A Differential Fault Attack on MICKEY 2.0

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Abstract. In this paper we present a differential fault attack on the stream cipher MICKEY 2.0 which is in eStream's hardware portfolio. While fault attacks have already been reported against the other two eStream hardware candidates Trivium and Grain, no such analysis is known for MICKEY. Using the standard assumptions for fault attacks, we show that if the adversary can induce random single bit faults in the internal state of the cipher, then by injecting around $2^{16.7}$ faults and performing $2^{32.5}$ computations on an average, it is possible to recover the entire internal state of MICKEY at the beginning of the key-stream generation phase. We further consider the scenario where the fault may affect at most three neighbouring bits and in that case we require around $2^{18.4}$ faults on an average.

Keywords: eStream, Fault attacks, MICKEY 2.0, Stream Cipher.

1 Introduction

The stream cipher MICKEY 2.0 [4] was designed by Steve Babbage and Matthew Dodd as a submission to the eStream project. The cipher has been selected as a part of eStream's final hardware portfolio. MICKEY is a synchronous, bitoriented stream cipher designed for low hardware complexity and high speed. After a TMD tradeoff attack [16] against the initial version of MICKEY (version 1), the designers responded by tweaking the design by increasing the state size from 160 to 200 bits and altering the values of some control bit tap locations. These changes were incorporated in MICKEY 2.0 and these are the only differences between MICKEY version 1 and MICKEY 2.0. While MICKEY 2.0 uses an 80-bit key and a variable length IV, a modified version of the cipher, MICKEY-128 2.0 that uses a 128-bit key [5] was also proposed by the designers.

The name MICKEY is derived from "Mutual Irregular Clocking Key-stream generator" which describes the behavior of the cipher. The state consists of two 100-bit shift registers named R and S, each of which is irregularly clocked and controlled by the other. The cipher specification underlines that each key can be used with up to 2^{40} different IVs of the same length, and that 2^{40} key-stream bits can be generated from each key-IV pair. Very little cryptanalysis of MICKEY 2.0 is available in literature. In fact it has been noted in [3, Section 3.2] that other than the observation related to time or power analysis attacks [12] on

straightforward implementations of the MICKEY family, there have been no known cryptanalytic advances on these ciphers. To the best our knowledge, the work in this paper presents the first cryptanalytic result of MICKEY 2.0 in terms of differential fault attack.

Since the work of [6,7], fault attacks have been employed to test the strengths and weaknesses of cryptographic primitives. Such attacks on stream ciphers was first described by Hoch and Shamir [13]. A typical fault attack [13] involves the random injection of faults (using laser shots/clock glitches [18, 19]) in a device (typically initialized by a secret key) which changes one or more bits of its internal state. The adversary then attempts to deduce information about the internal state/secret key using the output stream from this faulty device. In order to perform the attack, certain privileges are required like the ability to re-key the device, control the timing of the fault etc. The attack becomes impractical and unrealistic if the adversary is granted too many privileges. In this work we assume the following privileges of the adversary which are generally acceptable in cryptanalytic literature:

- She can re-key the cipher with the original key-IV and restart cipher operations multiple times.
- 2. She has precise control over the timing of fault injection.
- 3. Initially we assume that she can inject a fault that alters the bit value of one random register location in either the R or the S register. Later, in Section 4, we explore the situation when she can inject a fault that may affect more than one value in contiguous register locations. We present explicit results considering the events when upto three contiguous register locations may be affected in R or S.
- 4. She is however unable to fix the exact location of the R or S register where she wants to inject the fault. Obtaining the fault location by comparison of the fault-free and the faulty key-streams is one of the challenges while mounting the fault attack.

There are published works where the assumptions made are quite strong and requires the adversary to have more control over fault injections, e.g., the works [9, 11,17] consider that the attacker can reproduce multiple faults in the same (but unknown) locations. A detailed physical implementation using such fault model is presented in [11, Section IIIB]. In this work we use a more relaxed fault model in which the adversary is not required to fault an unknown register location multiple number of times.

Differential fault attack is a special class of fault attack in which the attacker uses the difference between fault-free and faultless key-streams to deduce the internal state or the secret key of the cipher. In case of MICKEY 2.0, the differential attack is possible due to the rather simplistic nature of the output function $(r_0 + s_0)$ used to produce key-stream bits. Additionally, there are some interesting properties of the state update function in MICKEY that help facilitate the attack that we shall describe.

The organization of the paper is as follows. In Section 2, we present a description of the cipher which is suitable for our analysis, where we also present

some notations that will be henceforth used in the paper. The complete attack assuming that the adversary is able to induce single bit faults in random register locations is described in Section 3. In Section 4 we explore the case when the adversary is able to induce a fault that affects the bit values of (random) consecutive (upto 3) register locations. Section 5 concludes the paper.

