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Efficient Implementations of MQPKS on Constrained Devices

Efficient Implementations of MQPKS on Constrained Devices

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Motivation

- Quantum computers can solve Discrete Logarithm problem and Factorization problem
- Alternatives must be found
- MQ based cryptography is one solution
- Many MQ schemes were partially or fully broken in the past
- Few implementations exist of the remaining schemes
- Fair comparison of schemes was only possible theoretically

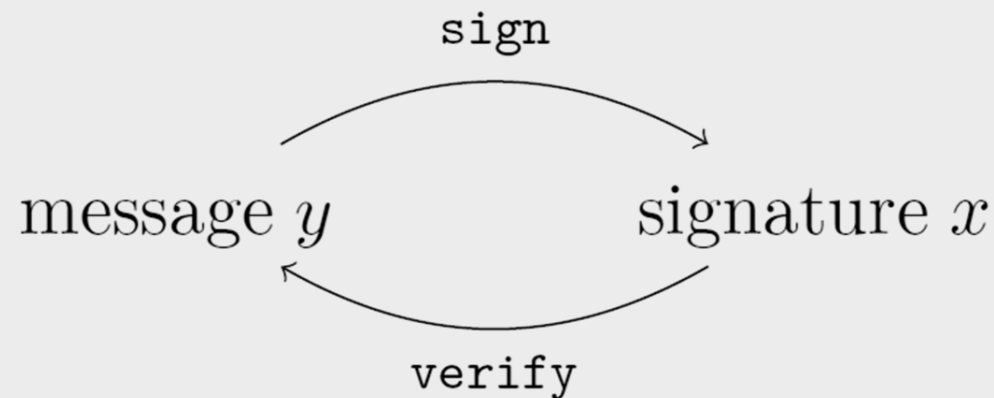
Goals

- Implement
 - all currently secure schemes
 - with the same security level
 - configurable code
 - including all currently known optimizations

- Show that MQ schemes are a good alternative to current schemes?

MQ Signature Schemes - Basics

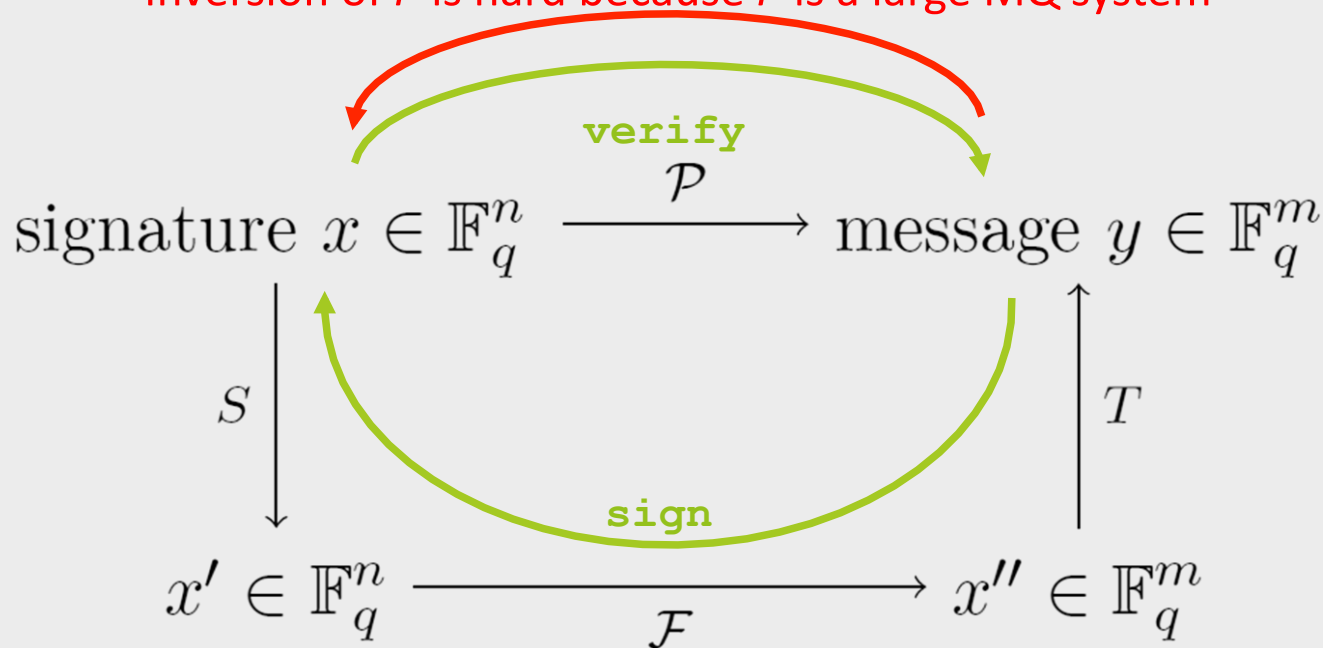
- `sign()` maps the message to signature with the secret key
- `verify()` maps the signature to message with the public key
- If the verification result is not the original message, the signature is invalid
- `sign` and `verify` are inverses of each other
- `verify(sign(message)) = message`



MQ Signature Schemes - Basics

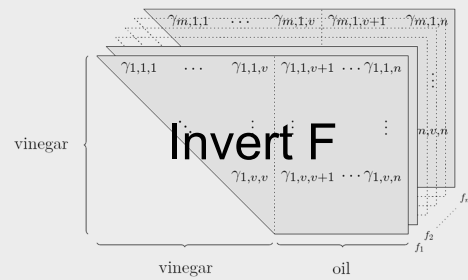
- Four maps exist in a general MQ scheme: P , S , F , and T
- P is the composition of S , F , and T and is the public key, $P = T \circ F \circ S$
- S , F , and T are the secret key

Inversion of P is hard because P is a large MQ system



Schemes

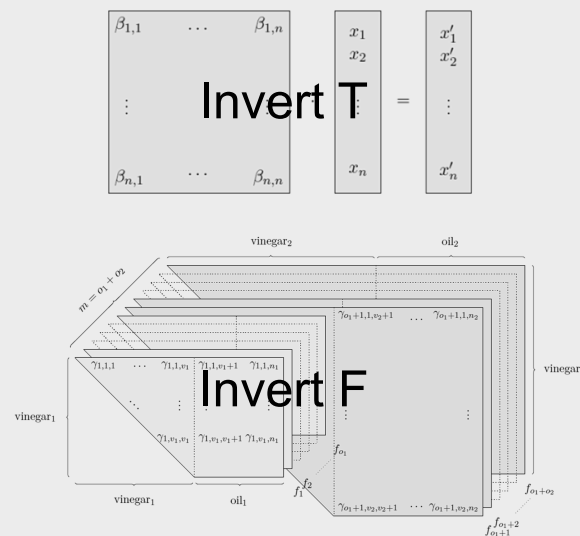
UOV



$$\begin{bmatrix} I & S' \\ 0 & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

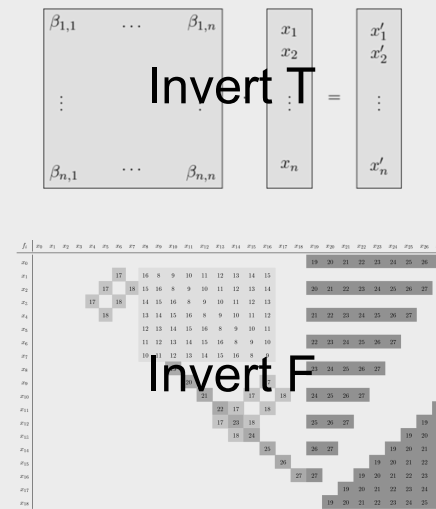
Rainbow



$$\begin{bmatrix} I & S'_1 & S'_2 \\ 0 & I & \\ 0 & 0 & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

enTTS

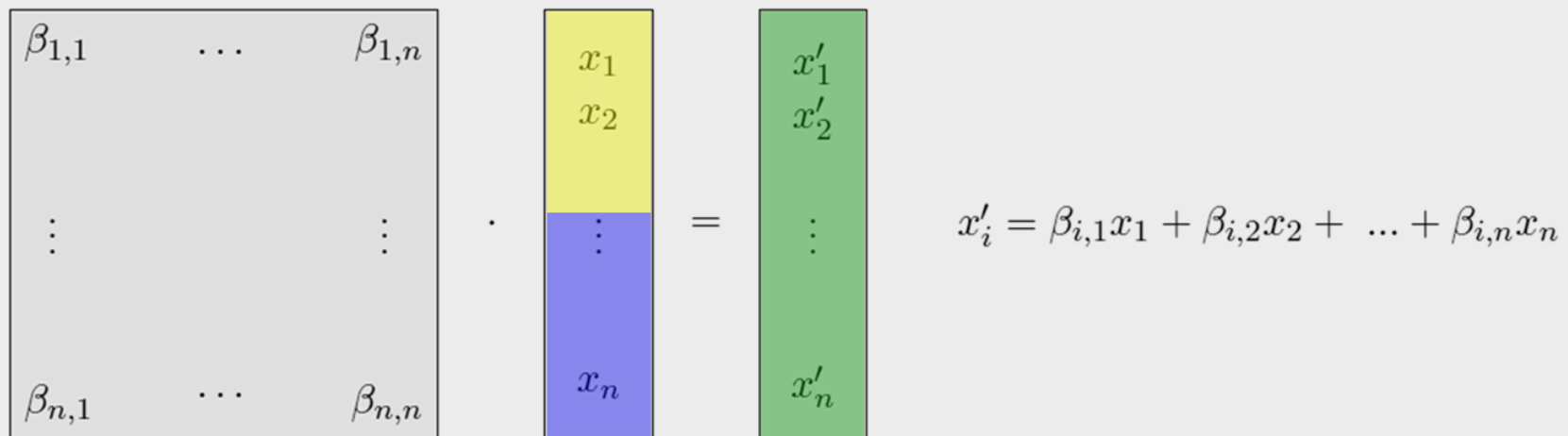


$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

Linear Maps

- Maps or transformations can also be seen as functions
- There exist two types of maps in MQ schemes: linear and MQ maps
- Linear maps mix variables and therefore “hide” existing structure



