super-polynomial Simulators

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Abstract. We propose a new framework for concurrently composable security that relaxes the security notion of UC security. As in previous frameworks, our notion is based on the idea of providing the simulator with super-polynomial resources. However, in our new framework simulators are only given *restricted access* to the results computed in super-polynomial time. This is done by modeling the super-polynomial resource as a stateful oracle that may directly interact with a functionality without the simulator seeing the communication. We call these oracles “shielded oracles”.

Our notion is fully compatible with the UC framework, i. e., protocols proven secure in the UC framework remain secure in our framework. Furthermore, our notion lies strictly between SPS and Angel-based security, while being closed under protocol composition.

Shielding away super-polynomial resources allows us to apply new proof techniques where we can replace super-polynomial entities by indistinguishable polynomially bounded entities. This allows us to construct secure protocols in the plain model using weaker primitives than in previous Angel-based protocols. In particular, we only use non-adaptive-CCA-secure commitments as a building block in our constructions.

As a feasibility result, we present a constant-round general MPC protocol in the plain model based on standard polynomial-time hardness assumptions that is secure in our framework. Our protocol can be made fully black-box. As a consequence, we obtain the *first* black-box construction of a constant-round concurrently secure general MPC protocol in the plain model based on polynomial-time hardness assumptions.

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1 Introduction

Cryptographic protocols typically run in a network where multiple protocols interact with each other. Some of them may even act in an adversarial manner. This makes designing protocols that are secure in such a general setting a complicated task. The universal composability (UC) framework [Can01] provides means for designing and analyzing cryptographic protocols in this concurrent setting. More specifically, it captures a security notion that implies two major properties: *general concurrent security* and *modular analysis*. The former means that a protocol remains secure even when run in an environment with multiple instances of arbitrary protocols. The latter implies that one can deduce the security of a protocol from its components. Unfortunately, there exist strong impossibility results [CF01; CKL03; Lin03; PR08; KL11] regarding the realizability of cryptographic tasks in the UC framework: One requires trusted setup assumptions in order to design UC-secure protocols for many cryptographic tasks. UC-secure protocols have thus been constructed based on various setup assumptions [Can+02; Bar+04; Can+07; KLP07; Kat07; CPS07; LPV09; Dac+13]. However, if the trusted setup is compromised, all security guarantees are lost. In general, one would like to base the security of cryptographic protocols on as little trust as possible.

In order to drop the requirement for trusted setup, relaxed notions of security have been developed. One of the most prominent solutions is “UC security with super-polynomial time simulators” (SPS), introduced in [Pas03]. In this model, the simulator is allowed to run in *super-polynomial time*, thereby overcoming the impossibility results. Various multi-party computation protocols without trusted setup that satisfy this notion have been constructed, e. g., [Pas03; BS05; LPV09; LPV12; Gar+12; Dac+13; Ven14]. SPS security weakens the security of the UC framework because the simulator, being able to run in super-polynomial time, may now be able to carry out stronger attacks in the ideal setting. Still, this security notion is meaningful, since for many cryptographic tasks the ideal setting has an information-theoretic nature. Contrary to UC security, however, security in this model is not closed under protocol composition. As a consequence, this notion neither supports general concurrent security nor modular analysis.

“Angel-based security” [PS04] overcomes these issues. In this model, both the adversary and the simulator have access to an oracle called “(Imaginary) Angel” that provides super-polynomial resources for *specific* computational problems. Many general MPC protocols without setup have been constructed in the Angel-based framework [PS04; MMY06; CLP10; LP12; KMO14; Kiy14; Goy+15; HV16]. Like UC-security, this notion is closed under protocol composition. Furthermore, Angel-based security implies SPS security. In fact, it provides a stronger security notion since the simulator has only access to specific super-polynomial computations. [CLP10] later recast the Angel-based security model in the extended UC (EUC) framework [Can+07] and dubbed their notion “UC with super-polynomial helpers”. In contrast to the non-interactive and stateless Angels in previous works, the “helpers” in [CLP10] are highly interactive and stateful.

In this work, we take this framework a step further. In our new framework, simulators only have *restricted access* to the results computed in super-polynomial

time. More specifically, we model the super-polynomial resources as stateful oracles that are “glued” to an ideal functionality. These oracles may directly interact with the functionality without the simulator observing the communication. The outputs of these oracles are therefore “shielded away” from the simulator. As with Angel-based security, our notion implies SPS security. Moreover, it can be shown that our notion is in fact strictly weaker than Angel-based security. Furthermore, our notion comes with a composition theorem guaranteeing general concurrent security. While modular analysis is not directly implied for technical reasons, using our composition theorem one can achieve modular analysis by constructing protocols with strong composition features. Protocols with these features can be “plugged” into large classes of UC-secure protocols in such a way that the composed protocol is secure in our framework. As a proof of concept, we construct a constant-round commitment scheme with such features.

In order to obtain a composable security notion, environments are “augmented” in our framework, i. e., they may invoke additional (ideal) protocols that include shielded oracles. Since the super-poly computations in these protocols are hidden away, these augmented environments have the unique property that they do not “hurt” protocols proven secure in the UC framework. Therefore, our notion is in fact fully compatible with the UC framework. Moreover, our concept of “shielding away” super-polynomial resources allows us to apply new proof techniques not applicable in previous frameworks: We are able to replace entities involving super-polynomial resources in our proofs by indistinguishable polynomially bounded entities. This allows us to construct (constant-round) protocols using weaker primitives than in previous Angel-based protocols.

1.1 Our results

We propose a new framework that is based on the idea of granting simulators only restricted access to the results of a super-polynomial oracle. We have the following results:

- *New Composable Security Notion:* Our notion of security is closed under general composition, it implies SPS security and is strictly weaker than Angel-based security. (Theorem 9, Proposition 8, Theorem 17)
- *UC-compatibility:* Protocols proven secure in the UC framework are also secure in our new framework. (Theorem 12, Corollary 13)
- *Modular Composition:* As a proof of concept, we present a constant-round commitment scheme in the plain model based on OWPs that is secure in our framework and can be “plugged” into a large class of UC-secure protocols, such that the composite protocol is secure in our framework. Furthermore, this construction can be made fully black-box based on homomorphic commitment schemes. To our best knowledge, this is the first constant-round (black-box) commitment scheme in the plain model based on a standard polynomial-time hardness assumption with such a composition feature. (Theorem 21, Corollary 22, Corollary 23, Theorem 26, Corollary 30)

- *Constant-round (black-box) MPC*: We present a modular construction of a constant-round general MPC protocol in the plain model based on standard polynomial-time hardness assumptions that is secure in our framework. This protocol can be made fully black-box based on homomorphic commitment schemes. As a consequence, we obtain the first black-box construction of a constant-round concurrently secure general MPC protocol in the plain model based on polynomial-time hardness assumptions. (Theorem 31)
- *Building on non-adaptive CCA-commitments*: Our constructions require weaker primitives than previous Angel-based protocols. Specifically, it suffices to use non-adaptive CCA-secure commitment schemes as a building block in our constructions instead of CCA-secure commitment schemes used previously. (Theorem 21, Theorem 26)

2 Related Work

The frameworks most related to ours are SPS and Angel-based security.

SPS security, introduced by [Pas03], provides a meaningful security notion for many cryptographic tasks such as commitment schemes or oblivious transfer. However, SPS security does not come with a composition theorem. There exist many constructions (in the plain model) satisfying this notion, e.g., [Pas03; BS05; LPV09; LPV12; Gar+12; Dac+13; Ven14]. Notably, [LPV12; Gar+12] constructed (non-black-box) constant-round general MPC protocols based on standard polynomial-time hardness assumptions.

Angel-based security [PS04] implies SPS security and comes with a composition theorem. Various general MPC protocols without setup have been constructed in the Angel-based setting [PS04; MMY06; CLP10; LP12; KMO14; Kiy14; Goy+15; HV16]. Some rely on non-standard or super-polynomial time assumptions [PS04; MMY06; KMO14]. The construction in [CLP10] is the first one to rely on standard polynomial-time assumptions, but has non-constant round complexity. Later works [Goy+15; Kiy14] have improved the round-complexity, while also relying on standard assumptions. The most round-efficient construction based on standard polynomial-time assumptions is [Kiy14], which requires $\tilde{O}(\log^2 n)$ rounds and makes only black-box use of the underlying cryptographic primitive. Some Angels in the literature, e.g., [CLP10; KMO14; Kiy14; Goy+15] come with a feature called “robustness” which guarantees that any attack mounted on a constant-round protocol using this angel can be carried out by a polytime adversary with no angels. Protocols proven secure for robust Angels can be “plugged” into UC-secure protocols, resulting in Angel-secure protocols. All known constructions for robust Angels based on standard polytime assumptions require a super-constant number of rounds. Moreover, [CLP13] construct a (super-constant-round) protocol that is secure in the Angel-based setting and additionally preserves certain security properties of other protocols running in the system. They call such protocols “environmentally friendly”.

We want to note that other security notions in the concurrent setting have been proposed that are not based on the idea of simulators with super-polynomial

resources. The “multiple ideal query model” [GJO10; GJ13; GGJ13; CGJ15] considers simulators that are allowed to make more than one output query per session to the ideal functionality. Another (not simulation-based) notion is “input indistinguishability” [MPR06; Gar+12] which guarantees that an adversary cannot decide which inputs have been used by the honest protocol parties. We note that this security notion is incomparable to ours.

3 Shielded Oracles

3.1 Definition of the Framework

Our model is based on the universal composability framework (UC). In this model, a protocol π carrying out a given task is defined to be secure by comparing it to an *ideal functionality* \mathcal{F} , which is a trusted and incorruptible party that carries out a given task in an ideally secure way. π is said to be secure if it “emulates” \mathcal{F} .

While the plain UC model leaves open how session identifiers and corruptions are organized, we follow the convention that both must be consistent with the hierarchical order of the protocols: The session identifier (*sid*) of a sub-protocol must be an extension of the session id of the calling protocol. Likewise, in order to corrupt a sub-party, an adversary must corrupt all parties that are above that sub-party in the protocol hierarchy.

We relax the UC security notion by introducing a super-polynomial time machine that may aid the simulator. This machine is modeled as a *stateful* oracle \mathcal{O} that is “glued” to an the ideal functionality \mathcal{F} . \mathcal{O} may freely interact with the simulator and \mathcal{F} . However, the simulator does not “see” the communication between between \mathcal{O} and \mathcal{F} . Since the output of the oracle is partially hidden from the simulator, we call \mathcal{O} a *shielded oracle*.

Definition 1 (Shielded oracles). A shielded oracle is a stateful oracle \mathcal{O} that can be implemented in super-polynomial time. By convention, the outputs of a shielded oracle \mathcal{O} are of the form $(\text{output-to-funct}, y)$ or $(\text{output-to-adv}, y)$.

The simulator is allowed to communicate with the functionality *only* via the shielded oracle. This way, the shielded oracle serves as an interface that carries out specific tasks the simulator could not do otherwise. The communication between the shielded oracle and the functionality is hidden away from the simulator. The actions of the shielded oracle may depend on the session identifier (*sid*) of the protocol session as well as the party identifiers of the corrupted parties.

Definition 2 (\mathcal{O} -adjoined functionalities). Given a functionality \mathcal{F} and a shielded oracle \mathcal{O} , define the interaction of the \mathcal{O} -adjoined functionality $\mathcal{F}^{\mathcal{O}}$ in an ideal protocol execution with session identifier *sid* as follows:

- $\mathcal{F}^{\mathcal{O}}$ internally runs an instance of \mathcal{F} with session identifier *sid*
 - When receiving the first message x from the adversary, $\mathcal{F}^{\mathcal{O}}$ internally invokes \mathcal{O} with input (sid, x) .
- All subsequent messages from the adversary are passed to \mathcal{O} .