2 Our description of MICKEY 2.0 PRGA and some notations

A detailed description of MICKEY 2.0 is available in [4]. It uses an 80-bit key and a variable length IV, the length of which may be between 0 and 80 bits. The physical structure of the cipher consists of two 100 bit registers R and S. Both registers are initially initialized to the all-zero state, and the three stages of register update 1. IV loading, 2. Key Loading, and 3. Pre Clock are executed sequentially before the production of the first key-stream bit. Thereafter in the PRGA (Pseudo Random bitstream Generation Algorithm) key-stream bits are produced. We will try to give an alternate description of this stage of operation of MICKEY 2.0. Consider a_0, a_1, a_2, a_3 to be variables over GF(2). Let a_0 be defined as $a_0 = a_2$, if $a_1 = 0$ and $a_0 = a_3$, if $a_1 = 1$. Then it is straightforward to see that a_0 can be expressed as a multivariate polynomial over GF(2), i.e., $a_0 = (1 + a_1) \cdot a_2 + a_1 \cdot a_3$. The state registers R and S, during the PRGA are updated by a call to the CLOCK_KG routine, which in turn calls the CLOCK_R and the CLOCK_S routine. In both these routines state update is done via a number of If-Else constructs. As a result of this the state update may be equivalently expressed as a series of multi-variate polynomials over GF(2). Let $r_0, r_1, \ldots, r_{99}, s_0, s_1, \ldots, s_{99}$ denote the internal state at a certain round during the MICKEY PRGA and let $r_0', r_1', \dots, r_{99}', s_0', s_1', \dots, s_{99}'$ denote the internal state at the next round. Then it is possible to write r'_i $\rho_i(r_0, r_1, \dots, r_{99}, s_0, s_1, \dots, s_{99}), s'_i = \beta_i(r_0, r_1, \dots, r_{99}, s_0, s_1, \dots, s_{99}), \forall i \in$ [0,99], where ρ_i,β_i are polynomial functions over GF(2). The exact forms of ρ_i, β_i are described in Appendix A. Before describing the attack we will describe certain notations that will be used henceforth.

- 1. $R_t = [r_0^t, r_1^t, \dots, r_{99}^t], S_t = [s_0^t, s_1^t, \dots, s_{99}^t]$ is used to denote the internal states of the R, S registers at the beginning of the round t of the PRGA. That is, r_i^t , s_i^t respectively denotes the i^{th} bit of the registers R, S at the beginning of round t of the PRGA. Note that $r_i^{t+1} = \rho_i(R_t, S_t)$ and $s_i^{t+1} = \beta_i(R_t, S_t)$.
- 2. The value of the variables $CONTROL_BIT_R$, $CONTROL_BIT_S$ at the PRGA round t are denoted by the variables CR_t , CS_t respectively. These bits are used by the R, S registers to exercise mutual self control over each other. Note that $CR_t = r_{67}^t + s_{34}^t$ and $CS_t = r_{33}^t + s_{67}^t$.
- 3. $R_{t,\Delta r_{\phi}}(t_0), S_{t,\Delta r_{\phi}}(t_0)$ (resp. $R_{t,\Delta s_{\phi}}(t_0), S_{t,\Delta s_{\phi}}(t_0)$) are used to denote the internal states of the cipher at the beginning of round t of the PRGA, when a fault has been injected in location ϕ of R (resp. S) at the beginning of round t_0 of the PRGA.

4. $z_{i,\Delta r_{\phi}}(t_0)$ or $z_{i,\Delta s_{\phi}}(t_0)$ denotes the key-stream bit produced in the i^{th} PRGA round, after a fault has been injected in location ϕ of R or S at the beginning of round t_0 of the PRGA. By z_i , we refer to the fault-free key-stream bit produced in the i^{th} PRGA round.

3 Complete description of the Attack

We will start with a few algorithmic tools that will be used later to mount the attack.

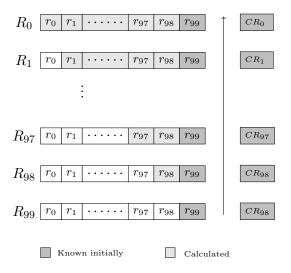


Fig. 1: Constructing the state R_0 . Starting from PRGA round 99, any bit calculated at PRGA round i is used to determine state bits of round i-1.

Lemma 1. Consider the first 100 states of the MICKEY 2.0 PRGA. If r_{99}^t and CR_t are known $\forall t \in [0, 99]$, then the initial state R_0 may be calculated efficiently.