$$\begin{matrix}
 \beta_{1,1} & \dots & \beta_{1,n} \\
 \vdots & & \vdots \\
 \beta_{n,1} & \dots & \beta_{n,n}
 \end{matrix}
 \cdot
 \begin{matrix}
 x_1 \\
 x_2 \\
 \vdots \\
 x_n
 \end{matrix}
 =
 \begin{matrix}
 x'_1 \\
 x'_2 \\
 \vdots \\
 x'_n
 \end{matrix}$$

$$x'_i = \beta_{i,1}x_1 + \beta_{i,2}x_2 + \dots + \beta_{i,n}x_n$$

Inverting Linear Maps

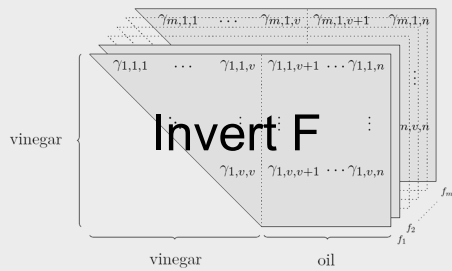
- S and T can be inverted by matrix inversion
- Matrix inversion can be done by Gaussian elimination algorithm for each column of identity matrix
- Inversion of a linear map is matrix vector multiplication with the inverse

$$\begin{array}{|c|} \hline \beta_{1,1} & \dots & \beta_{1,n} \\ \hline \vdots & & \vdots \\ \hline \beta_{n,1} & \dots & \beta_{n,n} \\ \hline \end{array} \cdot \begin{array}{|c|} \hline x_1 \\ x_2 \\ \vdots \\ x_n \\ \hline \end{array} = \begin{array}{|c|} \hline x'_1 \\ x'_2 \\ \vdots \\ x'_n \\ \hline \end{array}$$

T^{-1}

Schemes

UOV



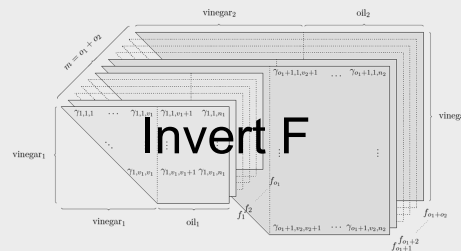
$$\begin{bmatrix} I & S' \\ 0 & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

Rainbow

$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert T



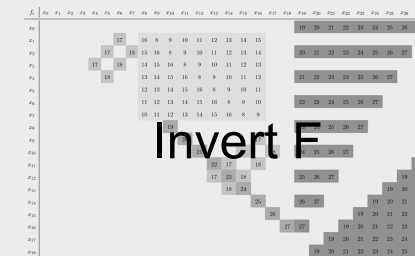
$$\begin{bmatrix} I & S'_1 & & \\ & I & S'_2 & \\ & 0 & I & \\ & 0 & & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

enTTS

$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert T

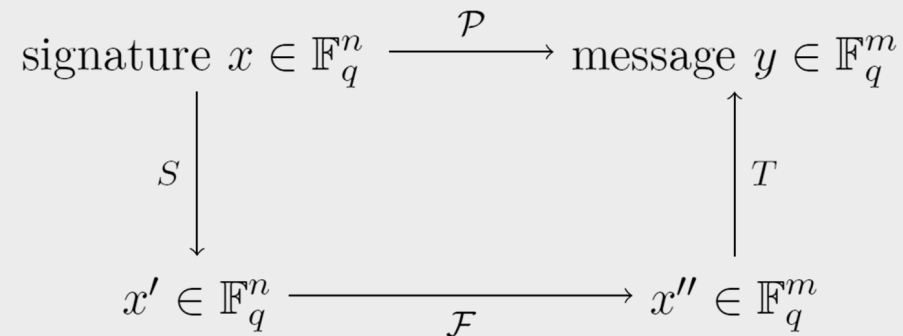


$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

MQ Maps

- F and P are MQ maps



- P has no special structure and is large, therefore hard to invert

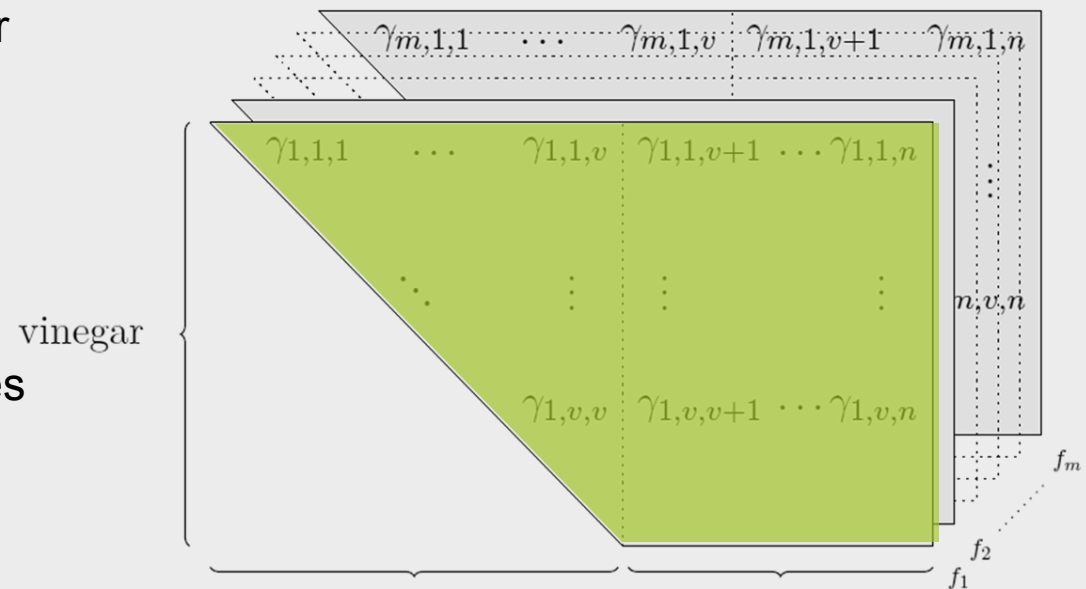
$$3x_1x_1 + 8x_1x_2 + 5x_1x_3 + 8x_2x_2 + 6x_2x_3 + 2x_3x_3 = m_1$$

$$1x_1x_1 + 7x_1x_2 + 9x_1x_3 + 3x_2x_2 + 7x_2x_3 + 2x_3x_3 = m_2$$

- A special structure in F is necessary to allow easy inversion
- This special structure is hidden by S and T

Inverting Central Maps - UOV

- Two variable groups: Oil & Vinegar
- Fix vinegar variables to make system linear
- A quadratic linear equation system remains after fixing
- Apply Gaussian elimination to get a solution for the oil variables



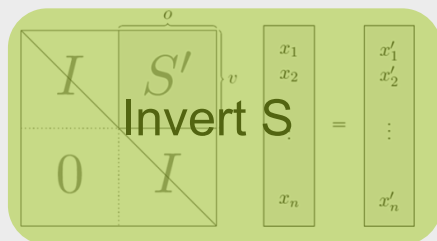
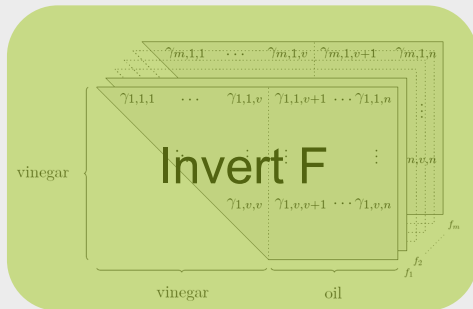
$x_1 \cdots x_4 \leftarrow$ fixed random values $r_1 \cdots r_4$

$$f_i = \underbrace{\gamma_{i,1,1}r_1r_1 + \gamma_{i,1,2}r_1r_2 + \gamma_{i,1,3}r_1r_3 + \gamma_{i,1,4}r_1r_4 + \gamma_{i,2,2}r_2r_2 + \gamma_{i,2,3}r_2r_3 + \gamma_{i,2,4}r_2r_4 + \gamma_{i,3,3}r_3r_3 + \gamma_{i,3,4}r_3r_4 + \gamma_{i,4,4}r_4r_4}_{\sum \text{constant terms} = v_i} + \underbrace{\gamma_{i,1,5}r_1x_5 + \gamma_{i,1,6}r_1x_6 + \gamma_{i,2,5}r_2x_5 + \gamma_{i,2,6}r_2x_6 + \gamma_{i,3,5}r_3x_5 + \gamma_{i,3,6}r_3x_6 + \gamma_{i,4,5}r_4x_5 + \gamma_{i,4,6}r_4x_6}_{\sum \text{linear terms} = c_{i,5}x_5, c_{i,6}x_6}$$