- Messages between the honest parties and \mathcal{F} are forwarded.
- Corruption messages are forwarded to \mathcal{F} and \mathcal{O} .
- When \mathcal{F} sends a message y to the adversary, $\mathcal{F}^\mathcal{O}$ passes y to \mathcal{O} .
- The external write operations of \mathcal{O} are treated as follows:
 - If \mathcal{O} sends (output-to-funct, y), $\mathcal{F}^\mathcal{O}$ sends y to \mathcal{F} .
 - If \mathcal{O} sends (output-to-adv, y), $\mathcal{F}^\mathcal{O}$ sends y to the adversary.

Let $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ be the ideal protocol with functionality $\mathcal{F}^\mathcal{O}$ as defined in [Can01].

In order to obtain a composable security notion, we introduce the notion of *augmented environments*. Augmented environments are UC environments that may invoke, apart from the challenge protocol, polynomially many instances of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ for a given functionality $\mathcal{F}^\mathcal{O}$. The only restriction is that the session identifiers of these instances as well as the session identifier of the challenge protocol are not extensions of one another.

Augmented environments may send inputs to and receive outputs from any invoked instance of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$. In addition, augmented environments can play the role of any adversary via the adversary’s interface of the functionality. In particular, augmented environments may corrupt parties sending the corresponding corruption message as input to the functionality.

In what follows we give a definition of an execution experiment with an $\mathcal{F}^\mathcal{O}$ -augmented environment. For simplicity and due to space constraints, the description is kept informal.

Definition 3 (The $\mathcal{F}^\mathcal{O}$ -execution experiment). *An execution of a protocol σ with adversary \mathcal{A} and an $\mathcal{F}^\mathcal{O}$ -augmented environment \mathcal{Z} on input $a \in \{0, 1\}^*$ and with security parameter $n \in \mathbb{N}$ is a run of a system of interactive Turing machines (ITMs) with the following restrictions:*

- First, \mathcal{Z} is activated on input $a \in \{0, 1\}^*$.
- The first ITM to be invoked by \mathcal{Z} is the adversary \mathcal{A} .
- \mathcal{Z} may invoke a single instance of a challenge protocol, which is set to be σ by the experiment. The session identifier of σ is determined by \mathcal{Z} upon invocation.
- \mathcal{Z} may pass inputs to the adversary or the protocol parties of σ .
- \mathcal{Z} may invoke, send inputs to and receive outputs from instances of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ as long as the session identifiers of these instances as well as the session identifier of the instance of σ are not extensions of one another.
- The adversary \mathcal{A} may send messages to protocol parties of σ as well as to the environment.
- The protocol parties of σ may send messages to \mathcal{A} , pass inputs to and receive outputs from subparties and give outputs to \mathcal{Z} .

Denote by $\text{Exec}(\sigma, \mathcal{A}, \mathcal{Z}[\mathcal{F}^\mathcal{O}])(n, a)$ the output of the $\mathcal{F}^\mathcal{O}$ -augmented environment \mathcal{Z} on input $a \in \{0, 1\}^*$ and with security parameter $n \in \mathbb{N}$ when interacting with σ and \mathcal{A} according to the above definition.

Define $\text{Exec}(\sigma, \mathcal{A}, \mathcal{Z}[\mathcal{F}^\mathcal{O}]) = \{\text{Exec}(\sigma, \mathcal{A}, \mathcal{Z}[\mathcal{F}^\mathcal{O}])(n, a)\}_{n \in \mathbb{N}, a \in \{0, 1\}^*}$

We will now define security in our framework in total analogy to the UC framework:

Definition 4 ($\mathcal{F}^\mathcal{O}$ -emulation). Let π and ϕ be protocols. π is said to emulate ϕ in the presence of $\mathcal{F}^\mathcal{O}$ -augmented environments, denoted by $\pi \geq_{\mathcal{F}^\mathcal{O}} \phi$, if for any PPT adversary \mathcal{A} there exists a PPT adversary (called “simulator”) \mathcal{S} such that for every $\mathcal{F}^\mathcal{O}$ -augmented PPT environment \mathcal{Z} it holds that

$$\text{Exec}(\pi, \mathcal{A}, \mathcal{Z}[\mathcal{F}^\mathcal{O}]) \stackrel{c}{\equiv} \text{Exec}(\phi, \mathcal{S}, \mathcal{Z}[\mathcal{F}^\mathcal{O}]) \quad (1)$$

Throughout this paper, we only consider *static* corruptions.

3.2 Basic Properties and Justification

In this section, we show that that our security notion is transitive and that the dummy adversary is complete within this notion. As a justification for our notion, we show that it implies super-polynomial time simulator (SPS) security.

Definition 5 ($\mathcal{F}^\mathcal{O}$ -emulation with respect to the dummy adversary). The dummy adversary \mathcal{D} is an adversary that when receiving a message (sid, pid, m) from the environment, sends m to the party with party identifier pid and session identifier sid , and that, when receiving m from the party with party identifier pid and session identifier sid , sends (sid, pid, m) to the environment.

Let π and ϕ be protocols. π is said to emulate ϕ in the presence of $\mathcal{F}^\mathcal{O}$ -augmented environments with respect to the dummy adversary, if

$$\exists \mathcal{S}_\mathcal{D} \forall \mathcal{Z} : \text{Exec}(\pi, \mathcal{D}, \mathcal{Z}[\mathcal{F}^\mathcal{O}]) \stackrel{c}{\equiv} \text{Exec}(\phi, \mathcal{S}_\mathcal{D}, \mathcal{Z}[\mathcal{F}^\mathcal{O}]) \quad (2)$$

Proposition 6 (Completeness of the dummy adversary). Let π and ϕ be protocols. Then, π emulates ϕ in the presence of $\mathcal{F}^\mathcal{O}$ -augmented environments if and only if π emulates ϕ in the presence of $\mathcal{F}^\mathcal{O}$ -augmented environments with respect to the dummy adversary.

The proof is almost exactly the same as in [Can01], and therefore only given in the full version of this work. The proof of transitivity is omitted here, too.

Proposition 7 (Transitivity). Let π_1, π_2, π_3 be protocols. If $\pi_1 \geq_{\mathcal{F}^\mathcal{O}} \pi_2$ and $\pi_2 \geq_{\mathcal{F}^\mathcal{O}} \pi_3$ then it holds that $\pi_1 \geq_{\mathcal{F}^\mathcal{O}} \pi_3$.

In order to justify our new notion, we prove that security with respect to $\mathcal{F}^\mathcal{O}$ -emulation implies security with respect to SPS-emulation which we will denote by \geq_{SPS} . See the full version for a formal definition of $\pi \geq_{\text{SPS}} \phi$. The proof is straightforward: View the oracle as part of the simulator. This simulator runs in super-polynomial time, hence can be simulated by an SPS-simulator.

Proposition 8 ($\mathcal{F}^\mathcal{O}$ -emulation implies SPS-emulation). Let \mathcal{O} be a shielded oracle. Assume $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{F}^\mathcal{O}$. Then it holds that $\pi \geq_{\text{SPS}} \mathcal{F}$.

3.3 Universal Composition

A central property of the UC framework is the universal composition theorem. This theorem guarantees that the security of a protocol is *closed* under protocol composition. This means that security guarantees can be given for a UC-secure protocol even if multiple other protocols interact with this protocol in a potentially adversarial manner. We prove a similar theorem in our framework. More specifically, we generalize the universal composition theorem to also include $\mathcal{F}^\mathcal{O}$ -hybrid protocols.

Theorem 9 (Composition theorem). *Let \mathcal{O} be a shielded oracle, \mathcal{F} and \mathcal{G} functionalities.*

1. (Polynomial hybrid protocols) *Let $\pi, \rho^\mathcal{G}$ be protocols. Assume $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{G}$. Then it holds that $\rho^\pi \geq_{\mathcal{F}^\mathcal{O}} \rho^\mathcal{G}$.*
2. ($\mathcal{F}^\mathcal{O}$ -hybrid protocols) *Let π be a protocol, $\rho^{\mathcal{F}^\mathcal{O}}$ a protocol in the $\mathcal{F}^\mathcal{O}$ -hybrid model. Assume $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{F}^\mathcal{O}$. Then it holds that $\rho^\pi \geq_{\mathcal{F}^\mathcal{O}} \rho^{\mathcal{F}^\mathcal{O}}$.*

Proof (of the second statement). For single instance composition (where ρ calls only a single instance of π), treat ρ as part of the environment and use the premise that $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{F}^\mathcal{O}$.

For the general case iteratively apply the single instance composition theorem. In each iteration a new instance of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ is replaced by an instance of π , and the remaining instances of π , $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ and ρ are treated as part of the augmented environment. The claim then follows using transitivity. \square

The universal composition theorem in the UC framework has two important implications: general concurrent security and modular analysis. The former means that a protocol remains secure even when run in an environment with multiple instances of arbitrary protocols. The latter implies that one can deduce the security of a protocol from its components.

Theorem 9 directly implies general concurrent security (with super-polynomial time simulators). However, modular analysis is not directly implied by Theorem 9. This is because the oracle \mathcal{O} may contain all “complexity” of the protocol π , i. e., proving security of $\rho^{\mathcal{F}^\mathcal{O}}$ may be as complex as proving security of ρ^π .

Still, one can use Theorem 9 to achieve modular analysis by constructing secure protocols with strong composition features. A protocol π with such composition features allows analyzing the security of a large class of protocols $\rho^\mathcal{F}$ in the UC framework and achieve security in our framework when replacing \mathcal{F} with π . As a proof of concept, we will show, using Theorem 9, that a large a class of protocols in the \mathcal{F}_{com} -hybrid model can be composed with a commitment protocol presented in this paper (Theorem 26).

The following is a useful extension of Theorem 9 for multiple oracles. The reader is referred to the full version for a proof.

Corollary 10 (Composition theorem for multiple oracles). *Let $\mathcal{O}, \mathcal{O}'$ be shielded oracles. Assume that $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{F}^\mathcal{O}$ and $\rho^{\mathcal{F}^\mathcal{O}} \geq_{\mathcal{F}^\mathcal{O}, \mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$. Then there exists a shielded oracle \mathcal{O}'' such that $\rho^\pi \geq_{\mathcal{G}^{\mathcal{O}''}} \mathcal{G}^{\mathcal{O}''}$.*

3.4 Polynomial Simulatability

We show a unique feature of our framework: For appropriate oracles to be defined below, augmented environments do not “hurt” UC-secure protocols. This means that a protocol that was proven secure in the UC framework is secure in our framework, too. This makes our security notion fully compatible with UC security.

Definition 11 (Polynomial simulatability). *Let \mathcal{O} be a shielded oracle, \mathcal{F} a functionality. Say that \mathcal{O} adjoined to \mathcal{F} is polynomially simulatable if there exists a (PPT) functionality \mathcal{M} such that for all $\mathcal{F}^\mathcal{O}$ -augmented environments \mathcal{Z} it holds that*

$$\mathcal{F}^\mathcal{O} \underset{\mathcal{F}^\mathcal{O}}{\geq} \mathcal{M} \quad (3)$$

If a functionality $\mathcal{F}^\mathcal{O}$ is polynomially simulatable then the super-polynomial power of the oracle \mathcal{O} is totally “shielded away” from the environment. Note that in Definition 11, indistinguishability must hold for *augmented* environments not only for polynomial environments.