Proof. Let the values of r_{99}^t and CR_t be known $\forall t \in [0,99]$. We will begin by noticing that the functions ρ_i for all values of $i \in [1,99]$ are of the form $\rho_i(\cdot) = r_{i-1} + (s_{34} + r_{67}) \cdot r_i + \alpha_i \cdot r_{99}$, where $s_{34} + r_{67}$ is the value of $CONTROL_BIT_R$. $\alpha_i = 1$, if $i \in RTAPS$ (this is a set of tap locations related to the design of MICKEY 2.0, see [4]) and is 0 otherwise. Now consider the following equation governing r_{99}^{09} :

$$r_{99}^{99} = \rho_{99}(R_{98}, S_{98}) = r_{98}^{98} + CR_{98} \cdot r_{99}^{98} + \alpha_{99} \cdot r_{99}^{98}.$$

In the above equation, r_{98}^{98} is the only unknown and it appears as a linear term, and so its value can be calculated immediately. We therefore know the values of

2 state bits of R_{98} : r_{99}^{98} , r_{98}^{98} . Similarly look at the equations governing r_{99}^{98} , r_{98}^{98} .

$$r_{99}^{98} = r_{98}^{97} + CR_{97} \cdot r_{99}^{97} + \alpha_{99} \cdot r_{99}^{97}, \ r_{98}^{98} = r_{97}^{97} + CR_{97} \cdot r_{98}^{97} + \alpha_{98} \cdot r_{99}^{97}.$$

As before, r_{98}^{97} is the lone unknown term in the first equation whose value is determined immediately. After this r_{97}^{97} becomes the only unknown linear term in the next equation whose value too is determined easily. Thus we know 3 bits of R_{97} : r_{97+i}^{97} , i=0,1,2. Continuing in such a bottom up manner we can successively determine 4 bits of R_{96} , 5 bits of R_{95} and eventually all the 100 bits of R_{0} . The process is explained pictorially in Figure 1.

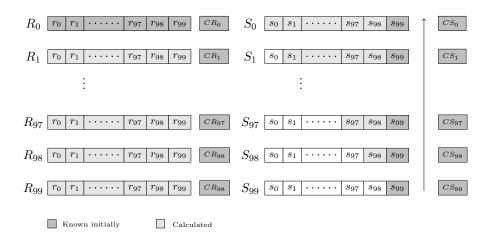


Fig. 2: Constructing the state S_0 . Starting from PRGA round 99, any bit calculated at PRGA round i is used to determine state bits of round i-1.

Lemma 2. Consider the first 100 states of the MICKEY 2.0 PRGA. If R_0 is known and s_{99}^t , CS_t , CR_t are known $\forall t \in [0, 99]$, then the initial state S_0 of the register S can be determined efficiently.

Proof. Since R_0 is known and so is CR_t for each $t \in [0, 99]$ we can construct all the bits of R_1 by calculating

$$r_i^1 = r_{i-1}^0 + CR_0 \cdot r_i^0 + \alpha_i \cdot r_{99}^0, \ \forall i \in [1, 99],$$

and r_0^1 is given as $r_0^0 \cdot CR_0 + r_{99}^0$. Once all the bits of R_1 are known, all the bits of R_2 may be determined by calculating

$$r_i^2 = r_{i-1}^1 + CR_1 \cdot r_i^1 + \alpha_i \cdot r_{99}^1, \ \forall i \in [1, 99],$$

and $r_0^2 = r_0^1 \cdot CR_1 + r_{99}^1$. Similarly all the bits of R_3, R_4, \dots, R_{99} can be calculated successively. As before, we begin by observing that the functions β_i for all values

of $i \in [1, 99]$ are of the form

$$\beta_i(\cdot) = s_{i-1} + \lambda_i \cdot (s_{67} + r_{33}) \cdot s_{99} + \hat{\beta}_i(s_i, s_{i+1}, \dots, s_{99}),$$

where $s_{67} + r_{33}$ is the value of $CONTROL_BIT_S$ and $\hat{\beta}_i$ is a function that depends on $s_i, s_{i+1}, \ldots, s_{99}$ but not any of $s_0, s_1, \ldots, s_{i-1}$. $\lambda_i = 1$ if $FB0_i \neq FB1_i$ (these are bit sequences related to the design of MICKEY 2.0, see [4]) and is 0 otherwise. Now consider the following equation governing s_{99}^{99} :

$$s_{99}^{99} = \beta_{99}(R_{98}, S_{98}) = s_{98}^{98} + \lambda_{99} \cdot CS_{98} \cdot s_{99}^{98} + \hat{\beta}_{99}(s_{99}^{98}).$$

In the above equation s_{98}^{98} is the only unknown and it appears as a linear term, and so its value can be calculated immediately. We therefore know the values of the 2 state bits of S_{98} : s_{99}^{98} , s_{98}^{98} . Similarly look at the equations governing s_{99}^{98} , s_{98}^{98} :

$$s_{99}^{98} = s_{98}^{97} + \lambda_{99} \cdot CS_{97} \cdot s_{99}^{97} + \hat{\beta}_{99}(s_{99}^{97}),$$

$$s_{98}^{98} = s_{97}^{97} + \lambda_{98} \cdot CS_{97} \cdot s_{99}^{97} + \hat{\beta}_{98}(s_{98}^{97}, s_{99}^{97}).$$

As before, s_{98}^{97} is the lone unknown term in the first equation whose value is determined immediately. After this s_{97}^{97} becomes the only unknown linear term in the next equation whose value too is determined easily. Thus we know 3 bits of S_{97} : s_{97+i}^{97} , i = 0, 1, 2. Continuing in such a bottom up manner we can successively determine 4 bits of S_{96} , 5 bits of S_{95} and eventually all the 100 bits of S_{0} . The process is explained pictorially in Figure 2.