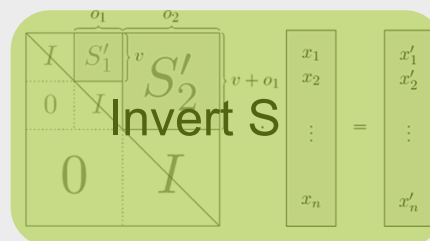
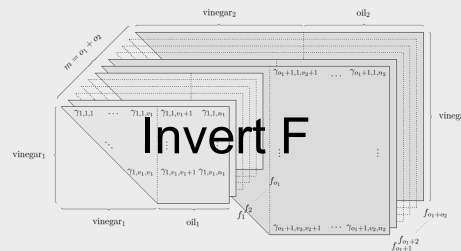
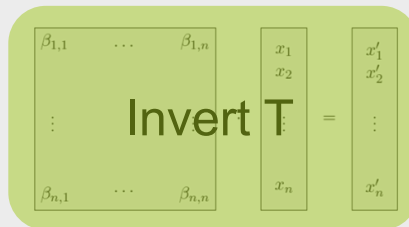
$$\begin{pmatrix} c_{1,5} & c_{1,6} \\ c_{2,5} & c_{2,6} \end{pmatrix} \cdot \begin{pmatrix} x_5 \\ x_6 \end{pmatrix} = \begin{pmatrix} m_1 - v_1 \\ m_2 - v_2 \end{pmatrix}$$

Schemes

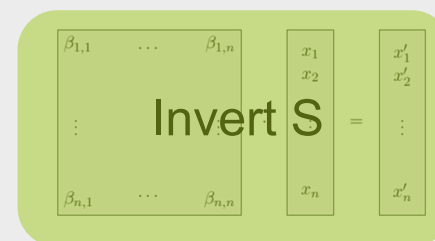
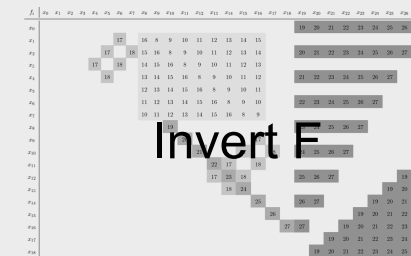
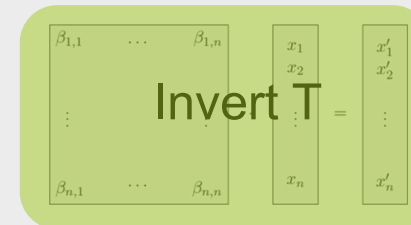
UOV



Rainbow

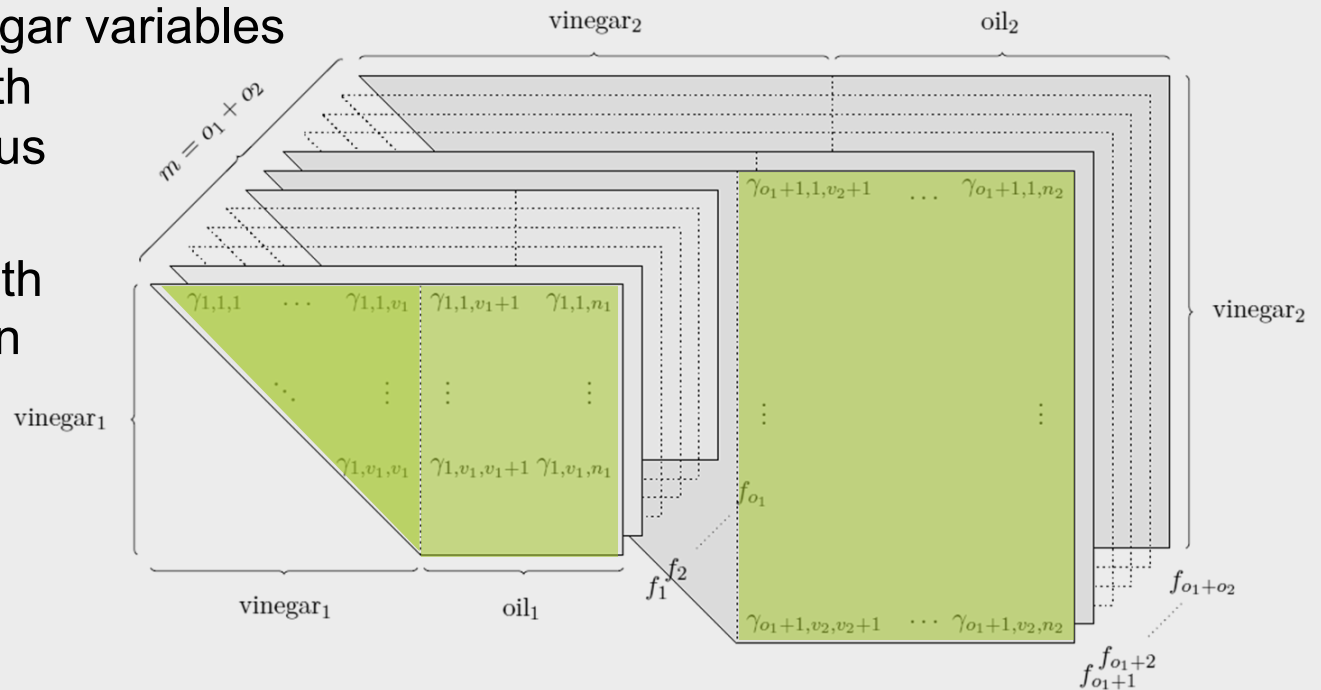


enTTS



Inverting Central Maps - Rainbow

- Two or more layers (like a Rainbow)
- Solve first layer as normal UOV instance
- In next layer fix vinegar variables not randomly but with solution from previous layer
- Solve layer again with Gaussian elimination



Rainbow(3,2,4) :

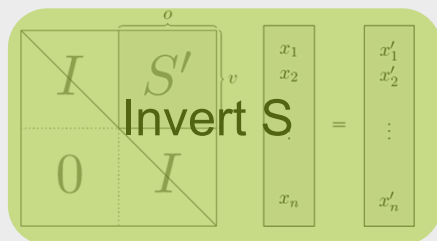
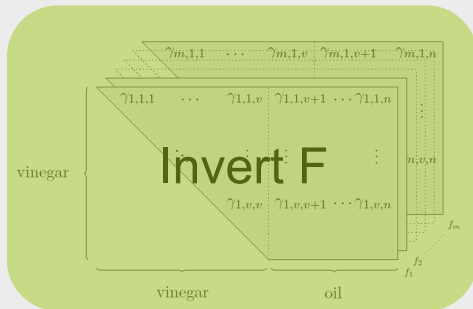
$x_1 x_2 x_3$

$x_4 x_5$

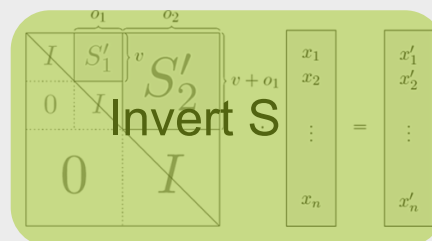
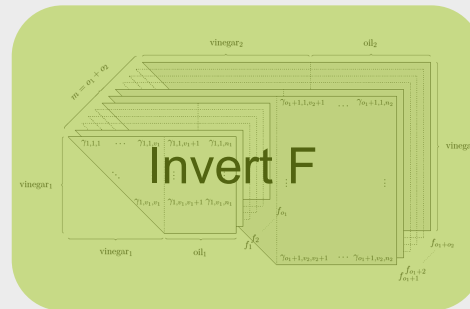
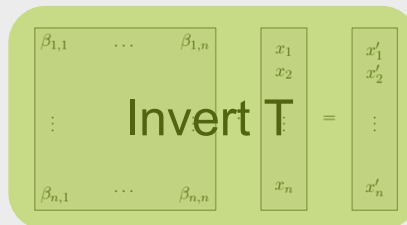
$x_6 x_7 x_8 x_9$

Schemes

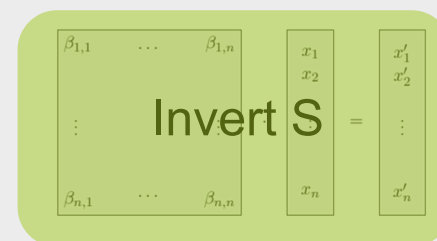
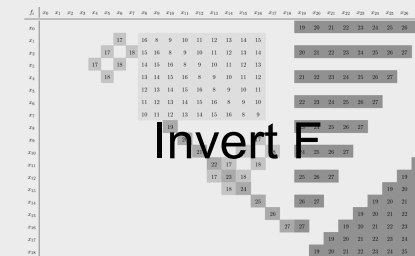
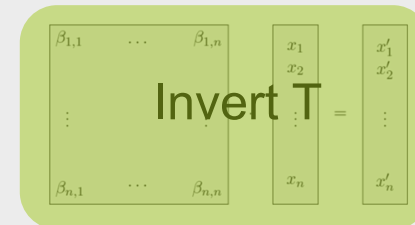
UOV



Rainbow



enTTS



Inverting Central Maps - enTTS

$$f_i = x_i + \sum_{j=1}^{2l-3} \gamma_{ij} x_j x_{2l-2+(i+j+1 \bmod 2l-1)} \quad \text{for } 2l-2 \leq i \leq 4l-4,$$