As a consequence, $\mathcal{F}^\mathcal{O}$ -augmented environments can be replaced by *efficient* environments if $\mathcal{F}^\mathcal{O}$ is polynomially simulatable.

Theorem 12 (Reduction to polynomial time environments). *Let \mathcal{O} be a shielded oracle and \mathcal{F} a functionality such that $\mathcal{F}^\mathcal{O}$ is polynomially simulatable. Let π, ϕ be protocols that are PPT or in the $\mathcal{F}^\mathcal{O}$ -hybrid model. It holds that*

$$\pi \underset{\mathcal{F}^\mathcal{O}}{\geq} \phi \iff \pi \underset{\text{poly}}{\geq} \phi \quad (4)$$

where the right-hand side means that π emulates ϕ in the presence of all $\mathcal{F}^\mathcal{O}$ -augmented environments that never invoke an instance of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$.

Proof. Poly-emulation implies $\mathcal{F}^\mathcal{O}$ -emulation: Replace all instances of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ with instances of \mathcal{M} using the fact that $\mathcal{F}^\mathcal{O}$ is polynomially simulatable. Treat all instances of \mathcal{M} as part of the environment. This new environment runs in polynomial time. Substitute π by ϕ using the premise. Replace all instances of \mathcal{M} with instances of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ again. The statement follows.

The converse is trivial. □

As augmented environments that never invoke instances of $\text{IDEAL}(\mathcal{F}^\mathcal{O})$ are identical to an UC-environment, the following corollary immediately follows.

Corollary 13 (Compatibility with the UC framework). *Let \mathcal{O} be a shielded oracle and \mathcal{F} a functionality such that $\mathcal{F}^\mathcal{O}$ is polynomially simulatable. It holds that*

$$\pi \underset{\mathcal{F}^\mathcal{O}}{\geq} \phi \iff \pi \underset{\text{UC}}{\geq} \phi \quad (5)$$

Note that this does not contradict the classical impossibility results for the plain UC framework (cp. [CF01]): If $\pi \underset{\mathcal{F}^\mathcal{O}}{\geq} \phi$ for a polynomially simulatable $\mathcal{F}^\mathcal{O}$,

then this only means that $\pi \geq_{\text{UC}} \mathcal{F}^{\mathcal{O}}$, but it does not follow that $\pi \geq_{\text{UC}} \mathcal{F}$. Although the super-polynomial power of \mathcal{O} is shielded away from the outside, it is indeed necessary.

Replacing augmented environments with efficient environments will be a key property in various proofs later in this paper. In particular, it will allow us to prove the security of protocols in our framework using relatively weak primitives such as *non-adaptively-secure-CCA* commitments as opposed to CCA-secure commitments, which are commonly used in Angel-based protocols.

Next, we show that by suitably tweaking a given oracle \mathcal{O} one can make $\mathcal{F}^{\mathcal{O}}$ polynomially simulatable while preserving the security relation.

Lemma 14 (Derived oracle). *Let \mathcal{O} be a shielded oracle such that $\pi \geq_{\mathcal{F}^{\mathcal{O}}} \mathcal{F}^{\mathcal{O}}$. Then there exists a shielded oracle \mathcal{O}' such that $\pi \geq_{\mathcal{F}^{\mathcal{O}'}} \mathcal{F}^{\mathcal{O}'}$ and additionally \mathcal{O}' adjoined to \mathcal{F} is polynomially simulatable.*

Proof. Since π emulates $\mathcal{F}^{\mathcal{O}}$, there exists a simulator $\mathcal{S}_{\mathcal{D}}$ for the dummy adversary \mathcal{D} . Define the shielded oracle \mathcal{O}' as follows: \mathcal{O}' internally simulates $\mathcal{S}_{\mathcal{D}}$ and \mathcal{O} , passes each message $\mathcal{S}_{\mathcal{D}}$ sends to \mathcal{F} to \mathcal{O} , sends each *output-to-funct* output from \mathcal{O} to \mathcal{F} and each *output-to-adv* output from \mathcal{O} to $\mathcal{S}_{\mathcal{D}}$, and forwards the communication between $\mathcal{S}_{\mathcal{D}}$ and the environment. By construction, for all $\mathcal{F}^{\mathcal{O}}$ -augmented environments \mathcal{Z} it holds that

$$\text{Exec}(\pi, \mathcal{D}, \mathcal{Z}[\mathcal{F}^{\mathcal{O}}]) \stackrel{c}{=} \text{Exec}(\mathcal{F}^{\mathcal{O}}, \mathcal{S}_{\mathcal{D}}, \mathcal{Z}[\mathcal{F}^{\mathcal{O}}]) \equiv \text{Exec}(\mathcal{F}^{\mathcal{O}'}, \mathcal{D}, \mathcal{Z}[\mathcal{F}^{\mathcal{O}}]) \quad (6)$$

It follows from Proposition 6 that $\pi \geq_{\mathcal{F}^{\mathcal{O}'}} \mathcal{F}^{\mathcal{O}'}$ and $\mathcal{F}^{\mathcal{O}'} \geq_{\mathcal{F}^{\mathcal{O}}} \pi$. Since $\mathcal{S}_{\mathcal{D}}$ runs in polynomial time, $\mathcal{F}^{\mathcal{O}}$ -augmented environments can simulate $\mathcal{F}^{\mathcal{O}'}$ -augmented environments. Therefore, $\pi \geq_{\mathcal{F}^{\mathcal{O}'}} \mathcal{F}^{\mathcal{O}'}$ and $\mathcal{F}^{\mathcal{O}'} \geq_{\mathcal{F}^{\mathcal{O}'}} \pi$. The theorem follows by defining \mathcal{M} to be the functionality that internally simulates the protocol π . \square

The following corollary shows that UC-secure protocols can be used as sub-protocols in protocols proven secure in our framework, while preserving security.

Corollary 15 (Composition with UC-secure protocols). *Let $\pi, \rho^{\mathcal{F}}$ be protocols such that $\pi \geq_{\text{UC}} \mathcal{F}$ and $\rho^{\mathcal{F}} \geq_{\mathcal{G}^{\mathcal{O}}} \mathcal{G}^{\mathcal{O}}$. Then there exists a shielded oracle \mathcal{O}' such that*

$$\rho^{\pi} \underset{\mathcal{G}^{\mathcal{O}'}}{\geq} \mathcal{G}^{\mathcal{O}'} \quad (7)$$

Proof. Since $\rho^{\mathcal{F}}$ is PPT there exists a shielded oracle \mathcal{O}' such that $\mathcal{G}^{\mathcal{O}'}$ is polynomially simulatable and $\rho^{\mathcal{F}} \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$ by Lemma 14. From Corollary 13 it follows that $\pi \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{F}$. The statement then follows from the composition theorem and the transitivity of $\mathcal{G}^{\mathcal{O}'}$ -emulation. \square

The last result demonstrates the compatibility of our framework with the UC framework again. While it is much more desirable to “plug” a protocol proven secure in our framework into a UC secure protocol—in order to obtain a secure protocol in the *plain model* (this will be addressed in Theorem 26 and Corollary 30)—doing it the other way around is still a convenient property. For instance, it allows one to instantiate “auxiliary” functionalities such as authenticated channels $\mathcal{F}_{\text{auth}}$ or secure channels \mathcal{F}_{SMT} , while preserving security.

3.5 Relation with Angel-based Security

A natural question that arises is how our security notion compares to Angel-based security. We will prove that for a large class of Angels (which to our best knowledge includes all Angels that can be found in the literature), Angel-based security implies our security notion. However, assuming the existence of one-way functions, the converse does not hold. Thus, our notion is *strictly weaker* than Angel-based security.

In the following, we denote by $\pi \geq_{\Gamma\text{-Angel}} \phi$ if π securely realizes ϕ with respect to an angel Γ . Note that the the following results also hold for “UC with super-polynomial helpers” put forward by [CLP10].

Definition 16 (Session-respecting Angel (informal)). *(See the full version for a formal treatment.) An Angel is called session-respecting if its internal state can be regarded as a vector with independent components for each session the Angel is queried for.*

Theorem 17 (Relation between angels and shielded oracles).

1. Assume $\pi \geq_{\Gamma\text{-Angel}} \mathcal{F}$ for an imaginary Angel Γ . If Γ is session-respecting, then there exists a shielded oracle \mathcal{O} such that $\pi \geq_{\mathcal{F}^\mathcal{O}} \mathcal{F}^\mathcal{O}$.
2. Assume the existence of one-way functions. Then there exists a protocol ρ (in the $\mathcal{F}_{\text{auth}}$ -hybrid model), a functionality \mathcal{G} and a shielded oracle \mathcal{O} s. t. $\rho \geq_{\mathcal{G}^\mathcal{O}} \mathcal{G}^\mathcal{O}$ but no imaginary angel Γ can be found such that $\rho \geq_{\Gamma\text{-Angel}} \mathcal{G}$ holds.

We give a proof sketch below. See the full version for a more formal treatment.

Proof (Idea of proof).

1. We consider the dummy adversary \mathcal{D} only. Since $\pi \geq_{\Gamma\text{-Angel}} \mathcal{F}$ we have

$$\exists \mathcal{S}_{\mathcal{D}}^{\Gamma} \forall \mathcal{Z}^{\Gamma} : \text{Exec}(\pi, \mathcal{D}^{\Gamma}, \mathcal{Z}^{\Gamma}) \equiv \text{Exec}(\mathcal{F}, \mathcal{S}_{\mathcal{D}}^{\Gamma}, \mathcal{Z}^{\Gamma}) \quad (8)$$

Now, we consider the experiment with shielded oracle $\mathcal{O} = \mathcal{S}_{\mathcal{D}}^{\Gamma}$, ideal functionality $\mathcal{F}^{\mathcal{O}}$ and simulator $\mathcal{S} = \mathcal{S}_{\mathcal{D}}$. Note that the code of $\mathcal{S}_{\mathcal{D}}$ is executed twice: by \mathcal{O} and by \mathcal{S} . As Γ is assumed to be session-respecting the operation of the Angel is split between \mathcal{O} , that internally runs a copy of the Angel for all queries within the challenge session, and the simulator \mathcal{S} , that handles all remaining queries having access to the global Angel Γ . It follows

$$\text{Exec}(\mathcal{F}, \mathcal{S}_{\mathcal{D}}^{\Gamma}, \mathcal{Z}^{\Gamma}) \equiv \text{Exec}(\mathcal{F}^{\mathcal{O}}, \mathcal{S}^{\Gamma}, \mathcal{Z}^{\Gamma}) \quad (9)$$

In order to prove $\pi \geq_{\mathcal{F}^{\mathcal{O}}} \mathcal{F}^{\mathcal{O}}$ we need to show

$$\exists \mathcal{S} \forall \mathcal{Z} : \text{Exec}(\pi, \mathcal{D}, \mathcal{Z}[\mathcal{F}^{\mathcal{O}}]) \equiv \text{Exec}(\mathcal{F}^{\mathcal{O}}, \mathcal{S}, \mathcal{Z}[\mathcal{F}^{\mathcal{O}}]) \quad (10)$$

and we claim that \mathcal{S} from above suffices. Assume that (10) does not hold, i. e. there is a $\mathcal{Z}[\mathcal{F}^{\mathcal{O}}]$ that can distinguish between interacting with π and \mathcal{D} or with $\mathcal{F}^{\mathcal{O}}$ and \mathcal{S} . Then there exists an environment \mathcal{Z}^{Γ} that internally runs $\mathcal{F}^{\mathcal{O}}$ simulating all augmented $\mathcal{F}^{\mathcal{O}}$ -sessions by means of the global Γ and thus contradicts (9).