3.1 Faulting specific bits of R, S

Before getting into the details of the attack, we further note that the output key-stream bits z_t, z_{t+1}, \ldots can also be expressed as polynomial functions over R_t, S_t . We have

$$z_{t} = r_{0}^{t} + s_{0}^{t} = \theta_{0}(R_{t}, S_{t}),$$

$$z_{t+1} = r_{0}^{t+1} + s_{0}^{t+1} = \rho_{0}(R_{t}, S_{t}) + \beta_{0}(R_{t}, S_{t}) = \theta_{1}(R_{t}, S_{t}),$$

$$z_{t+2} = r_{0}^{t+2} + s_{0}^{t+2} = \rho_{0}(R_{t+1}, S_{t+1}) + \beta_{0}(R_{t+1}, S_{t+1}) = \theta_{2}(R_{t}, S_{t})$$

The exact forms of $\theta_0, \theta_1, \theta_2$ are given in Table 1.

In the rest of this section we will assume that the adversary is able to (a) re-key the device containing the cipher with the original key-IV, (b) apply faults to specific bit locations in the R, S registers and (c) exercise control over the timing of fault injection. Note that (b) is a stronger assumption, but we do not need it in our attack. We are using this assumption here to build a sub-routine. In the next subsection we shall demonstrate how the adversary can partially identify the location of any fault injected at a random position by comparing the faulty and fault-free key-streams.

We begin by observing the following differential properties of the functions $\theta_0, \theta_1, \theta_2$.

Table 1: The functions θ_i

i	$\ heta_i(\cdot)$
0	$r_0 + s_0$
1	$r_0 \cdot r_{67} + r_0 \cdot s_{34} + r_{99} + s_{99}$
2	$r_0 \cdot r_{66} \cdot r_{67} + r_0 \cdot r_{66} \cdot s_{34} + r_0 \cdot r_{67} \cdot r_{99} + r_0 \cdot r_{67} \cdot s_{33} + r_0 \cdot r_{67} \cdot s_{34} \cdot s_{35} + r_0 \cdot r_{67} \cdot s$
	$ r_0 \cdot r_{67} \cdot s_{34} + r_0 \cdot r_{67} + r_0 \cdot r_{99} \cdot s_{34} + r_0 \cdot s_{33} \cdot s_{34} + r_0 \cdot s_{34} \cdot s_{35} + r_{33} \cdot s_{99} + r_{99} \cdot s_{34} \cdot s_{35} + r_{33} \cdot s_{99} + r_{99} \cdot s_{34} \cdot s_{35} + r_{99} \cdot s_{34} + r_{99} \cdot s_{34$
	$r_{66} \cdot r_{99} + r_{67} \cdot r_{99} \cdot s_{34} + r_{98} + r_{99} \cdot s_{33} + r_{99} \cdot s_{34} \cdot s_{35} + r_{99} \cdot s_{34} + r_{99} + r_{99} \cdot s_{34} + r_{99} \cdot s$
	$s_{67} \cdot s_{99} + s_{98}$

- (1) $\theta_1(\ldots, r_{67}, \ldots) + \theta_1(\ldots, 1 + r_{67}, \ldots) = r_0$
- (2) $\theta_1(r_0,\ldots) + \theta_1(1+r_0,\ldots) = s_{34}+r_{67}$
- (3) $\theta_2(\ldots, s_{99}) + \theta_2(\ldots, 1 + s_{99}) = s_{67} + r_{33}$

These differential properties have the following immediate implications.

$$z_{t+1} + z_{t+1,\Delta r_{67}}(t) = \theta_1(R_t, S_t) + \theta_1(R_{t,\Delta r_{67}}(t), S_{t,\Delta r_{67}}(t)) = r_0^t$$
 (1)

$$z_{t+1} + z_{t+1,\Delta r_0}(t) = \theta_1(R_t, S_t) + \theta_1(R_{t,\Delta r_0}(t), S_{t,\Delta r_0}(t)) = s_{34}^t + r_{67}^t = CR_t$$
(2)

$$z_{t+2} + z_{t+2,\Delta s_{99}}(t) = \theta_2(R_t, S_t) + \theta_2(R_{t,\Delta s_{99}}(t), S_{t,\Delta s_{99}}(t)) = s_{67}^t + r_{33}^t = CS_t \quad (3)$$

The above equations hold for all the values of $t=0,1,2,\ldots$ This implies that if the adversary is able to re-key the device with the original key-IV pair multiple times and apply faults at PRGA rounds $t=0,1,2,3,\ldots,100$ at precisely¹ the R register locations 0,67 and the S register location 99, then by observing the difference between the fault-less and faulty key-stream bits, she would be able to recover the values of r_0^t, CR_t, CS_t for all values of $t=0,1,2,\ldots,100$. The fault at each register location must be preceded by re-keying.