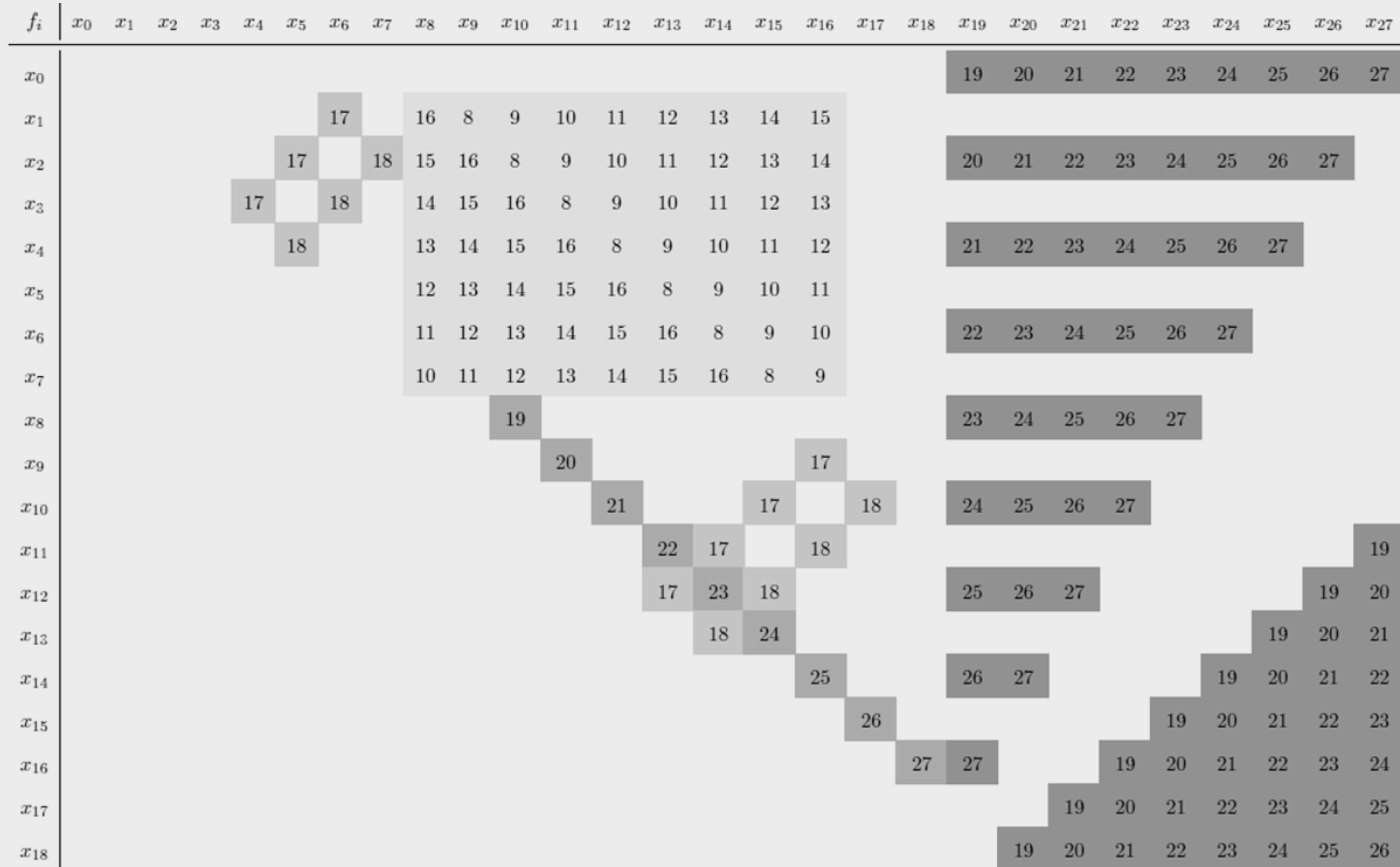
$$f_i = x_i + \sum_{j=1}^{l-2} \gamma_{ij} x_{i+j-(4l-3)} x_{i-j-2l} + \sum_{j=l-1}^{2l-3} \gamma_{ij} x_{i+j-3l+3} x_{i-j+l-2}$$

for $i = 4l-3$ or $4l-2$,

$$f_i = x_i + \gamma_{i0} x_{i-2l+1} x_{i-2l-1} + \sum_{j=4l-1}^i \gamma_{i,j-(4l-2)} x_{2(i-j)} x_j$$

$$+ \sum_{j=i+1}^{6l-3} \gamma_{i,j-(4l-2)} x_{4l-1+i-j} x_j \quad \text{for } 4l-1 \leq i \leq 6l-3$$

Inverting Central Maps – enTTS



Inverting Central Maps - enTTS

- enTTS Layer 1:
 - Fix x_1 to x_7 randomly
 - Multiply with coefficients to get a LES
 - Solve with Gaussian elimination

$$\begin{pmatrix}
 1 & p_{8,1}x_1 & p_{8,2}x_2 & p_{8,3}x_3 & p_{8,4}x_4 & p_{8,5}x_5 & p_{8,6}x_6 & p_{8,7}x_7 & 0 \\
 0 & 1 & p_{9,1}x_1 & p_{9,2}x_2 & p_{9,3}x_3 & p_{9,4}x_4 & p_{9,5}x_5 & p_{9,6}x_6 & p_{9,7}x_7 \\
 p_{10,7}x_7 & 0 & 1 & p_{10,1}x_1 & p_{10,2}x_2 & p_{10,3}x_3 & p_{10,4}x_4 & p_{10,5}x_5 & p_{10,6}x_6 \\
 p_{11,6}x_6 & p_{11,7}x_7 & 0 & 1 & p_{11,1}x_1 & p_{11,2}x_2 & p_{11,3}x_3 & p_{11,4}x_4 & p_{11,5}x_5 \\
 p_{12,5}x_5 & p_{12,6}x_6 & p_{12,7}x_7 & 0 & 1 & p_{12,1}x_1 & p_{12,2}x_2 & p_{12,3}x_3 & p_{12,4}x_4 \\
 p_{13,4}x_4 & p_{13,5}x_5 & p_{13,6}x_6 & p_{13,7}x_7 & 0 & 1 & p_{13,1}x_1 & p_{13,2}x_2 & p_{13,3}x_3 \\
 p_{14,3}x_3 & p_{14,4}x_4 & p_{14,5}x_5 & p_{14,6}x_6 & p_{14,7}x_7 & 0 & 1 & p_{14,1}x_1 & p_{14,2}x_2 \\
 p_{15,2}x_2 & p_{15,3}x_3 & p_{15,4}x_4 & p_{15,5}x_5 & p_{15,6}x_6 & p_{15,7}x_7 & 0 & 1 & p_{15,1}x_1 \\
 p_{16,1}x_1 & p_{16,2}x_2 & p_{16,3}x_3 & p_{16,4}x_4 & p_{16,5}x_5 & p_{16,6}x_6 & p_{16,7}x_7 & 0 & 1
 \end{pmatrix} \cdot \begin{pmatrix} x_8 \\ x_9 \\ x_{10} \\ x_{11} \\ x_{12} \\ x_{13} \\ x_{14} \\ x_{15} \\ x_{16} \end{pmatrix} = \begin{pmatrix} y_8 \\ y_9 \\ y_{10} \\ y_{11} \\ y_{12} \\ y_{13} \\ y_{14} \\ y_{15} \\ y_{16} \end{pmatrix}$$

enTTS(20,28) : x_0 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} x_{11} x_{12} x_{13} x_{14} x_{15} x_{16} x_{17} x_{18} x_{19} x_{20} x_{21} x_{22} x_{23} x_{24} x_{25} x_{26} x_{27}

Inverting Central Maps - enTTS

- enTTS Layer 2:
 - Can be solved directly

$$\begin{aligned}
 x_{17} &= y_{17} - p_{17,1}x_1x_6 - p_{17,2}x_2x_5 - p_{17,3}x_3x_4 - p_{17,4}x_9x_{16} - p_{17,5}x_{10}x_{15} - p_{17,6}x_{11}x_{14} - p_{17,7}x_{12}x_{13} \\
 x_{18} &= y_{18} - p_{18,1}x_2x_7 - p_{18,2}x_3x_6 - p_{18,3}x_4x_5 - p_{18,4}x_{10}x_{17} - p_{18,5}x_{11}x_{16} - p_{18,6}x_{12}x_{15} - p_{18,7}x_{13}x_{14}
 \end{aligned}$$

enTTS(20,28) : x_0 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} x_{11} x_{12} x_{13} x_{14} x_{15} x_{16} x_{17} x_{18} x_{19} x_{20} x_{21} x_{22} x_{23} x_{24} x_{25} x_{26} x_{27}