2. Let $\tilde{\rho}$ be a commitment protocol such that $\tilde{\rho} \geq_{\mathcal{F}_{\text{com}}^{\mathcal{O}}} \mathcal{F}_{\text{com}}^{\mathcal{O}}$ and \mathcal{O} adjoined to \mathcal{F}_{com} is poly-simulatable. One can find such a protocol using the Angel-based protocol in [CLP10], part 1 of this theorem and Lemma 14, assuming the existence of one-way functions. Define the protocol ρ to be identical to $\tilde{\rho}$ except for the following instruction:

Before the actual commit phase begins, the receiver chooses a_1, \dots, a_n uniformly at random (n is the security parameter) and sends $\text{Commit}(a_i)$ ($i = 1, \dots, n$) to the sender (by running the program of the honest sender in $\tilde{\rho}$ with the pid of the sender). The sender replies with $(1, \dots, 1) \in \{0, 1\}^n$. The receiver then checks if the values he received from the sender equal (a_1, \dots, a_n) . If yes, the receiver outputs “11” (2-bit string). Otherwise, the protocol parties execute the protocol $\tilde{\rho}$.

By construction, it holds that $\rho \geq_{\mathcal{F}_{\text{com}}^{\mathcal{O}}} \mathcal{F}_{\text{com}}^{\mathcal{O}}$. This follows from the fact that every $\mathcal{F}^{\mathcal{O}}$ -augmented environment can be replaced by an efficient environment (since \mathcal{O} attached to \mathcal{F} is polynomially simulatable) and efficient environments can guess the correct a_i only with negligible probability (otherwise $\tilde{\rho}$ would be insecure, contradicting $\tilde{\rho} \geq_{\mathcal{F}_{\text{com}}^{\mathcal{O}}} \mathcal{F}_{\text{com}}^{\mathcal{O}}$).

Assume for the sake of contradiction that there exists an imaginary angel Γ s. t. $\rho \geq_{\Gamma\text{-Angel}} \mathcal{F}_{\text{com}}$ holds. Let the sender be corrupted. Since the adversary has access to Γ , he can run the program of the simulator. The simulator must be able to extract commitments (because $\rho \geq_{\Gamma\text{-Angel}} \mathcal{F}_{\text{com}}$). This enables the adversary to extract all a_i (by relaying the commitments from the receiver each to a different internal copy of the simulator), forcing the receiver to output “11” in the real model experiment. This cannot be simulated in the ideal model experiment, however. We have thus reached a contradiction. \square

Theorem 17 raises the question if it is possible to construct secure protocols with “interesting properties” in our framework that are not (known to be) secure in the Angel-based setting. We will answer this question in the affirmative, presenting a modular construction of a general MPC protocol in the plain model that is constant-round (and black-box) and based only on standard polynomial-time hardness assumptions (Theorem 31).

We would like to briefly note that by Theorem 17 we can already conclude that we can realize every (well-formed) functionality in our framework by importing the results of [CLP10].

Proposition 18 (General MPC in the plain model). *Assume the existence of enhanced trapdoor permutations. For every (well-formed)³ functionality \mathcal{F} , there exists an extraction oracle \mathcal{O} and a protocol ρ (in the plain model⁴) such that*

$$\rho \underset{\mathcal{F}^{\mathcal{O}}}{\geq} \mathcal{F}^{\mathcal{O}} \tag{11}$$

³ See [Can+02] for a definition of well-formed functionalities.

⁴ A model without any trusted setup except for authenticated communication channels.

4 A Constant-Round Commitment Scheme

In this section we will construct a constant-round commitment scheme that is secure in our framework. We note that we assume authenticated channels and implicitly work in the $\mathcal{F}_{\text{auth}}$ -hybrid model.

Let $\langle C, R \rangle$ be a commitment scheme that we will use a building block for our bit commitment scheme Π later. We require $\langle C, R \rangle$ to be tag-based. In a tag-based commitment scheme the committer and receiver additionally use a “tag”—or identity—as part of the protocol [PR05; DDN00]. Moreover we require $\langle C, R \rangle$ to be “immediately committing” as in the following definition.

Definition 19 (Immediately committing). *A commitment scheme $\langle C, R \rangle$ is called immediately committing if the first message in the protocol comes from the sender and already perfectly determines the value committed to.*

The above definition implies that the commitment scheme is perfectly binding and super-polynomially extractable, i. e., given the transcript an extractor can find the unique message of the commitment by exhaustive search.

For the discussion of our commitment scheme, we settle the following notation. Let $s = ((s_{i,b})) \in \{0, 1\}^{2n}$ for $i \in [n]$ and $b \in \{0, 1\}$ be a $2n$ -tuple of bits. For an n -bit string $I = b_1 \cdots b_n$, we define $s_I := (s_{1,b_1}, \dots, s_{n,b_n})$. Thus I specifies a selection of n of the $s_{i,b}$, where one of these is selected from each pair $s_{i,0}, s_{i,1}$.

Construction 1. *The bit commitment scheme Π is defined as follows. Whenever the basic commitment scheme $\langle C, R \rangle$ is used, the committing party uses its pid and the sid as its tag. Let $m \in \{0, 1\}$*

- Commit(m):
 - R: Choose a random n -bit string I and commit to I using $\langle C, R \rangle$
 - S: Pick n random bits $s_{i,0}$ and compute $s_{i,1} = s_{i,0} \oplus m$ for all $i \in [n]$.
 - S and R run $2n$ sessions of $\langle C, R \rangle$ in parallel in which S commits to the s_{i,b_i} ($i \in [n], b_i \in \{0, 1\}$).
- Unveil:
 - S: Send all $s_{i,b_i} \in \{0, 1\}$ ($i \in [n], b_i \in \{0, 1\}$) to R.
 - R: Check if $s_{1,0} \oplus s_{1,1} = \dots = s_{n,0} \oplus s_{n,1}$. If this holds, unveil the string I to S.
 - S: If R unveiled the string correctly, then unveil all s_I .
 - R: Check if S unveiled correctly. If yes, let s'_1, \dots, s'_n be the unveiled values. Check if $s'_i = s_{i,b_i}$ for all $i \in [n]$. If so, output $m := s_{1,0} \oplus s_{1,1}$.

The above construction is reminiscent of [DS13] who presented a compiler that transforms any ideal straight-line extractable commitment scheme into an extractable and equivocal commitment scheme.

Note that if an attacker is able to learn the index set I in the commit phase then he can easily open the commitment to an arbitrary message m' by sending “fake” shares $t_{i,b}$, such that $t_I = s_I$, and $t_{\neg I} = s_I \oplus (m', \dots, m')$. (Here \oplus is interpreted element-wise.) Hence Π is equivocal for super-polynomial machines.

We claim that this protocol securely realizes $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ for a certain shielded oracle \mathcal{O} . We first describe \mathcal{O} , before we move to the theorem.

Construction 2. We define the actions of the shielded oracle \mathcal{O} as follows.⁵

If the sender is corrupted

- \mathcal{O} chooses a random n -bit string I , and commits to the string I to the adversary \mathcal{A} using $\langle C, R \rangle$.
- \mathcal{O} acts as honest receiver in $2n$ sessions of $\langle C, R \rangle$ in parallel. After these sessions have completed, \mathcal{O} extracts each instance of $\langle C, R \rangle$, obtaining the shares $(s_{i,b}$ for $i \in [n]$) and $b \in \{0, 1\}$. (If a commitment cannot be extracted, the corresponding share is set to \perp)
- \mathcal{O} computes $m_i := s_{i,0} \oplus s_{i,1}$ for all $i \in [n]$. (Indices i where one or both of the $s_{i,b}$ is \perp are ignored.) Let $m \in \{0, 1\}$ be the most frequently occurring m_i . (If there are multiple m_i occurring with the highest frequency, m chooses $m = 0$). \mathcal{O} relays (Commit, m) to \mathcal{F}_{com}
- When \mathcal{A} sends shares $s'_{1,0}, s'_{1,1}, \dots, s'_{n,0}, s'_{n,1}$ in the unveil phase of Π , \mathcal{O} acts as an honest receiver, unveiling I .
- Finally, if \mathcal{A} 's unveil is accepting, \mathcal{O} instructs \mathcal{F}_{com} to unveil the message.

If the receiver is corrupted

- \mathcal{O} acts as the sender in an execution of Π , engaging in a commit session of $\langle C, R \rangle$ with the adversary. If the adversary's commitment is accepting, \mathcal{O} extracts this instance of $\langle C, R \rangle$ obtaining a string I (If parts of this string cannot be extracted they are set to \perp).
- \mathcal{O} picks n random bits $s_{i,0}$, and lets $s_{i,1} = s_{i,0}$ for all $i \in [n]$, as if it were honestly committing to $m = 0$. Next, it runs $2n$ instances of Π in parallel, committing to the $s_{i,b}$.
- In the unveil phase, when \mathcal{O} learns the message m , it computes “fake” shares $t_{i,b}$ as follows: $t_I = s_I$ and $t_{\neg I} = s_{\neg I} \oplus (m, \dots, m)$ (\oplus is interpreted element-wise.). \mathcal{O} sends these shares $t_{i,b}$ to the adversary.
- \mathcal{O} acts as the honest sender in the unveil phase of Π . If \mathcal{A} 's unveil of I is accepting, then \mathcal{O} honestly executes the unveil phase for all bit shares t_I . (Otherwise, \mathcal{O} outputs nothing and ignores all further inputs.)

If **no parties are corrupted**, \mathcal{O} simulates an honest execution of protocol Π on input 0 , forwarding all messages to the adversary. Since \mathcal{O} knows the index string I (because \mathcal{O} has created it itself) it can create fake shares just like in the case of a corrupted receiver.

If **both parties are corrupted**, \mathcal{O} just executes the dummy adversary \mathcal{D} internally. (Note that \mathcal{Z} only interacts with \mathcal{D} in the real experiment if both parties are corrupted).

This concludes the description of the shielded oracle \mathcal{O} . Observe that \mathcal{O} can be implemented in super-polynomial time. Also note that in the case of *both or no* party being corrupted, \mathcal{O} can be implemented in polynomial time.

Before we can state our theorem, we need another assumption about the commitment scheme $\langle C, R \rangle$.

⁵ For ease of notation, we drop the prefixes `output-to-fnct` and `output-to-adv` in the messages output by \mathcal{O} .

Definition 20 (pCCA-secure commitment schemes). Let $\langle C, R \rangle$ be a tag-based commitment scheme. A pCCA-decommitment oracle \mathcal{E} interacts with an adversary \mathcal{A} in polynomial many parallel sessions of $\langle C, R \rangle$ as an honest receiver with tags chosen by the adversary. After all sessions have been completed successfully, \mathcal{E} simultaneously reveals all committed values to \mathcal{A} (note that when a session has multiple compatible committed values, \mathcal{E} reveals only one of them. Hence, there might exist many decommitment oracles).

Consider the probabilistic experiment $\text{IND}_b(\langle C, R \rangle, \mathcal{A}^\mathcal{E}, 1^n, z)$ with $b \in \{0, 1\}$:

On input 1^n and auxiliary input z , the adversary \mathcal{A} adaptively chooses a pair of challenge values $v_0, v_1 \in \{0, 1\}$ together with a tag and sends them to the challenger. The challenger commits to v_b using $\langle C, R \rangle$ with that tag. The output of the experiment is the output of $\mathcal{A}^\mathcal{E}$. If any of the tags used by \mathcal{A} for queries to the pCCA-decommitment oracle equals the tag of the challenge, the output of the experiment is replaced by \perp .