Determining the other bits Hereafter, the values s_0^t for all t=0,1,2, $3,4,\ldots,100$ may be found by solving: $s_0^t=z_t+r_0^t$. Since $\beta_0(\cdot)=s_{99}$, this implies that $s_0^{t+1}=s_{99}^t$, $\forall t=0,1,2,\ldots$ Therefore calculating the values of s_0^t , $\forall t\in[1,100]$ is the same as calculating s_{99}^t , $\forall t\in[0,99]$. The values of r_{99}^t , $\forall t\in[0,99]$ may be obtained as follows. Consider the equation for z_{t+1} :

$$z_{t+1} = \theta_1(R_t, S_t) = r_0^t \cdot r_{67}^t + r_0^t \cdot s_{34}^t + r_{99}^t + s_{99}^t = CR_t \cdot r_0^t + r_{99}^t + s_{99}^t, \ \forall t \in [0, 99].$$

Note that r_{99}^t is the only unknown linear term in these equations and hence its value too can be determined immediately. At this point, we have the following state bits with us:

$$[r_0^t,\ r_{99}^t,\ CR_t,\ s_0^t,\ s_{99}^t,\ CS_t],\ \forall t\in[0,99].$$

¹ We would like to point out that our actual attack does not need precise fault injection at all locations of *R*, *S*. This will be explained in the next sub-section.

Now by using the techniques outlined in Lemma 1 we can determine all the bits of the state R_0 . Thereafter using Lemma 2, one can determine all the bits of S_0 . Thus we have recovered the entire internal state at the beginning of the PRGA.

3.2 How to identify the random locations where faults are injected

In this subsection we will show how the adversary can identify the locations of randomly applied faults to the registers R and S. Although it will not be possible to conclusively determine the location of faults applied to each and every location of R and the S registers, we will show that the adversary can, with some probability, identify faulty streams corresponding to locations 0,67 of R and 99 of S. The adversary will then use the techniques described in Subsection 3.1 to complete the attack.

To help with the process of fault location identification, we define the first and second Signature vectors for the location ϕ of R as

$$\begin{split} &\varPsi_{r_{\phi}}^{1}[i] = \begin{cases} 1\text{, if } z_{t+i} = z_{t+i,\Delta r_{\phi}}(t) \text{ for all choices of } R_{t}, S_{t}, \\ 0\text{, otherwise.} \end{cases} \\ &\varPsi_{r_{\phi}}^{2}[i] = \begin{cases} 1\text{, if } z_{t+i} \neq z_{t+i,\Delta r_{\phi}}(t) \text{ for all choices of } R_{t}, S_{t}, \\ 0\text{, otherwise.} \end{cases} \end{split}$$

for $i = 0, 1, 2, \dots, l - 1$. Here $l \approx 40$ is a suitably chosen constant.

Remark 1. The value of l should be large enough so that one can differentiate 100 randomly generated bit sequences over GF(2) by comparing the first l bits of each sequence. By Birthday paradox, this requires the value of l to be at least $2 \cdot \log_2 100 \approx 14$. We take l = 40 as computer simulations show that this value of l is sufficient to make a successful distinction with high probability.

Similarly one can define Signature vectors for any location ϕ the register S.

$$\begin{split} & \varPsi_{s_{\phi}}^{1}[i] = \begin{cases} 1, & \text{if } z_{t+i} = z_{t+i,\Delta s_{\phi}}(t) \text{ for all choices of } R_{t}, S_{t}, \\ 0, & \text{otherwise.} \end{cases} \\ & \varPsi_{s_{\phi}}^{2}[i] = \begin{cases} 1, & \text{if } z_{t+i} = z_{t+i,\Delta s_{\phi}}(t) \text{ for all choices of } R_{t}, S_{t}, \\ 0, & \text{otherwise.} \end{cases} \end{split}$$

The task for the fault location identification routine is to determine the fault location ϕ of R (or S) by analyzing the difference between z_t, z_{t+1}, \ldots and $z_{t,\Delta r_{\phi}}(t), z_{t+1,\Delta r_{\phi}}(t), \ldots$ (or $z_{t,\Delta s_{\phi}}(t), z_{t+1,\Delta s_{\phi}}(t), \ldots$) by using the Signature vectors $\Psi^1_{r_{\phi}}, \Psi^2_{r_{\phi}}$ (or $\Psi^1_{s_{\phi}}, \Psi^2_{s_{\phi}}$).

Note that the i^{th} bit of $\Psi^1_{r_{\phi}}$ is 1 if and only if the $(t+i)^{th}$ key-stream bits produced by R_t, S_t and $R_{t,\Delta r_{\phi}}(t), S_{t,\Delta r_{\phi}}(t)$ are the same for all choices of the internal state R_t, S_t and that i^{th} bit of $\Psi^2_{r_{\phi}}$ is 1 if the above key-stream bits are different for all choices of the internal state.

The concept of Signature vectors to deduce the location of a randomly applied fault was introduced in [9]. However the analysis of [9] can not be reproduced for MICKEY 2.0, since a lot of different register locations have the same Signature vector. However one can observe the following which are important to mount the attack.