Inverting Central Maps - enTTS

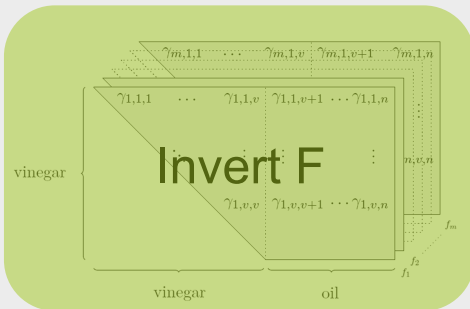
- enTTS Layer 3:
 - Fix x_0 randomly
 - Multiply already known values with coefficients to get a LES
 - Solve LES

$$\begin{pmatrix}
 1 + p_{19,1}x_0 & p_{19,2}x_{18} & p_{19,3}x_{17} & p_{19,4}x_{16} & p_{19,5}x_{15} & p_{19,6}x_{14} & p_{19,7}x_{13} & p_{19,8}x_{12} & p_{19,9}x_{11} \\
 p_{20,1}x_2 & 1 + p_{20,2}x_0 & p_{20,3}x_{18} & p_{20,4}x_{17} & p_{20,5}x_{16} & p_{20,6}x_{15} & p_{20,7}x_{14} & p_{20,8}x_{13} & p_{20,9}x_{12} \\
 p_{21,1}x_4 & p_{21,2}x_2 & 1 + p_{21,3}x_0 & p_{21,4}x_{18} & p_{21,5}x_{17} & p_{21,6}x_{16} & p_{21,7}x_{15} & p_{21,8}x_{14} & p_{21,9}x_{13} \\
 p_{22,1}x_6 & p_{22,2}x_4 & p_{22,3}x_2 & 1 + p_{22,4}x_0 & p_{22,5}x_{18} & p_{22,6}x_{17} & p_{22,7}x_{16} & p_{22,8}x_{15} & p_{22,9}x_{14} \\
 p_{23,1}x_8 & p_{23,2}x_6 & p_{23,3}x_4 & p_{23,4}x_2 & 1 + p_{23,5}x_0 & p_{23,6}x_{18} & p_{23,7}x_{17} & p_{23,8}x_{16} & p_{23,9}x_{15} \\
 p_{24,1}x_{10} & p_{24,2}x_8 & p_{24,3}x_6 & p_{24,4}x_4 & p_{24,5}x_2 & 1 + p_{24,6}x_0 & p_{24,7}x_{18} & p_{24,8}x_{17} & p_{24,9}x_{16} \\
 p_{25,1}x_{12} & p_{25,2}x_{10} & p_{25,3}x_8 & p_{25,4}x_6 & p_{25,5}x_4 & p_{25,6}x_2 & 1 + p_{25,7}x_0 & p_{25,8}x_{18} & p_{25,9}x_{17} \\
 p_{26,1}x_{14} & p_{26,2}x_{12} & p_{26,3}x_{10} & p_{26,4}x_8 & p_{26,5}x_6 & p_{26,6}x_4 & p_{26,7}x_2 & 1 + p_{26,8}x_0 & p_{26,9}x_{18} \\
 p_{27,1}x_{16} & p_{27,2}x_{14} & p_{27,3}x_{12} & p_{27,4}x_{10} & p_{27,5}x_8 & p_{27,6}x_6 & p_{27,7}x_4 & p_{27,8}x_2 & 1 + p_{27,9}x_0
 \end{pmatrix} \cdot \begin{pmatrix} x_{19} \\ x_{20} \\ x_{21} \\ x_{22} \\ x_{23} \\ x_{24} \\ x_{25} \\ x_{26} \\ x_{27} \end{pmatrix} = \begin{pmatrix} y_{19} - p_{19,0}x_8x_{10} \\ y_{20} - p_{20,0}x_9x_{11} \\ y_{21} - p_{21,0}x_{10}x_{12} \\ y_{22} - p_{22,0}x_{11}x_{13} \\ y_{23} - p_{23,0}x_{12}x_{14} \\ y_{24} - p_{24,0}x_{13}x_{15} \\ y_{25} - p_{25,0}x_{14}x_{16} \\ y_{26} - p_{26,0}x_{15}x_{17} \\ y_{27} - p_{27,0}x_{16}x_{18} \end{pmatrix}$$

enTTS(20,28) : $x_0 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} x_{11} x_{12} x_{13} x_{14} x_{15} x_{16} x_{17} x_{18} x_{19} x_{20} x_{21} x_{22} x_{23} x_{24} x_{25} x_{26} x_{27}$

Schemes

UOV



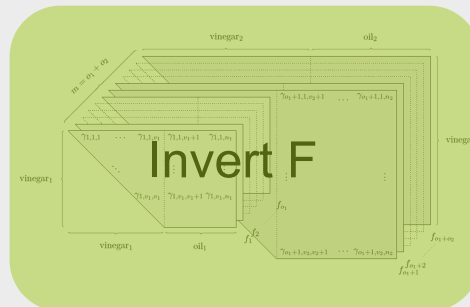
$$\begin{bmatrix} I & S' \\ 0 & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

Rainbow

$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert T



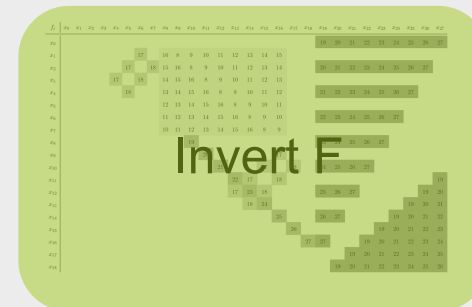
$$\begin{bmatrix} I & S'_1 & \dots & S'_v \\ 0 & I & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & I \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

enTTS

$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert T



$$\begin{bmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{bmatrix} \begin{matrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{matrix} = \begin{matrix} x'_1 \\ x'_2 \\ \vdots \\ x'_n \end{matrix}$$

Invert S

Optimizations - Reduced Polynomials

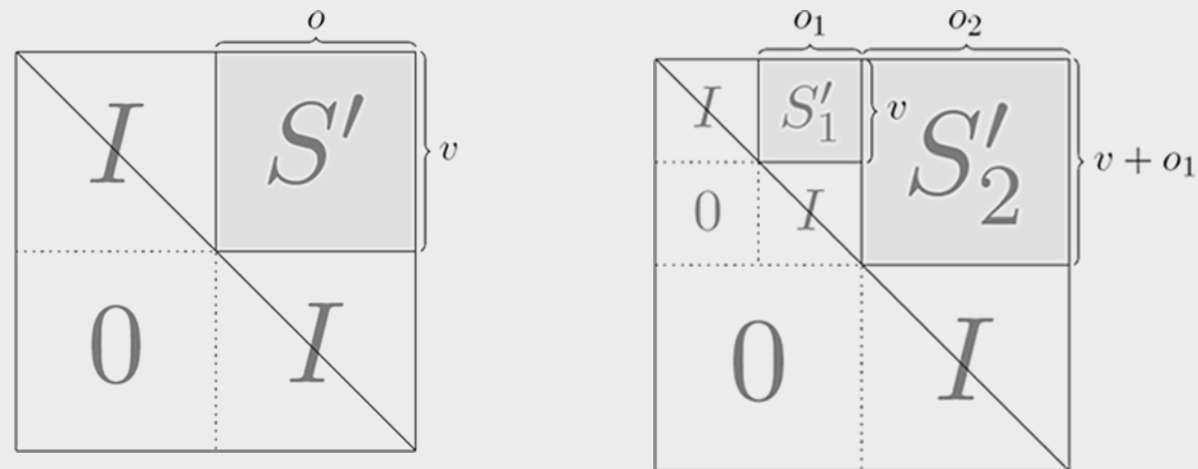
- Leaving out linear and constant terms in polynomials saves time and space
- Can be applied to UOV and Rainbow

$$p^{(k)}(x_1, \dots, x_n) := \sum_{1 \leq i < j \leq n} \gamma_{ij}^{(k)} x_i x_j + \sum_{1 \leq i \leq n} \beta_i^{(k)} x_i + \alpha^{(k)}$$

- In the linear transformations the constant parts are also left out

Optimizations - Self Invertible Linear Maps

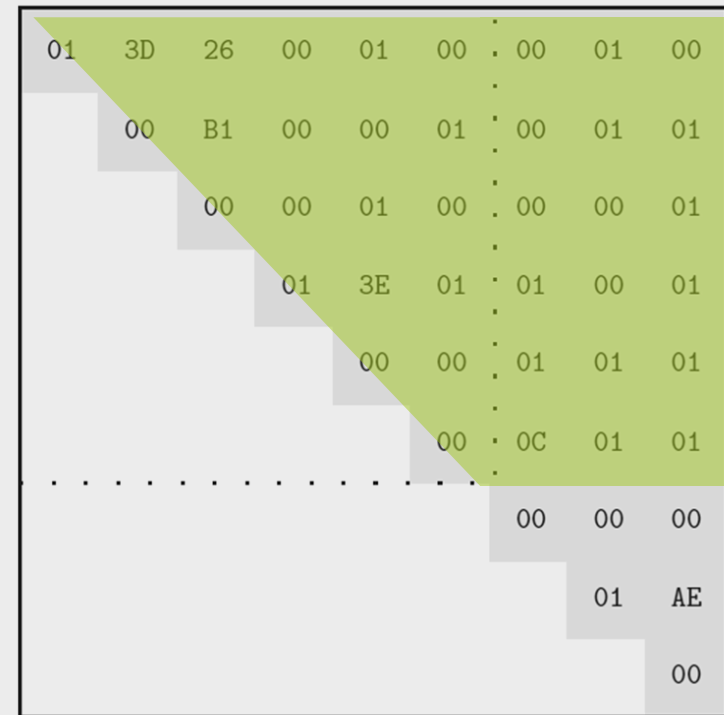
- In case of UOV and Rainbow S can be chosen of the form:



- S is self invertible $S^{-1} = S$, so no inversion is necessary.
- Multiplications in UOV signature generation are reduced from $n \cdot n$ to $o \cdot v$
- Private key is smaller

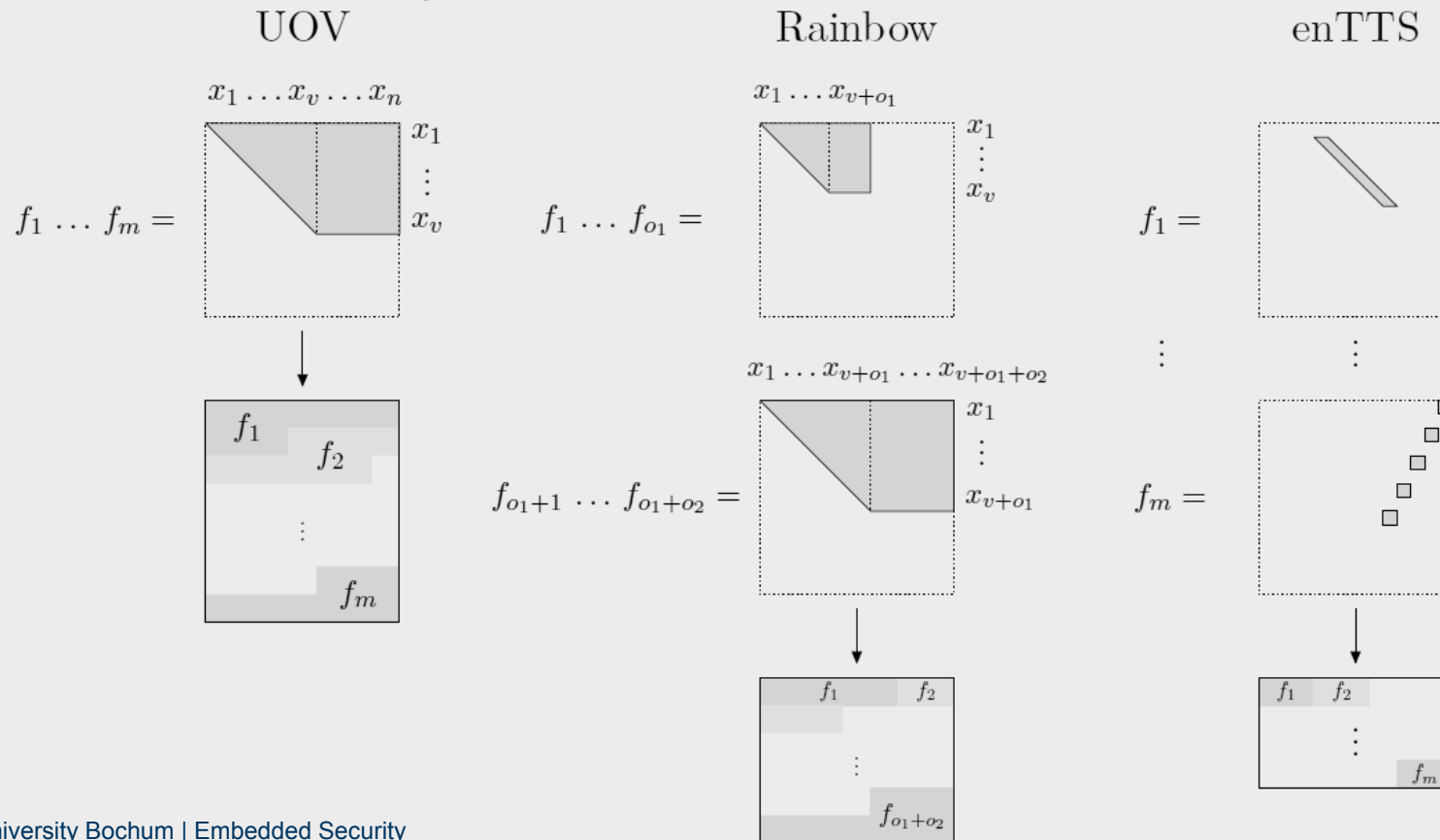
Optimizations - 0/1 UOV

- 0/1 UOV is an optimization for UOV
- Petzold, Thomae, Wolf et. al showed that large parts of the public key can be chosen randomly fixed
- This part can be treated as a system parameter and is not part of the public key anymore
- Faster verification is possible because the arithmetic in GF(2) is easier:
 - 1= copy or 0 = not
 - An additional check is necessary if an element is from GF(2) or GF(2⁸)
- Key generation: First choose P and then calculate F



Implementation - Central Map Memory Mapping

- Keys are saved without zeros
- Serial read out using `pointer++`



Implementation – Exponential Representation

- $GF(2^8)$ arithmetic with table look up
- Multiplication is addition in exponent mod (2^m-1)

$$\text{mul}(a,b) = \text{exp}(\text{log}(a)+\text{log}(b) \bmod (2^m-1)) \quad 3 \text{ pgm_read}()$$

- Saving memory access by keeping temporary results in exponential representation when next operation is a multiplication

$$\text{mul}(\text{mul}(a,b), c) = \text{exp}(\text{log}[\text{exp}(\text{log}(a)+\text{log}(b) \bmod (2^m-1))] + \text{log}[c] \bmod (2^m-1)) \quad 6 \text{ pgm_read}()$$

$$\text{mul}(\text{mul}(a,b), c) = \text{exp}((\text{log}(a)+\text{log}(b) \bmod (2^m-1)) + \text{log}[c] \bmod (2^m-1)) \quad 4 \text{ pgm_read}()$$

- Keys are saved in exponential representation, too.

Implementation – Generic Code

- Heavy use of #define
- Code generator for enTTS
- Increasing parameters is very easy

```

/* ----- SIZES ----- */
#define __O __M
#define __N (uint16_t) (__V+__O)
#define __LENGTH_OV (uint16_t) ((__O*__V)+((__V
#define __LENGTH_F (uint16_t) __LENGTH_OV*__M
#define __LENGTH_L (uint16_t) __N*__N
#define __LENGTH_P (uint16_t) (__M*(__N*(__N+1)
#define __D (uint16_t) ((__V*(__V+1))/2)
#define __D2 (uint16_t) ((__O*(__O+1))/2)

```

```

for(m=0; m<__M; m++) //all polynomials
{
    i=0;
    oil[m]=message[m]; //copy message to oil, because gauss awaits it in there later
    for(k=0; k<__V; k++)
    {
        for(j=k; j<__V; j++) // read in coefficients of F in exponential representation
        {
            oil[m] ^= mul_x_ee(vinegar_quadrat[i++],pgm_read_byte_far((pointer_f++)));
        }
        for(j=0; j<__O; j++) //vinegar x oil, both in exponential form
        {
            lgs[(m*__M)+j] ^= mul_x_ee(vinegar[k],pgm_read_byte_far((pointer_f++)));
        }
    }
}

```

Comparison – Parameter Choice

- Due to the 8bit micro controller GF(2⁸) was chosen as the field
- To be able to compare the schemes on equal conditions parameters for equal security levels are necessary
- For every scheme exist different attacks

Scheme	Security	Parameter	Direct attack	Band Separation	MinRank	HighRank	Kipnis-Shamir	Reconciliation
UOV (<i>o, v</i>)	2 ⁶⁴	(21, 28)	2 ⁶⁷ (<i>g</i> = 1)	-	-	-	2 ⁶⁶	2 ¹³¹ (<i>k</i> = 2)
	2 ⁸⁰	(28, 37)	2 ⁸⁵ (<i>g</i> = 1)	-	-	-	2 ⁸³	2 ¹⁶⁶ (<i>k</i> = 2)
	2 ¹²⁸	(44, 59)	2 ¹³⁰ (<i>g</i> = 1)	-	-	-	2 ¹³⁴	2 ²⁵⁶ (<i>k</i> = 2)
Rainbow (<i>v, o₁, o₂</i>)	2 ⁶⁴	(15, 10, 10)	2 ⁶⁷ (<i>g</i> = 1)	2 ⁷⁰	2 ¹⁴¹	2 ⁹³	2 ¹²⁵	2 ²⁴² (<i>k</i> = 6)
	2 ⁸⁰	(18, 13, 14)	2 ⁸⁵ (<i>g</i> = 1)	2 ⁸¹	2 ¹⁶⁷	2 ¹²⁶	2 ¹⁴³	2 ²⁵⁴ (<i>k</i> = 5)
	2 ¹²⁸	(36, 21, 22)	2 ¹³¹ (<i>g</i> = 2)	2 ¹³¹	2 ³¹³	2 ¹⁹²	2 ²⁹⁰	2 ⁵²³ (<i>k</i> = 7)
enTTS (<i>ℓ, m, n</i>)	2 ⁶⁴	(7, 28, 40)	2 ⁸⁹ (<i>g</i> = 1)	2 ⁶⁸	2 ¹²⁶	2 ¹¹⁷	2 ¹²⁷	-
	2 ⁸⁰	(9, 36, 52)	2 ¹¹⁰ (<i>g</i> = 2)	2 ⁸⁵	2 ¹⁵⁹	2 ¹⁵¹	2 ¹⁶⁰	-
	2 ¹²⁸	(15, 60, 88)	2 ¹⁷⁶ (<i>g</i> = 3)	2 ¹³¹	2 ²⁵⁸	2 ²⁴⁹	2 ²⁵⁹	-