$\langle C, R \rangle$ is said to be parallel-CCA-secure if there exists an \mathcal{E} s. t. for all PPT adversaries \mathcal{A} it holds that:⁶

$$\text{IND}_0(\langle C, R \rangle, \mathcal{A}^\mathcal{E}, 1^n, z) \stackrel{c}{\equiv} \text{IND}_1(\langle C, R \rangle, \mathcal{A}^\mathcal{E}, 1^n, z)$$

Note that previous protocols proven secure in the Angel-based framework required (adaptive) CCA-secure commitments schemes [CLP10; Goy+15; Kiy14]. For our notion it suffices to assume parallel-CCA-secure (i. e. non-adaptive) commitment schemes as a building block.

Theorem 21. Assume that $\langle C, R \rangle$ is parallel-CCA-secure and immediately committing. Then $\Pi \geq_{\mathcal{F}_{\text{com}}^\mathcal{O}} \mathcal{F}_{\text{com}}^\mathcal{O}$, where Π is as defined in Construction 1 and \mathcal{O} is the shielded oracle as defined in Construction 2.

Proof. By Proposition 6 it suffices to find a simulator for the dummy adversary. By construction of \mathcal{O} the simulator in the ideal experiment can be chosen to be identical to the dummy adversary.

The main idea of the proof is to consider a sequence of hybrid experiments for a PPT environment \mathcal{Z} that may externally invoke polynomially many $\mathcal{F}_{\text{com}}^\mathcal{O}$ -sessions and iteratively replace those sessions by the real protocol Π in a specific order utilizing the fact that the super-polynomial computations of \mathcal{O} are hidden away and thus the replacements are unnoticeable by \mathcal{Z} , or otherwise we would obtain a PPT adversary against the hiding property of $\langle C, R \rangle$.

Step 1: Let \mathcal{Z} be a PPT environment that may externally invoke polynomial many $\mathcal{F}_{\text{com}}^\mathcal{O}$ -sessions. We denote the output of this experiment by the random variable $\text{Exec}(\mathcal{F}_{\text{com}}^\mathcal{O}, \mathcal{Z})$. Let $\text{Exec}(\Pi, \mathcal{Z})$ be the output of \mathcal{Z} if all instances of $\mathcal{F}_{\text{com}}^\mathcal{O}$ sessions are replaced by the instances of the protocol Π . We show that for all environments \mathcal{Z} it holds that

$$\text{Exec}(\mathcal{F}_{\text{com}}^\mathcal{O}, \mathcal{Z}) \stackrel{c}{\equiv} \text{Exec}(\Pi, \mathcal{Z}) \tag{12}$$

⁶ In our special case the decommitment oracle \mathcal{E} is unique since we assume an immediately committing commitment scheme.

Let \mathcal{Z} be an environment. By a standard averaging argument we can fix some random coins r for \mathcal{Z} . Thus we can assume henceforth that \mathcal{Z} is deterministic.

We call instances of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ (or Π) where the sender or receiver is corrupted *sender sessions* or *receiver sessions*, respectively. Since in the cases where both or no party is corrupted, the \mathcal{O} -adjoined functionalities in this case can be treated as part of the environment. We therefore only need to consider $\mathcal{F}^{\mathcal{O}}$ -augmented environments that only invoke either sender sessions or receiver sessions.

We say a *discrepancy* occurred, if in any ideal sender session of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ \mathcal{O} extracts a value m , but later \mathcal{Z} correctly unveils a value $m' \neq m$. First notice that unless a discrepancy happens, the output of an ideal sender session is identically distributed to the output of the real protocol Π .

We will now distinguish two cases.

1. The probability that \mathcal{Z} causes a discrepancy is negligible.
2. The probability that \mathcal{Z} causes a discrepancy is non-negligible.

Case 1: We replace all sender sessions with instances of Π , incurring only a negligible statistical distance. We are left with a hybrid experiment in which only the receiver sessions are still ideal. We will now iteratively replace ideal receiver sessions with the real protocol, beginning with the *last* session that is started.

Assume that there are at most q receiver sessions. Define hybrids H_0, \dots, H_q as follows. Hybrid H_i is the experiment where the first i receiver sessions are ideal and the remaining $q - i$ receiver sessions are replaced by instances of Π (in which the receiver is corrupted). Clearly, H_q is identical to the experiment where all receiver sessions are ideal, whereas H_0 is the experiment where all receiver sessions are real. The experiment H_i outputs whatever \mathcal{Z} outputs. Let $P_i = \Pr[H_i = 1]$ denote the probability that \mathcal{Z} outputs 1 in the hybrid game H_i . Assume now that $\epsilon := |P_0 - P_q|$ is non-negligible, i. e., \mathcal{Z} has non-negligible advantage ϵ in distinguishing H_0 from H_q . We will now construct an adversary \mathcal{A}_{Π} that breaks the hiding property of Π with advantage ϵ/q .

By the averaging principle, there must exist an index $i^* \in [q]$ such that $|P_{i^*-1} - P_{i^*}| \geq \epsilon/q$. By a standard coin-fixing argument, we can fix the coins selected by the \mathcal{O} -instances inside the first $i^* - 1$ (ideal) receiver sessions. Fixing these coins maintains \mathcal{Z} 's distinguishing advantage. Since we fixed the coins of \mathcal{Z} before, the experiment is now deterministic until the start of receiver session i^* . Since \mathcal{Z} is fully deterministic up until this point, the first message of \mathcal{Z} in session i^* , which is a commitment on the bit string I , is also computed deterministically.

We can now construct the non-uniform adversary \mathcal{A} against the hiding property of $\langle C, R \rangle$. (We note that we do not construct an adversary \mathcal{A} for the standard hiding game but for a multi-instance variant.) As a non-uniform advice, \mathcal{A} receives a complete trace of all messages sent until this point. This includes all bit strings I_1, \dots, I_{i^*} to which \mathcal{Z} committed to in all receiver sessions $1, \dots, i^*$ (it also includes \mathcal{Z} 's input). Note that all messages come from a deterministic process, and the corresponding I_i are uniquely determined by the first messages of each session i since $\langle C, R \rangle$ is immediately committing.

\mathcal{A} now proceeds as follows. \mathcal{A} internally simulates \mathcal{Z} and all sessions invoked by \mathcal{Z} . This simulation can be done in *polynomial time*, since all sender sessions

and the subsequent receiver sessions $i^* + 1$ through q have been replaced by instances of Π , and \mathcal{A} knows the index strings I_i that are used in the (ideal) receiver sessions 1 through i^* .

Let m^* be the message that \mathcal{Z} chooses as input for the sender in session i^* . \mathcal{A} reads $I \stackrel{\text{def}}{=} I_{i^*}$ from its non-uniform advice and samples a tuple s_I of n random strings. It then computes $s_{-I} = s_I \oplus (m^*, \dots, m^*)$ and $s'_{-I} = s_I$ for all $i \in [n]$. \mathcal{A} sends the messages (s_{-I}, s'_{-I}) to the hiding experiment. It now forwards all the messages between the hiding experiment and \mathcal{Z} and simultaneously commits honestly on all values s_I to \mathcal{Z} . When \mathcal{Z} requires that the commitments for all s_I be opened, \mathcal{A} honestly unveils these. When \mathcal{Z} terminates, \mathcal{A} outputs whatever \mathcal{Z} output in the experiment. This concludes the description of \mathcal{A} .

We will now analyze \mathcal{A} 's advantage. If the challenger of the hiding game picks the messages s'_{-I} , \mathcal{Z} obtains a commitment on the all-zero string in \mathcal{A} 's simulation. Therefore, in this case the view of \mathcal{Z} is distributed identically to the view inside the hybrid H_{i^*} . If the challenger of the hiding game picks the messages s_{-I} , \mathcal{Z} obtains a commitment to the message m which is identical to the view of \mathcal{Z} inside the hybrid H_{i^*-1} . It follows

$$\text{Adv}(\mathcal{A}) = |\Pr[H_{i^*} = 1] - \Pr[H_{i^*-1} = 1]| = |P_{i^*} - P_{i^*-1}| \geq \epsilon/q, \quad (13)$$

i.e. \mathcal{A} breaks the hiding property of protocol $\langle C, R \rangle$ with advantage ϵ/q , which concludes case 1. (Note that in this case \mathcal{A} does not need the pCCA oracle.)

Case 2: We now turn to case 2. A first observation is that we only need to consider augmented environments that invoke exactly *one* external session where the sender is corrupted. This is because if a (general) environment \mathcal{Z} causes a discrepancy with non-negligible probability, then there exists a session j^* in which a discrepancy happens *for the first time*. An environment \mathcal{Z}' that invokes only one session where the sender is corrupted can then simulate \mathcal{Z} , guess j^* and simulate all the other sessions where the sender is corrupted with the real protocol. It holds that \mathcal{Z}' also causes a discrepancy with non-negligible probability.

So we henceforth assume that \mathcal{Z} invokes at most q sessions and only one session where the sender is corrupted. In what follows, we will replace all ideal sessions where the receiver is corrupted with real protocols using the same strategy as in case 1. Define the hybrids H_0, \dots, H_q as in case 1 except that now \mathcal{Z} can additionally invoke exactly one sender session in all these hybrids. Clearly, H_q is identical to the experiment where all sessions are ideal, whereas H_0 is the experiment where all receiver sessions are real. Let $P_i = \Pr[H_i = 1]$ again.

Assume now that \mathcal{Z} can distinguish between H_0 and H_q with non-negligible advantage ϵ . Then there exists an index $i^* \in [q]$ such that $|P_{i^*-1} - P_{i^*}| \geq \epsilon/q$. We can now fix the coins that are used in the first $i^* - 1$ ideal sessions until the point where session i^* starts, while maintaining \mathcal{Z} 's distinguishing advantage.

We will construct a non-uniform adversary \mathcal{A}' that breaks the parallel-cca-security of $\langle C, R \rangle$ with advantage ϵ/q . As in case 1, \mathcal{A}' receives as a non-uniform advice a trace of a run of \mathcal{Z} which also includes all index sets I_i to which \mathcal{Z} committed in all sessions until session i^* and possibly the shares to which \mathcal{Z} committed in the only sender-session (again, it also includes \mathcal{Z} 's input).

\mathcal{A}' now proceeds the same way as in case 1. It internally runs \mathcal{Z} and simulates either hybrid H_{i^*-1} or H_{i^*} for \mathcal{Z} by embedding the challenge of the hiding game into the simulated session i^* . The adversary \mathcal{A}' simulates all ideal receiver sessions for $i \leq i^*$ with the help of its advice while all subsequent *receiver* sessions for $i > i^*$ have already been replaced by Π . If \mathcal{Z} has already started to commit to the shares in the only sender session then (by definition) these shares are also part of \mathcal{A}' 's advice and \mathcal{A}' can simulate the sender session. (Note that $\langle C, R \rangle$ is immediately committing, hence the first message of (the parallel executions of) $\langle C, R \rangle$ uniquely determines the shares). If \mathcal{Z} has not yet started to commit to the shares in the sender session then \mathcal{A}' can use its parallel-cca oracle to extract them by forwarding the corresponding messages between the oracle and \mathcal{Z} . After the experiment terminates, \mathcal{A}' outputs whatever \mathcal{Z} outputs.

The analysis of \mathcal{A}' is the same as in case 1 and we end up with the conclusion that \mathcal{A}' breaks the parallel-cca-security of protocol $\langle C, R \rangle$ with advantage ϵ/q .