Theorem 1. The following statements hold for the Signature vectors $\Psi^1_{r_s}, \Psi^2_{r_s}$, $\Psi_{s_{\phi}}^1, \Psi_{s_{\phi}}^2$ of MICKEY 2.0.

- $\begin{array}{lll} \textbf{A.} & Although \ \varPsi_{r_{\phi}}^{1}[0]=1, \forall \phi \in [1,99] \ but \ we \ have \ \varPsi_{r_{0}}^{2}[0]=1. \\ \textbf{B.} & \varPsi_{r_{\phi}}^{1}[0]=\varPsi_{r_{\phi}}^{1}[1]=1, \forall \phi \in [1,99] \setminus \{67,99\}. \\ \textbf{C.} & \varPsi_{r_{99}}^{2}[1]=1, \ and \ \varPsi_{r_{67}}^{2}[1]=0. \\ \textbf{D.} & Although \ \varPsi_{s_{\phi}}^{1}[0]=1, \forall \phi \in [1,99] \ but \ we \ have \ \varPsi_{s_{0}}^{2}[0]=1. \\ \textbf{E.} & \varPsi_{s_{\phi}}^{1}[0]=\varPsi_{s_{\phi}}^{1}[1]=1, \forall \phi \in [1,99] \setminus \{34,99\}. \\ \textbf{F.} & \varPsi_{s_{99}}^{2}[1]=1, \ and \ \varPsi_{s_{34}}^{2}[1]=0. \end{array}$

Proof. We present the proof for Case A. The proofs for the remaining cases are similar and can be worked out along the lines of the proof for Case A. A detailed proof is also available in [8].

A. We have

$$z_t + z_{t,\Delta r_0}(t) = \theta_0(R_t, S_t) + \theta_0(R_{t,\Delta r_0}(t), S_{t,\Delta r_0}(t))$$

= $(r_0^t + s_0^t) + (1 + r_0^t + s_0^t) = 1, \ \forall R_t, S_t \in \{0, 1\}^{100}.$

So, $\Psi_{r_0}^2[0] = 1$. Also θ_0 is not a function of any r_i, s_i for $i \in [1, 99]$ and so

$$\theta_0(R_{t,\Delta r_{\phi}}(t), S_{t,\Delta r_{\phi}}(t)) = \theta_0(R_t, S_t) \ \forall \phi \in [1, 99] \text{ and so we have}$$

$$z_t + z_{t,\Delta r_{\phi}}(t) = \theta_0(R_t, S_t) + \theta_0(R_{t,\Delta r_{\phi}}(t), S_{t,\Delta r_{\phi}}(t))$$

= 0, $\forall \phi \in [1, 99], \forall R_t, S_t \in \{0, 1\}^{100}.$

So, $\Psi_{r_{\phi}}^{1}[0] = 1$ for all $\phi \in [1, 99]$.

Thus the proof.

Now, consider the attack scenario in which the adversary is able to re-key the device with the same key-IV multiple number of times and inject a single fault at a random location of register R at the beginning of any particular PRGA round $t \in [0, 100]$ and obtain faulty key-streams. She continues the process until she obtains 100 different faulty key-streams corresponding to 100 different fault locations in R and for each $t \in [0, 100]$ (as mentioned earlier this is done by comparing the first l bits of each faulty key-stream sequence). Assuming that every location has equal probability of getting injected by fault, the above process on an average takes around $100 \cdot \sum_{i=1}^{100} \frac{1}{i} \approx 2^{9.02}$ faults [2] and hence re-keyings for each value of $t \in [0,100]$ and hence a total of $101 \cdot 2^{9.02} \approx 2^{15.68}$ faults. The process has to be repeated for the S register, and so the expected number of faults is $2 \cdot 2^{15.68} = 2^{16.68}$.

Mathematically speaking, if we define $Z_t = [z_t, z_{t+1}, \dots, z_{t+l-1}]$, and $\Delta_{r, \epsilon} Z_t$ $=[z_{t,\Delta r_{\phi}}(t),z_{t+1,\Delta r_{\phi}}(t),\ldots,z_{t+l-1,\Delta r_{\phi}}(t)],$ then the adversary at this point has knowledge of the 100 differential key-streams $\eta_{t,r_{\phi}} = Z_t + \Delta_{r_{\phi}} Z_t$ for each value of $t \in [0, 100]$. The adversary however does not know the exact fault location corresponding to any differential stream i.e. she has been unable to assign fault location labels to any of the differential streams. With this information in hand we shall study the implications of the observations **A** to **F**.

Implication of A: For any $t \in [0, 100]$, $\Psi_{r_0}^2[0] = 1$ guarantees that there is at least one differential stream with $\eta_{t,r_{\phi}}[0] = 1$ whereas $\Psi_{r_{\phi}}^1[0] = 1, \forall \phi \in [1,99]$ guarantees that that there is exactly one differential stream with this property. This implies that out of the 100 differential streams for any PRGA round t the one and only differential stream with this property must have been produced due to a fault on the 0^{th} location in R. Note that labelling of this stream helps us determine the values of CR_t for all $t \in [0, 100]$ from Eqn. (2).