Comparison - Sign

	Scheme	n	m	private Key [Byte]	Parameter [Byte]	Clockcycles x 1000	Time[ms] @32MHz	Code Size [Byte]
	enTTS(5, 20, 28)	28	20	1351	*	153	4.79	12890
	enTTS(5, 20, 28)[YCCC06]	28	20	1417	*	568 ¹	17.75 ²	-
2 ⁶⁴	UOV(21, 28)	49	21	21462	*	1,615	50.49	2188
	0/1 UOV(21, 28)	49	21	12936	8526	1,577	49.29	2258
	Rainbow(15, 10, 10)	35	20	9250	*	848	26.51	4162
	enTTS(7, 28, 40)	40	28	2731	*	332	10.37	24898
2 ⁸⁰	UOV(28, 37)	65	28	49728	*	3,637	113.66	2188
	0/1 UOV(28, 37)	65	28	30044	19684	3,526	110.20	2258
	Rainbow(18, 13, 14)	45	27	19682	*	1,740	54.38	4162
	enTTS(9, 36, 52)	52	36	4591	*	609	19.03	41232
2 ¹²⁸	UOV(44, 59)	103	44	194700	*	13,314	416.07	2188
	0/1 UOV(44, 59)	103	44	116820	77880	12,782	399.43	2258
	Rainbow(36, 21, 22)	79	43	97675	*	8,227	257.11	4162
	enTTS(15, 60, 88)	88	60	13051	*	2,142	66.94	116698

Comparison - Verify

	Scheme	n	m	public Key [Byte]	Parameter [Byte]	Clockcycles x 1000	Time[ms] @32MHz	Code Size [Byte]
2 ⁶⁴	enTTS(5, 20, 28)	28	20	8120	*	1,126	35.22	827
	enTTS(5, 20, 28)[YCCC06]	28	20	8680	*	5,808 ¹	181.5 ²	-
	UOV(21, 28)	49	21	25725	*	1,690	52.83	466
	0/1 UOV(21, 28)	49	21	4851	20874	1,395	43.60	578
2 ⁸⁰	Rainbow(15, 10, 10)	35	20	12600	*	1,010	31.58	466
	enTTS(7, 28, 40)	40	28	22960	*	2,558	79.95	827
	UOV(28, 37)	65	28	60060	*	3,911	122.23	466
	0/1 UOV(28, 37)	65	28	11368	48692	3,211	100.37	578
2 ¹²⁸	Rainbow(18, 13, 14)	45	27	27945	*	2,214	69.19	466
	enTTS(9, 36, 52)	52	36	49608	*	6,658	208.07	827
	UOV(44, 59)	103	44	235664	*	14,134	441.70	466
	0/1 UOV(44, 59)	103	44	43560	192104	13,569	424.04	578
2 ¹²⁸	Rainbow(36, 21, 22)	79	43	135880	*	9,216	288.01	466
	enTTS(15, 60, 88)	88	60	234960	*	3,0789	962.17	827

Comparison – Other Schemes

- Our implementations:
 - enTTS(5,20,28) [security < 2^{64}] sign in 4.79 ms / verify 35.22 ms
 - enTTS(9,36,52) [2^{80}] sign in 19.03 ms / verify in 208.07 ms
 - Rainbow(18,13,17) [2^{80}] sign in 54.38 ms / verify in 69.19 ms

- Other schemes:

Method	Time[ms]@32MHz	
	sign	verify
enTTS(5, 20, 28)[YCCC06]	17.75 ¹	181.5 ¹
ECC-P160 (SECG) [GPW ⁺ 04]	203 ¹	203 ¹
ECC-P192 (SECG) [GPW ⁺ 04]	310 ¹	310 ¹
ECC-P224 (SECG) [GPW ⁺ 04]	548 ¹	548 ¹
RSA-1024 [GPW ⁺ 04]	2,748 ¹	108 ¹
RSA-2048 [GPW ⁺ 04]	20,815 ¹	485 ¹
NTRU-251-127-31 sign [DPP08]	143 ¹	-

Conclusion

Rainbow
Verification time
Public key size

enTTS
Signature time
Secret key size

UOV & 0/1 UOV
Code size
(Public key size)

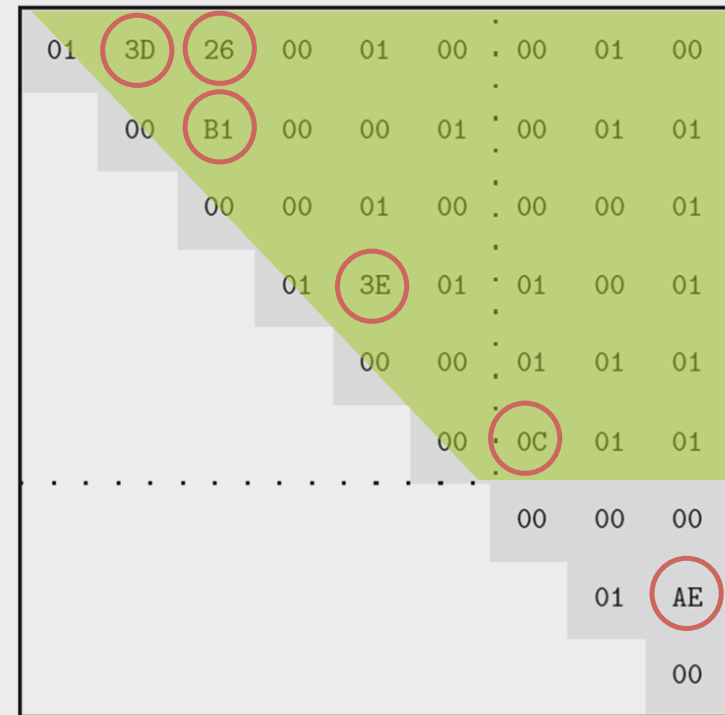
Future aspects

- 0/1 UOV could be improved by using a generated or cyclic system parameter instead a fixed one
- 0/1 UOV could save 8 elements in one byte instead of saving 1 bit in a byte
- The focus of this work was on fast schemes, the code size / time trade-off could be investigated further
- Assembler implementations could speed up the schemes even more

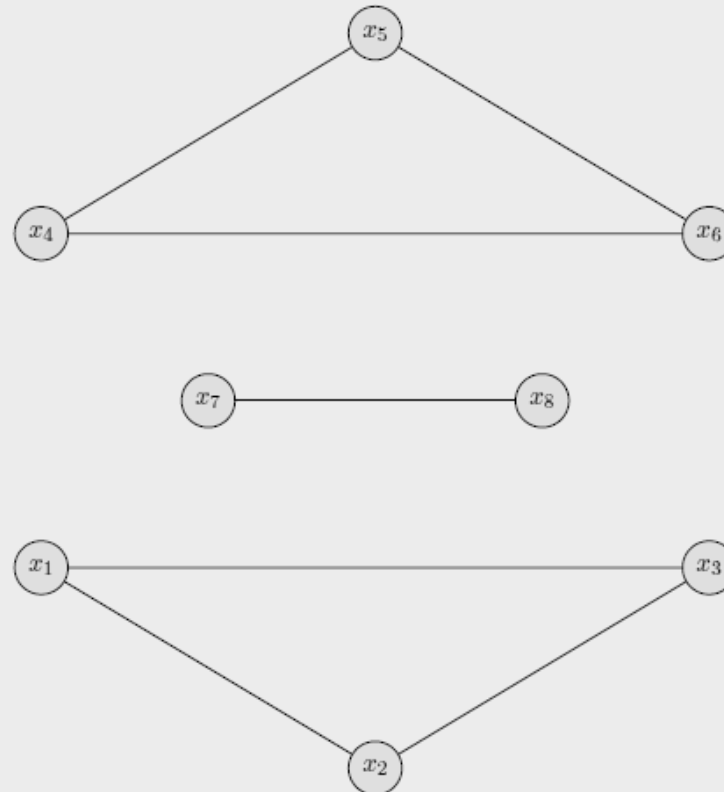
**Thank you for your attention.
Any Questions?**

Optimizations - 0/1 UOV

- To prevent a reduction of the key to elements only from GF(2), a special monomial ordering is necessary
- Elements must be combined in a way that even when many GF(2⁸) elements are fixed the key has still elements from GF(2⁸)