Hence, it remains to consider environments that invoke exactly one sender-session (all receiver sessions are real and hence can be treated as part of the environment). Assume that such an environment \mathcal{Z} causes a discrepancy with non-negligible probability ϵ' .

We will now construct a non-uniform adversary \mathcal{A}'' that breaks the hiding property of the commitment scheme $\langle C, R \rangle$. \mathcal{A}'' takes part in a partial one-way hiding experiment where the challenger picks a random string $I = b_1 \cdots b_n$ and commits to this string using the commitment scheme $\langle C, R \rangle$. \mathcal{A}'' then sends a vector (a_1, \dots, a_n) to the experiment where $a_l \in \{0, 1, \perp\}$. Let $M = \{l \mid a_l \neq \perp\}$. \mathcal{A}'' wins if $\text{card}(M) \geq n/2$ and $a_l = b_l$ for all $l \in M$. It holds that since $\langle C, R \rangle$ is hiding, \mathcal{A}'' can win this experiment only with negligible probability.

\mathcal{A}'' receives as non-uniform advice the input of \mathcal{Z} . \mathcal{A}'' now proceeds as follows: \mathcal{A}'' forwards the commitment it receives in the experiment to \mathcal{Z} as in the commit phase of the one sender session that \mathcal{Z} can invoke. When \mathcal{Z} sends the commitments on the shares $s_{l,b}$, \mathcal{A}'' forwards them to its parallel-CCA-oracle, thus learning the values $s_{l,b}$ that \mathcal{Z} committed to. \mathcal{A}'' can now simulate the oracle \mathcal{O} and reconstruct the message m defined by these shares (by defining m to be the most frequent value that occurs in $\{s_{i,0} \oplus s_{i,1}\}_{i \in [n]}$ just like \mathcal{O}). When \mathcal{Z} sends the shares $s'_{l,b}$ in the unveil phase of the sender session, \mathcal{A}'' compares them to the originally extracted shares $s_{l,b}$ and defines the vector (a_1, \dots, a_n) as

$$a_l := \begin{cases} b_l & \text{if } \exists b_l \in \{0, 1\} : s_{l,b_l} = s'_{l,b_l} \wedge s_{l,-b_l} \neq s'_{l,-b_l} \\ \perp & \text{else (if no such } b_i \text{ exists)} \end{cases} \quad (\star) \quad (14)$$

and sends (a_1, \dots, a_n) to the experiment.

We will now analyze \mathcal{A}'' 's success probability. Let M be the set of indices l for that condition (\star) holds. If \mathcal{Z} causes a discrepancy, it holds that all tuples of shares $(s'_{l,0}, s'_{l,1})$ define the same but different message $m' \neq m$ than the majority of the original shares $(s_{l,0}, s_{l,1})$, i. e. $\text{card}(M) \geq n/2$. Moreover, for each $l \in M$ b_l equals the l th bit of I . Hence, by construction, \mathcal{A}'' wins with non-negligible probability if \mathcal{Z} causes a discrepancy with non-negligible probability.

Step 2: We will now prove that for every $\mathcal{F}^{\mathcal{O}}$ -augmented environment

$$\text{Exec}(\Pi, \mathcal{D}, \mathcal{Z}[\mathcal{F}_{\text{com}}^{\mathcal{O}}]) \stackrel{c}{\equiv} \text{Exec}(\mathcal{F}_{\text{com}}^{\mathcal{O}}, \mathcal{D}, \mathcal{Z}[\mathcal{F}_{\text{com}}^{\mathcal{O}}]) .$$

If the *sender is corrupted* then nothing needs to be shown, as in this case the real and ideal experiment are statistically close. This follows from the fact that by step 1, case 2, an $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ -augmented environment can cause a discrepancy only with negligible probability.

If the *receiver is corrupted* then by step 1 the real and ideal experiment are both indistinguishable to an experiment where all instances of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ invoked by the environment have been replaced by the real protocol. Hence the outputs of the real and ideal experiment are indistinguishable.

If *no party is corrupted* then one can first replace all sender sessions and receiver sessions with the real protocol using step 1, obtaining a polynomial time environment. Then one can prove indistinguishability by using a very similar reduction to the hiding property as in step 1, case 1.

If *both parties are corrupted* then the real and ideal experiment are identically distributed. \square

The premise of Theorem 21 can be further relaxed by using only a *weakly* pCCA oracle instead of a standard pCCA oracle. A weakly pCCA oracle returns \perp everywhere in case that at least one commitment is not accepting. Weakly pCCA suffices because a shielded oracle in a sender session (acting as the honest receiver) aborts if at least one commitment is not accepting in the commit phase.

The underlying commitment scheme $\langle C, R \rangle$ can be instantiated with the 8-round construction in [Goy+14]. It is straightforward to see that this scheme is pCCA secure by using the extractor in its security proof. The Zero-Knowledge Argument of Knowledge inside [Goy+14] is instantiated with the Feige-Shamir protocol [FS90] and—deviating from the original work—the basic commitment scheme is instantiated by the Blum commitment [Blu81] because we require an immediately committing protocol. Since this scheme is constant-round, we obtain the following result:

Corollary 22. *Assume the existence of one-way permutations. Then there is a constant-round protocol Π_{com} and a shielded oracle \mathcal{O} such that $\Pi_{\text{com}} \geq_{\mathcal{F}_{\text{com}}^{\mathcal{O}}} \mathcal{F}_{\text{com}}^{\mathcal{O}}$.*

The above construction is non-black-box since [Goy+14] (instantiated this way) is non-black-box. However, recall that the only non-black-box part of [Goy+14] is a ZK proof for proving knowledge of committed values and that these values satisfy linear relations. As already pointed out in [Goy+14], this can both be done making only black-box use of a homomorphic commitment scheme. Instantiating [Goy+14] with a perfectly binding homomorphic commitment scheme thus yields a fully black-box construction. Since we need an immediately committing scheme in the plain model for our protocol we let the sender (and not a trusted setup) generate the commitment key of the homomorphic commitment. This construction can be used as a building block in [Goy+14] if the homomorphic commitment scheme is “verifiable”. A verifiable homomorphic commitment scheme allows

one to (non-interactively) verify that a commitment key is well-formed. For instance, the ElGamal commitment scheme [ElG84] (which is based on the DDH assumption) is a verifiable perfectly binding homomorphic commitment scheme [AIR01]. The Linear Encryption scheme [BBS04] (which is based on the DLin assumption) can also be viewed as a commitment scheme with these properties.

Corollary 23. *Assume the existence of verifiable perfectly binding homomorphic commitment schemes. Then there exists a constant-round black-box protocol Π_{com}^{BB} and a shielded oracle \mathcal{O} such that $\Pi_{com}^{BB} \geq_{\mathcal{F}_{com}^{\mathcal{O}}} \mathcal{F}_{com}^{\mathcal{O}}$*

5 A Modular Composition Theorem for Π

We show that we can plug the protocol Π from Construction 1 into a large class of UC-secure protocols in the \mathcal{F}_{com} -hybrid model in such a way that the composite protocol is secure in our framework. We first define Commit-Compute protocols and parallel-CCA-UC-emulation.

Definition 24 (Commit-Compute protocols). *Let $\rho^{\mathcal{F}_{com}}$ be a protocol in the \mathcal{F}_{com} -hybrid model. We call $\rho^{\mathcal{F}_{com}}$ a commit-compute protocol or CC protocol if it can be broken down into two phases: An initial commit phase, where the only communication allowed is sending messages to instances of \mathcal{F}_{com} . After the commit phase is over, a compute phase begins where sending messages to instances of \mathcal{F}_{com} except for unveil-messages is prohibited, but all other communication is allowed.*

Definition 25 (pCCA-UC-emulation). *We write $\rho \geq_{\mathcal{E}\text{-pCCA}} \phi$ if a protocol ρ UC-emulates a protocol ϕ in the presence of (non-uniform) environments that may interact with a pCCA-decommitment oracle \mathcal{E} as defined in Definition 20 for tags that are not extensions of the session identifier of the challenge protocol.*

In the following, let Π be the protocol as in Construction 1 with an immediately committing and parallel-CCA secure commitment scheme $\langle C, R \rangle$. Let \mathcal{E} be the (uniquely defined) pCCA-decommitment oracle of $\langle C, R \rangle$.

We are now ready to state the theorem:

Theorem 26. *Let $\rho^{\mathcal{F}_{com}}$ be a CC protocol and \mathcal{G} a functionality. If $\rho^{\mathcal{F}_{com}} \geq_{\mathcal{E}\text{-pCCA}} \mathcal{G}$ then there exists a shielded oracle \mathcal{O}' such that*

$$\rho^{\Pi} \underset{\mathcal{G}^{\mathcal{O}'}}{\geq} \mathcal{G}^{\mathcal{O}'}$$

Proof. Since $\rho^{\mathcal{F}_{com}} \geq_{\mathcal{E}\text{-pCCA}} \mathcal{G}$ there exists a dummy adversary simulator $\mathcal{S}_{\mathcal{D}}$. Let \mathcal{O} be the shielded oracle from Construction 2, s. t. $\Pi \geq_{\mathcal{F}_{com}^{\mathcal{O}}} \mathcal{F}_{com}^{\mathcal{O}}$. We define the shielded oracle \mathcal{O}' as follows. \mathcal{O}' internally simulates multiple instances of \mathcal{O} (one for each instance of \mathcal{F}_{com} in ρ) and $\mathcal{S}_{\mathcal{D}}$, and forwards messages as follows.

- Messages from the adversary addressed to an instance of \mathcal{F}_{com} are forwarded to the corresponding internal instance of \mathcal{O} .

- Messages from an internal instance of \mathcal{O} to an instance of \mathcal{F}_{com} are forwarded to the dummy adversary simulator $\mathcal{S}_{\mathcal{D}}$.
- Messages between $\mathcal{S}_{\mathcal{D}}$ and the functionality \mathcal{G} are forwarded.
- Messages from the dummy adversary simulator $\mathcal{S}_{\mathcal{D}}$ addressed as coming from an instance of \mathcal{F}_{com} are forwarded to the respective instance of \mathcal{O} .
- Messages from the dummy adversary simulator $\mathcal{S}_{\mathcal{D}}$ not addressed as coming from an instance of \mathcal{F}_{com} are output to the adversary (without forwarding them to an internal instance of \mathcal{O}).

We claim that for this oracle $\rho^{\Pi} \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$ holds. By Proposition 6 it is sufficient to find a simulator for the dummy adversary. The simulator will be the dummy adversary in the ideal world.

Recall that we call instances of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ (or Π) where the sender or receiver is corrupted *sender sessions* or *receiver sessions*, respectively.

We denote by $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$ the protocol $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}}}$ where all ideal sender sessions have been replaced by the real protocol. Let $\text{Exec}(\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}, \mathcal{Z})$ denote an execution of an environment \mathcal{Z} with (polynomially many) instances of $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$. Furthermore, denote by $\text{Exec}(\mathcal{G}^{\mathcal{O}'}, \mathcal{Z})$ an execution of an environment \mathcal{Z} where all instances of $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$ have been replaced by instances of $\mathcal{G}^{\mathcal{O}'}$.

Let \mathcal{Z} be an environment in the experiment $\text{Exec}(\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}, \mathcal{Z})$. By a standard averaging argument we can fix some random coins r for \mathcal{Z} . Thus we can assume henceforth that \mathcal{Z} is deterministic.