Implication of B, C: Once the differential stream corresponding to the 0^{th} location has been labelled we now turn our attention to the remaining 99 streams. Statement B guarantees that of the remaining 99 streams at least 97 have the property

(P1)
$$\eta_{t,r_{\phi}}[0] = \eta_{t,r_{\phi}}[1] = 0.$$

Statement C guarantees that the number of streams with the property

(P2)
$$\eta_{t,r_{\phi}}[0] = 0, \eta_{t,r_{\phi}}[1] = 1.$$

is at most 2 and at least 1. If the number of streams that satisfy (P1) is 98 and (P2) is 1, then the lone stream satisfying (P2) must have been produced due to fault on location 99 of R. This immediately implies that $\eta_{t,r_{67}}[1] = 0$ which by Eqn. (1) in turn implies that $r_0^t = 0$. Else if the number of streams satisfying (P1) is 97 and (P2) is 2 then it implies that the streams satisfying (P2) were produced due to faults in location 67,99 of R. This implies $\eta_{t,r_{67}}[1] = r_0^t = 1$.

Repeating the entire process on Register S one can similarly obtain the vectors $\Delta_{s_{\phi}}Z_t$ and the differential streams $\eta_{t,s_{\phi}}=Z_t+\Delta_{s_{\phi}}Z_t$ for all values of $t\in[0,100]$. As before the streams $\eta_{t,s_{\phi}}$ are unlabeled. Let us now study the implications of \mathbf{D} , \mathbf{E} , \mathbf{F} .

Implication of D: For any $t \in [0,100]$, $\varPsi^2_{s_0}[0] = 1$ guarantees that there is at least one differential stream with $\eta_{t,s_{\phi}}[0] = 1$ whereas $\varPsi^1_{s_{\phi}}[0] = 1, \forall \phi \in [1,99]$ guarantees that that there is exactly one differential stream with this property. This implies that out of the 100 differential streams for any PRGA round t the one and only differential stream with this property must have been produced due to a fault on the 0^{th} location in S.

Implication of E, F: Once the differential stream corresponding to the 0^{th} location has been labelled we now turn our attention to the remaining 99 streams. The statement **E** guarantees that of the remaining 99 streams at least 97 have the property

(P3)
$$\eta_{t,s_{\phi}}[0] = \eta_{t,s_{\phi}}[1] = 0.$$

Statement \mathbf{F} guarantees that the number of streams with the property

(P4)
$$\eta_{t,s_{\phi}}[0] = 0, \eta_{t,s_{\phi}}[1] = 1,$$

is at most 2 and at least 1.

- Case 1 If the number of streams that satisfy (P3) is 98 and (P4) is 1 then the lone stream satisfying (P4) must have been produced due to fault on location 99 of S. Once the stream corresponding to location 99 of S has been labelled, we can use Eqn (3) to determine $CS_t = \eta_{t,s_{99}}[2]$.
- Case 2 If the number of streams satisfying (P3) is 97 and (P4) is 2 then it implies that the streams satisfying (P4) were produced due to faults in location 34,99 of S.
 - (i) Now if the bit indexed 2 of both these vectors are equal then we can safely assume $CS_t = \eta_{t,s_{99}}[2] = \eta_{t,s_{34}}[2]$.
 - (ii) A confusion occurs when $\eta_{t,s_{99}}[2] \neq \eta_{t,s_{34}}[2]$. In such a situation we would be unable to conclusively able to determine the value of CS_t .

Assuming independence, we assume that Cases 1, 2 have equal probability of occurring. Given the occurrence of Case 2, we can also assume that 2(i), 2(ii) occurs with equal probability. Therefore the probability of confusion, i.e., the probability that we are unable to determine the value of CS_t for any t is approximately equal to $\frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$. Let γ denote the number of $t \in [0, 100]$ such that CS_t can not be conclusively determined then γ is distributed according to $\gamma \sim Binomial(101, \frac{1}{4})$. Therefore the expected value of γ is $E(\gamma) = 101 \cdot \frac{1}{4} = 25.25$. Also the probability that $P(\gamma > 35) = \sum_{k=36}^{101} {101 \choose k} {3 \choose 4}^{101-k} \approx 0.01$. In such a situation the adversary must guess the γ values of CS_t to perform the attack, which implies that the adversary must perform the calculations in Section 3.1 and Lemma 1, Lemma 2 a total of 2^{γ} times to complete the attack. For the correct value of the guesses, the calculated state R_0, S_0 will produce the given fault-free key-stream sequence. We present a complete description of the attack in Algorithm 1.