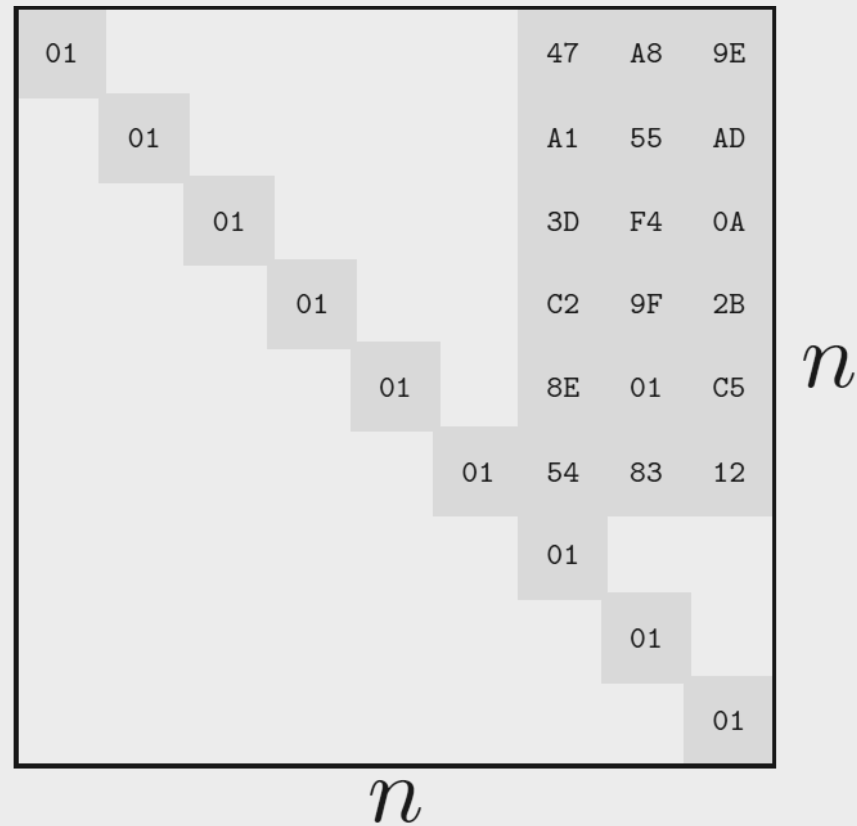
0/1 UOV Key Gen – Complementary Turan Graph



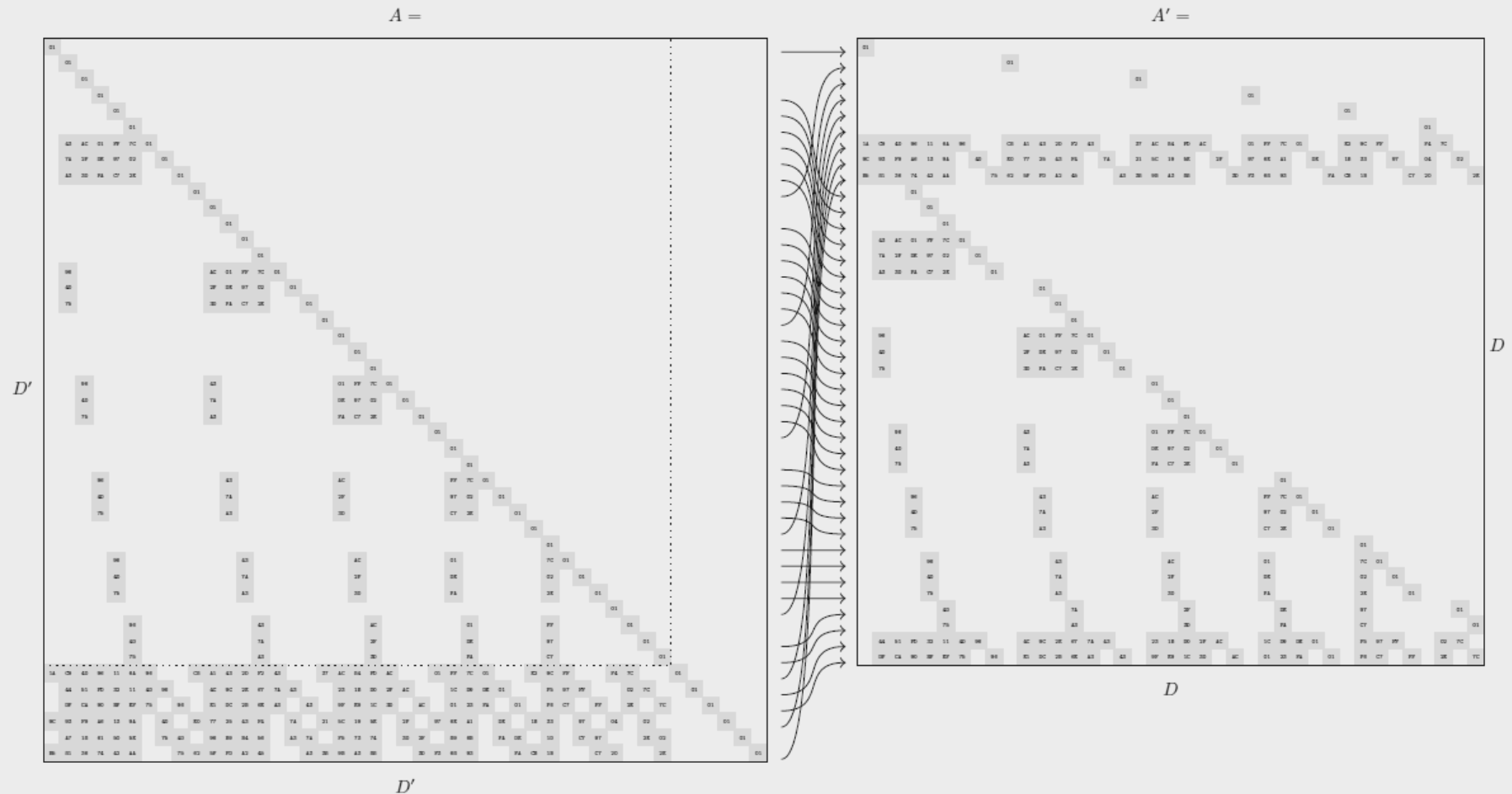
$$\dots + x_1x_2 + x_1x_3 + x_2x_3 + x_4x_5 + x_4x_6 + x_5x_8 + x_7x_8$$

0/1 UOV Key Gen – Choosing S

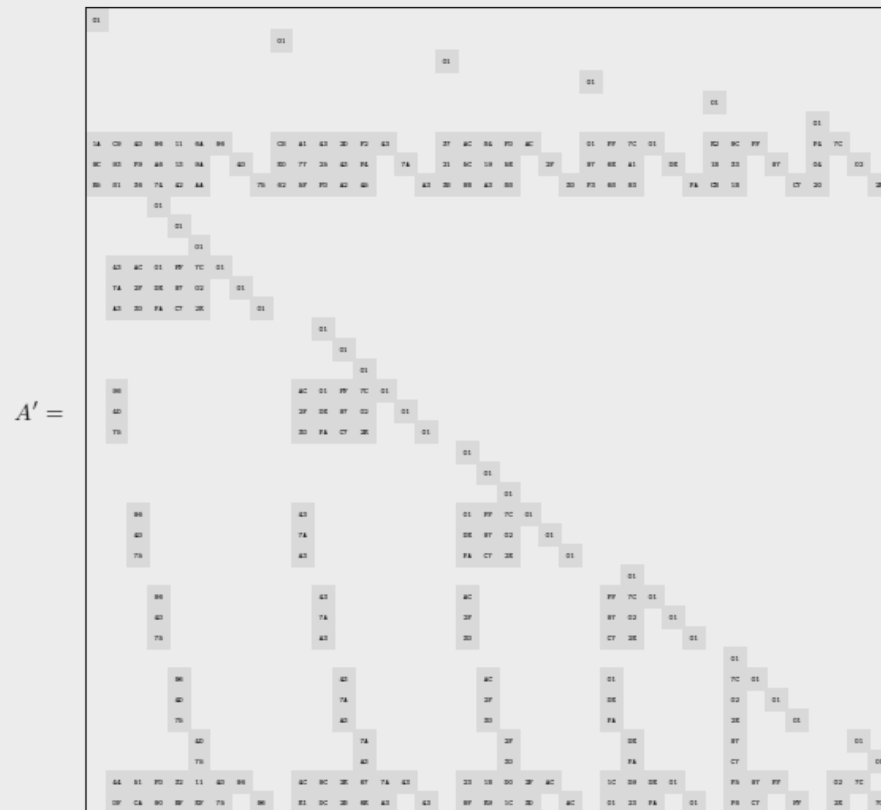
$$S = S^{-1} =$$



0/1 UOV Key Gen – Calculating A



0/1 UOV Key Gen – Inverting A



0/1 UOV Key Gen – Calculating F and P

$$F = B \cdot A'^{-1}$$

$f_1, f_2, f_3 =$

01	3D	25	00	01	00	A8	8D	33
	00	B1	00	00	01	54	3C	CB
		00	00	01	00	0E	C8	2E
			01	2E	01	23	09	D6
				00	00	05	90	C1
					00	4E	A5	5B

00	27	57	00	01	01	E7	1D	C1
	01	5F	00	01	00	2D	51	DD
		00	00	00	01	F0	5C	04
			00	B2	01	F0	6C	8F
				01	01	2A	3A	CB
					00	6E	2A	75

00	7E	8F	00	01	00	47	7E	05
	00	94	00	00	00	53	D2	4D
		01	01	01	00	CE	90	2F
			00	A4	01	FE	00	8F
				00	01	E2	D2	47
					01	50	49	2B

$$P = F \cdot A$$

$p_1, p_2, p_3 =$

01	3D	25	00	01	00	00	01	00
	00	B1	00	00	01	00	01	01
		00	00	01	00	00	00	01
			01	2E	01	01	00	01
				00	00	01	01	01
					00	0C	01	01
						00	00	00
							01	8E
								00

00	27	57	00	01	01	01	00	00
	01	5F	00	01	00	00	00	00
		00	00	00	01	00	00	01
			00	B2	01	00	01	01
				01	01	01	01	01
					00	A8	01	00
						00	00	01
							00	4F
								01

00	7E	8F	00	01	00	00	01	00
	00	94	00	00	00	00	00	00
		01	01	01	00	00	00	01
			00	A4	01	01	00	01
				00	01	00	00	00
					01	9E	00	00
							01	01
								00
								45
								00