In the following hybrid argument, we will have to globally order the main sessions by the *ending* of their commit-phase and (adaptively) invoke instances of $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$, $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}}}$ or $\mathcal{G}^{\mathcal{O}'}$ based on this order. Since the message scheduling may be random, however, this order is not determined a-priori.

In the following, we will therefore have the experiment in the hybrids implement the commit-phases of all invoked protocols “obliviously”, i. e., interact with the environment by running the programs of the shielded oracles and store the inputs of the honest parties without following their instructions in the commit-phases. Note that the only communication that is *visible* to the environment in the commit-phase is its interaction with the shielded oracles or the receiver in an instance of I_s . The latter interaction is identical to an interaction with the shielded oracle in a sender session. Each time the adversary commits to a value, this value is extracted (by a super-polynomial computation) and stored. Note that the inputs of the honest parties have no effect on the messages the shielded oracles output to the adversary in the commit phase.

Once the commit phases of an instance of $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$ has ended, the experiment in the hybrids will invoke an instance of $\rho^{I_s, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$, $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}}}$ or $\mathcal{G}^{\mathcal{O}'}$ depending on the position within the global order of sessions. The experiment will then invoke the honest parties with their respective inputs and follow their instructions (it will also invoke the simulator $\mathcal{S}_{\mathcal{D}}$ with the extracted values if this session is $\mathcal{G}^{\mathcal{O}'}$). Messages from $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ or $\mathcal{S}_{\mathcal{D}}$ to instances of \mathcal{O} (which are “ok” messages) are suppressed. This way, the emulation is consistent with the messages in the

commit phase and distributed identically as if one of the protocols $\mathcal{G}^{\mathcal{O}'}$, $\rho^{H_S, \mathcal{F}_{\text{com}}^{\mathcal{O}'}}$, or $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}'}}$ was executed from the beginning.

Step 1. We show that

$$\text{Exec}(\rho^{H_S, \mathcal{F}_{\text{com}}^{\mathcal{O}'}}(\mathcal{Z})) \stackrel{c}{\equiv} \text{Exec}(\mathcal{G}^{\mathcal{O}'}, \mathcal{Z}) \quad (15)$$

Let $q(n)$ be an upper bound on the number of instances of $\rho^{H_S, \mathcal{F}_{\text{com}}^{\mathcal{O}'}}$ that \mathcal{Z} invokes. Consider the $2q(n) + 1$ hybrids $H_{00}, H_{01}, H_{10}, H_{11}, H_{20}, \dots, H_{q(n)0}$ which are constructed as follows:

Definition of hybrid H_{ij} : Execute the commit phases of each session “without running the code of the parties” by invoking instances of \mathcal{O} . Follow the instruction of each instance of \mathcal{O} . Parties are only there as placeholders for the environment in the commit phase. Their instructions will be execute after the commit phase of the respective session is over. Note that this can be done since the actions of the parties in the commit phase have no effect on the view of the environment in this phase. Messages output from an instance of \mathcal{O} are stored as well. After the commit phase of a session is over do the following:

1. If this is the k th session in which the commit phase has ended and $k \leq i$ then invoke an instance of the dummy adversary simulator and the functionality \mathcal{G} . Hand the dummy parties their respective inputs and the dummy adversary simulator the messages output by the instances of \mathcal{O} . Follow the instructions of the dummy adversary simulator and \mathcal{G} . Ignore messages of the dummy adversary simulator to the environment if these messages are coming from an instance of \mathcal{F}_{com} in the commit phase (i.e. an “ok” message). In the unveil phase, messages from the dummy adversary simulator mimicking an interaction with \mathcal{F}_{com} (which are messages of the form (unveil, b)) are forwarded to the respective instance of \mathcal{O} . Messages from the dummy adversary simulator not mimicking an interaction with an instance of \mathcal{F}_{com} are output (without forwarding them to an internal instance of \mathcal{O}).
2. If $k = i + 1$ and $j = 0$ or $k > i + 1$ then run the protocol parties of $\rho^{\mathcal{F}_{\text{com}}}$ with their inputs and follow their instructions. For all subsessions where the sender is corrupted invoke instances H_S and execute the commit phase of H_S using the same randomness for the receiver as the respective oracle (do not pass the messages to the environment). For all subsessions where the receiver or both or no party has been corrupted invoke instances of \mathcal{F}_{com} and adjoin the respective oracle. Send the outputs of the instances of \mathcal{O} to the respective instances of \mathcal{F}_{com} . Ignore “ok” messages from the instances of \mathcal{F}_{com} .
3. If $k = i + 1$ and $j = 1$ then run the parties of $\rho^{\mathcal{F}_{\text{com}}}$ with their inputs in the commit phase and follow their instructions. For all subsessions invoke an instance of \mathcal{F}_{com} and adjoin the respective oracle. Send the extracted committed values of the \mathcal{O} -instances in sender sessions to the respective \mathcal{F}_{com} -instance. Ignore “ok” messages from the instances of \mathcal{F}_{com} .

Observe that $H_{00} = \text{Exec}(\rho^{\Pi_S, \mathcal{F}_{\text{com}}^{\mathcal{O}}}, \mathcal{Z})$ and $H_{q(n)0} = \text{Exec}(\mathcal{G}^{\mathcal{O}'}, \mathcal{Z})$.

Let P_{ij} denote the probability that \mathcal{Z} outputs 1 in hybrid H_{ij} . Assume $|P_{00} - P_{q(n)0}|$ is non-negligible. Then there exists an index i^* such that either $|P_{i^*1} - P_{(i^*+1)0}|$ or $|P_{i^*0} - P_{i^*1}|$ is also non-negligible.

Case 1: $|P_{i^*1} - P_{(i^*+1)0}|$ is non-negligible. In this case, these neighboring hybrids are equal except that in the $(i^* + 1)$ th session $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}}}$ is replaced by $\mathcal{G}^{\mathcal{O}'}$.

We fix the coins that are used in the experiment in all sessions until the point where the $(i^* + 1)$ th commit phase has ended, while maintaining \mathcal{Z} 's distinguishing advantage.

We can now construct an environment \mathcal{Z}' that distinguishes $\rho^{\mathcal{F}_{\text{com}}}$ from \mathcal{G} . As a non-uniform advice, \mathcal{Z}' receives a complete trace of all messages sent until this point, including all shares s_i and strings I that \mathcal{Z} committed to until the point where the $(i^* + 1)$ th commit phase has ended. \mathcal{Z}' internally simulates the execution experiment with \mathcal{Z} using its advice. Messages to the $(i^* + 1)$ th session are sent to the challenge protocol. \mathcal{Z}' may (tentatively) also invoke instances of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ in order to simulate the instances of $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ that are invoked after the point where the $(i^* + 1)$ th commit phase has ended.

Observe that the real execution corresponds to hybrid H_{i^*1} and the ideal execution to hybrid $H_{(i^*+1)0}$. By construction, \mathcal{Z}' distinguishes $\rho^{\mathcal{F}_{\text{com}}}$ from \mathcal{G} . Since $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ is polynomially simulatable, \mathcal{Z}' can be replaced by a polynomial time environment that also distinguishes $\rho^{\mathcal{F}_{\text{com}}}$ from \mathcal{G} , using Theorem 12. This is a contradiction (to the definition of the dummy adversary simulator).

Case 2: $|P_{i^*0} - P_{i^*1}|$ is non-negligible. In this case, these neighboring hybrids are equal except that in the $(i^* + 1)$ th session $\rho^{\Pi_S, \mathcal{F}_{\text{com}}^{\mathcal{O}}}$ is replaced by $\rho^{\mathcal{F}_{\text{com}}^{\mathcal{O}'}}$. Since \mathcal{Z} distinguishes these hybrids it holds that with non-negligible probability \mathcal{Z} causes a *discrepancy* in hybrid H_{i^*1} as otherwise these hybrids would be statistically close. Let $\tilde{\mathcal{Z}}$ be the environment that internally runs \mathcal{Z} and outputs 1 as soon as a discrepancy occurs.⁷ By construction, $\tilde{\mathcal{Z}}$ outputs 1 with non-negligible probability in H_{i^*1} . We will now consider $i^* + 1$ new hybrids h_0, \dots, h_{i^*} .

⁷ To make the environment able to learn the committed value in a $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ -hybrid protocol, we redefine the shielded oracle \mathcal{O} for the case of a corrupted sender as follows: After the unveil phase is over, the oracle first outputs the extracted committed value to the simulator and after receiving a notification message from the simulator it sends an unveil message to the functionality. Denote this modified oracle by $\tilde{\mathcal{O}}$. Furthermore define $\tilde{\Pi}$ to be identical to Π , except that before outputting the committed value, the receiver sends the committed value to the sender. The sender then sends a notification message to the receiver, who then outputs the committed value. It follows from the exact same arguments as in the proof of Theorem 21 that $\tilde{\Pi} \geq_{\mathcal{F}_{\text{com}}^{\tilde{\mathcal{O}}}} \tilde{\mathcal{F}_{\text{com}}^{\tilde{\mathcal{O}}}}$ and that $\tilde{\mathcal{O}}$ adjoined to \mathcal{F}_{com} is polynomially simulatable. Using these modified versions in the above proof one obtains $\rho^{\tilde{\Pi}} \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$. Since Π unconditionally emulates $\tilde{\Pi}$ it holds that $\rho^{\Pi} \geq_{\mathcal{G}^{\mathcal{O}'}} \rho^{\tilde{\Pi}}$, hence $\rho^{\Pi} \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$.

Definition of hybrid h_j : Execute the commit phases of each session “without running the code of the parties” as described in the description of the hybrids H_{ij} . After the commit phase of a session is over do the following (for a fixed $j \in \{0, \dots, i^*\}$):

1. If $k \leq i^* - j$ then invoke an instance of the dummy adversary simulator and the functionality \mathcal{G} . Hand the dummy parties their respective inputs and the dummy adversary simulator the messages output by the instances of \mathcal{O} . Follow the instructions of the dummy adversary simulator and \mathcal{G} . Ignore messages of the dummy adversary simulator to the environment if these messages are coming from an instance of \mathcal{F}_{com} in the commit phase (i. e. an “ok” message). In the unveil phase, messages from the dummy adversary simulator mimicking an interaction with \mathcal{F}_{com} (which are messages of the form (unveil, b)) are forwarded to the respective instance of \mathcal{O} (with the same SID). Messages from the dummy adversary simulator not mimicking an interaction with an instance of \mathcal{F}_{com} are output (without forwarding them to an internal instance of \mathcal{O})
2. If this is the k th session in which the commit phase has ended and $i^* - j + 1 \leq k \leq i^* + 1$ then run the protocol parties of $\rho^{\mathcal{F}_{\text{com}}}$ with their inputs in the commit phase and follow their instructions. For all subsessions where the receiver or both or no party is corrupted invoke instances of \mathcal{F}_{com} and adjoin the respective oracle. Send the outputs of the instances of \mathcal{O} to the respective instances of \mathcal{F}_{com} . Ignore “ok” messages from the instances of \mathcal{F}_{com} .
3. If $k \geq i^* + 2$ then run the protocol parties of $\rho^{\mathcal{F}_{\text{com}}}$ with their inputs in the commit phase and follow their instructions. For all subsessions invoke an instance of \mathcal{F}_{com} and adjoin the respective oracle. Send the extracted committed values of the \mathcal{O} -instances in sender sessions to the respective \mathcal{F}_{com} -instance. Ignore “ok” messages from the instances of \mathcal{F}_{com} .

Observe that $h_0 = H_{i^*1}$. Let j^* be the *largest index* such that $\tilde{\mathcal{Z}}$ causes a discrepancy in hybrid h_{j^*} with non-negligible probability. (j^* is well-defined, since there is an index for which this property holds, namely 0). Furthermore, $j^* \leq i^* - 1$. This follows from the following argument. Observe that the last hybrid h_{i^*} only contains instances of $\rho^{\mathcal{F}_{\text{com}}}$ (since all instance of \mathcal{G} have been replaced). Because Π emulates $\mathcal{F}_{\text{com}}^{\mathcal{O}}$ and due to the composition theorem $\text{Exec}(\rho^{\Pi}, \mathcal{Z})$ is indistinguishable from h_{i^*} . Since no discrepancy occurs in $\text{Exec}(\rho^{\Pi}, \mathcal{Z})$ it follows that a discrepancy can occur in h_{i^*} only with negligible probability.

By construction, $\tilde{\mathcal{Z}}$ distinguishes the hybrids h_{j^*} and h_{j^*+1} (in the first hybrid $\tilde{\mathcal{Z}}$ outputs 1 with non-negligible probability and in the second hybrid only with negligible probability).

We will now modify these hybrids. For $k \in \{j^*, j^* + 1\}$ define the hybrid hyb_{k-j^*} to be identical to h_k except for the following: At the beginning, the experiment randomly selects one sender session in one of the commit phases $1, \dots, i^* + 1$. In all commit phases that end *after* the $(i^* - j^*)$ th commit phase the real protocol Π_S is invoked instead of $\mathcal{F}^{\mathcal{O}_S}$ in all sender sessions that have not been selected at the beginning. The one sender session that has been selected at the beginning always remains ideal.

It holds that $\tilde{\mathcal{Z}}$ also distinguishes hyb_0 from hyb_1 . This is because $\tilde{\mathcal{Z}}$ still causes a discrepancy in hyb_0 with non-negligible probability because with high probability ($1/\text{poly}$) the first session in which $\tilde{\mathcal{Z}}$ causes a discrepancy is selected. Furthermore, $\tilde{\mathcal{Z}}$ causes a discrepancy in hyb_1 only with negligible probability.

We fix the coins that are used in the experiment in all sessions until the point where the $(i^* - j^*)$ th commit phase has ended, while maintaining $\tilde{\mathcal{Z}}$'s distinguishing advantage.

We can now construct an environment \mathcal{Z}'' that distinguishes $\rho^{\mathcal{F}^{\text{com}}}$ from \mathcal{G} . As a non-uniform advice, \mathcal{Z}'' receives a complete trace of all messages sent until this point, including all shares s_i and index sets I that $\tilde{\mathcal{Z}}$ committed to until the point where the $(i^* - j^*)$ th commit phase has ended. \mathcal{Z}'' proceeds as follows: It internally simulates the execution experiment with $\tilde{\mathcal{Z}}$ using its advice, randomly picking a sender session at the beginning. Messages to the $(i^* - j^*)$ th session are sent to the challenge protocol. \mathcal{Z}'' can simulate the only instance of \mathcal{F}^{os} that may occur in a commit phase with its pCCA-oracle \mathcal{E} . \mathcal{Z}'' may (tentatively) also invoke ideal receiver sessions in order to simulate ideal receiver sessions that are invoked after the point where the $(i^* - j^*)$ th commit phase has ended.

Observe that the real execution corresponds to hybrid hyb_1 and the ideal execution to hybrid hyb_0 . By construction, \mathcal{Z}'' distinguishes $\rho^{\mathcal{F}^{\text{com}}}$ from \mathcal{G} . With the same argument as in the proof of Theorem 21, step 1, case 2, one can replace all ideal receiver sessions that \mathcal{Z}'' invokes with instances of the real protocol. By construction, an environment \mathcal{Z}'' was found that can query the pCCA-oracle \mathcal{E} and distinguish $\rho^{\mathcal{F}^{\text{com}}}$ and \mathcal{D} from \mathcal{G} and $\mathcal{S}_{\mathcal{D}}$. We have thus reached a contradiction.

Step 2. We show that $\rho^{\Pi} \geq_{\mathcal{G}^{\mathcal{O}'}} \mathcal{G}^{\mathcal{O}'}$, completing the proof.

Let \mathcal{Z} be a $\mathcal{G}^{\mathcal{O}'}$ -augmented environments. By step 1, we can replace all instances of $\mathcal{G}^{\mathcal{O}'}$ with instances of $\rho^{\Pi_{\mathcal{S}}, \mathcal{F}^{\text{com}}}$. Since Π emulates $\mathcal{F}_{\text{com}}^{\text{com}}$, it follows from the composition theorem that we can replace (the challenge protocol) ρ^{Π} also with $\rho^{\Pi_{\mathcal{S}}, \mathcal{F}^{\text{com}}}$. Again by step 1, we can replace all instances of $\rho^{\Pi_{\mathcal{S}}, \mathcal{F}^{\text{com}}}$ back with instances of $\mathcal{G}^{\mathcal{O}'}$. The theorem follows. \square

If the following property holds for the commitment scheme $\langle C, R \rangle$, the premise $\rho^{\mathcal{F}^{\text{com}}} \geq_{\mathcal{E}\text{-pCCA}} \mathcal{G}$ is automatically fulfilled.

Definition 27 (*r*-non-adaptive robustness). *Let $\langle C, R \rangle$ be a tag-based commitment scheme and \mathcal{E} a pCCA-decommitment oracle for it as in Definition 20. For $r \in \mathbb{N}$, we say that $\langle C, R \rangle$ is *r*-non-adaptively-robust w. r. t. \mathcal{E} if for every PPT adversary \mathcal{A} , there exists a PPT simulator \mathcal{S} , such that for every PPT *r*-round interactive Turing machine \mathcal{B} , the following two ensembles are computationally indistinguishable:*

$$\begin{aligned} & - \{ \langle \mathcal{B}(y), \mathcal{A}^{\mathcal{E}}(z) \rangle (1^n) \}_{n \in \mathbb{N}, y \in \{0,1\}^*, z \in \{0,1\}^*} \\ & - \{ \langle \mathcal{B}(y), \mathcal{S}(z) \rangle (1^n) \}_{n \in \mathbb{N}, y \in \{0,1\}^*, z \in \{0,1\}^*} \end{aligned}$$

The above definition is a weakening of the (adaptive) robustness property put forward by [CLP10].

Corollary 28. *If additionally the commitment scheme $\langle C, R \rangle$ in Π is r -non-adaptively-robust, then for every r -round CC protocol $\rho^{\mathcal{F}^{\text{com}}}$ it holds that if $\rho^{\mathcal{F}^{\text{com}}} \geq_{UC} \mathcal{G}$ then there exists a shielded oracle \mathcal{O}' such that*

$$\rho^{\Pi} \underset{\mathcal{G}^{\mathcal{O}'}}{\geq} \mathcal{G}^{\mathcal{O}'}$$

Up to now we could instantiate $\langle C, R \rangle$ with a modified version of [Goy+14] as described above of Corollary 22. To additionally make this scheme r -non-adaptively-robust w. r. t. \mathcal{E} one can add “redundant slots” using the idea of [LP09] (the scheme needs to have at least $r + 1$ slots to be r -non-adaptively-robust).

In the following lemma we show that every UC-secure protocol $\rho^{\mathcal{F}^{\text{com}}}$ can be transformed into a UC-secure CC protocol.

Lemma 29 (CC compiler). *Let $\rho^{\mathcal{F}^{\text{com}}}$ be a protocol in the \mathcal{F}_{com} -hybrid model. Then there exists a CC protocol $\text{Comp}(\rho)^{\mathcal{F}^{\text{com}}}$ such that $\text{Comp}(\rho)^{\mathcal{F}^{\text{com}}} \geq_{UC} \rho^{\mathcal{F}^{\text{com}}}$. Furthermore, if $\rho^{\mathcal{F}^{\text{com}}}$ is constant-round then so is $\text{Comp}(\rho)^{\mathcal{F}^{\text{com}}}$.*

Proof (Idea of proof). Replace each instance of \mathcal{F}_{com} with a *randomized commitment* where the sender commits to a bit b by sending a random value a to \mathcal{F}_{com} and $a \oplus b$ to the receiver. Note that since the protocol is PPT the number of commitments of each party is polynomially bounded. Put all randomized calls to \mathcal{F}_{com} in a single commit phase. \square

Let Π_r be the constant-round protocol as in Construction 1 where $\langle C, R \rangle$ is instantiated with the immediately committing, parallel-CCA secure and r -non-adaptively-robust modified version of [Goy+14] as described above. Furthermore, let Π_r^{BB} be the same as Π_r , except that [Goy+14] is instantiated with a verifiable perfectly binding homomorphic commitment scheme, thus making the construction fully black-box. Applying Corollary 28 and Lemma 29 one obtains the following:

Corollary 30. *Assume the existence of one-way permutations. Let $\rho^{\mathcal{F}^{\text{com}}}$ be a constant-round protocol and \mathcal{G} a functionality. If $\rho^{\mathcal{F}^{\text{com}}} \geq_{UC} \mathcal{G}$ then there exists a shielded oracle \mathcal{O}' such that for sufficiently large r it holds that*

$$\text{Comp}(\rho)^{\Pi_r} \underset{\mathcal{G}^{\mathcal{O}'}}{\geq} \mathcal{G}^{\mathcal{O}'}$$

Furthermore, assuming the existence of verifiable perfectly binding homomorphic commitment schemes, the same property holds for Π_r^{BB} .

6 Constant-Round (Black-Box) General MPC

We can now apply Corollary 30 to obtain a constant-round general MPC protocol based on standard polynomial-time hardness assumptions that is secure in our framework. [HV15] showed that for every well-formed functionality \mathcal{F} there exists a constant-round protocol $\rho^{\mathcal{F}^{\text{com}}}$ that UC-emulates \mathcal{F} , assuming two-round semi-honest oblivious transfer. Plugging Π_r (for a sufficiently large r) into this protocol

yields a constant-round general MPC protocol based on standard assumptions (e.g. enhanced trapdoor permutations). Furthermore, since the construction in [HV15] is black-box, plugging Π_r^{BB} into [HV15] yields a fully black-box construction of a constant-round general MPC protocol based on polynomial-time hardness assumptions that is secure in our framework.

Theorem 31 (Constant-round general MPC in the plain model).

- (a) *Assume the existence of enhanced trapdoor permutations. Then for every well-formed functionality \mathcal{F} , there exists a constant-round protocol $\pi_{\mathcal{F}}$ (in the plain model) and a shielded oracle \mathcal{O} such that*

$$\pi_{\mathcal{F}} \underset{\mathcal{F}^{\mathcal{O}}}{\geq} \mathcal{F}^{\mathcal{O}} \quad (16)$$

- (b) *Assume the existence of verifiable perfectly binding homomorphic commitment schemes and two-round semi-honest oblivious transfer. Then for every well-formed functionality \mathcal{F} , there exists a constant-round protocol $\pi_{\mathcal{F}}^{BB}$ (in the plain model) and a shielded oracle \mathcal{O} such that*

$$\pi_{\mathcal{F}}^{BB} \underset{\mathcal{F}^{\mathcal{O}}}{\geq} \mathcal{F}^{\mathcal{O}} \quad (17)$$

$\pi_{\mathcal{F}}^{BB}$ uses the underlying homomorphic commitment scheme and oblivious transfer only in a black-box way.

7 Conclusion

Shielded super-polynomial resources allow for general concurrent composition in the plain model while being compatible with UC security. As an application a secure constant-round (black-box) general MPC protocol was modularly designed and future work will be needed to make this proof of concept a general principle.

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