3.3 Issues related to the length of the IV

It is known that MICKEY 2.0 employs a variable length IV of length at most 80. So if v is the length of the IV then the cipher will run for v+80 (Key loading) +100 (Preclock) clock intervals before entering the PRGA phase. Our attack requires that the first faults are to be injected at the beginning of the PRGA. In order to do that the adversary must know the value of v. This not a strong assumption as IVs are assumed to be known. However even if the adversary does not know the IV or its length the attack can be performed. Since $0 \le v \le 80$ must be satisfied, the strategy of the adversary who does not know the value of v will be as follows. She will inject the first set of faults at clock round 260 which corresponds to the PRGA round p = 260-180-v = 80-v. After performing the attack, the adversary will end up constructing the internal state R_p , S_p instead of R_0 , S_0 . Finding the value of p by looking at the faultless key-stream sequence is straightforward. However, we would like to note that finding R_0 , S_0 is a slightly stronger result because, as reported in [16], there is a finite entropy loss for the state update operation in the MICKEY PRGA.

```
Generate and record the fault-free keystream z_0, z_1, z_2, \ldots for some key-IV K, IV
t \leftarrow 0
while t \le 100 \text{ do}
     while 100 different faulty key-stream sequences \Delta_{r_{\phi}} Z_t have not been obtained do
          Re-key the cipher with key-IV K, IV;
          Inject a fault at a random unknown location \phi \in [0, 99] in R at PRGA round t;
          Record the faulty key-stream sequence \Delta_{r_{\phi}} Z_t;
end
Calculate r_0^t, CR_t, \forall t \in [0, 100] using A, B, C;
while t \leq 100 \text{ do}
     while 100 different faulty key-stream sequences \Delta_{s_{\phi}} Z_t have not been obtained do
          Re-key the cipher with key-IV K, IV;
          Inject a fault at a random unknown location \phi \in [0, 99] in S at PRGA round t;
          Record the faulty key-stream sequence \Delta_{s_{\phi}} Z_t;
     end
     t \leftarrow t + 1:
end
Using D, E, F calculate CS_t, for all such t \in [0, 100] for which there is no confusion;
Let the number of undecided bits CS_t = \gamma;
for Each of the 2^{\gamma} guesses of the undecided CS_t's do
     Use techniques of Subsection 3.1 compute r_0^t, r_{99}^t, CR_t, s_0^t, s_{99}^t, CS_t, \forall t \in [0, 99];
     Use Lemma 1, Lemma 2 try to compute R_0, S_0;
     if R_0, S_0 produce the sequence z_0, z_1, z_2, \ldots then
          Output the required state R_0, S_0;
     end
end
```

Algorithm 1: Fault Attack against MICKEY 2.0

3.4 Complexity of the Attack

As mentioned in Section 3.2, the attack requires the adversary to obtain 100 different faulty key-streams corresponding to all fault locations in R for PRGA rounds $t \in [0, 100]$. This requires $101 \cdot 100 \cdot \sum_{i=1}^{100} \frac{1}{k} \approx 2^{15.68}$ faults on an average. The same process must be repeated for the register S and hence the expected number of total faults is $2^{16.68}$. The computational overload comes from guessing the γ values of CS_t which can not be found out by observing the differential key-streams. This requires a computational effort proportional to 2^{γ} . Since γ is distributed according to $Binomial(101, \frac{1}{4})$, the expected value of γ is 25.25. The expected value of the computation complexity is therefore given by $E(2^{\gamma}) = \sum_{k=0}^{101} \binom{101}{k} \binom{4}{4}^k \binom{3}{4}^{101-k} 2^k \approx 2^{32.5}$.

4 Case of Multiple bit faults

In this section we explore the situation in which the adversary is unable to induce a single bit flip of the internal state every time she injects a fault. We assume that the best she can do is affect the bit values of three consecutive locations of the state. This gives rise to three situations (a) the attacker flips exactly one register bit (100 possibilities), (b) she flips 2 consecutive locations i, i+1 of R/S (99 possibilities), (c) she flips 3 consecutive locations i, i+1, i+2

of R/S (98 possibilities). Studying such a model makes sense if we attack an implementation of MICKEY where the register cells of the R and S registers are physically positioned linearly one after the other. Now, this attack scenario gives rise to 100 + 99 + 98 = 297 different instances of faults due to any single fault injection, and we will assume that all these instances are equally likely to occur. As before we will assume that the adversary is able to re-key the device with the original Key-IV and obtain all the 297 faulty streams for any PRGA round $t \in [0, 100]$ by randomly injecting faults in either the R or S register. For each PRGA round the attacker thus needs around $297 \cdot \ln 297 \approx 2^{10.7}$ faults. Thus the fault requirement for the R register is $101 \cdot 2^{10.7} = 2^{17.4}$. The process has to be repeated for the S register and so the total fault requirement is $2 \cdot 2^{17.4} = 2^{18.4}$.

Let $\Phi = \{\phi_1, \phi_2, \dots, \phi_k\}$ denote the indices of k $(k \leq 3)$ continuous locations in the R (or S) register. The the notations $R_{t,\Delta r_{\Phi}}(t_0), S_{t,\Delta r_{\Phi}}(t_0), R_{t,\Delta s_{\Phi}}(t_0), S_{t,\Delta s_{\Phi}}(t_0), S_{t,\Delta r_{\Phi}}(t_0), S_{t,\Delta r_{\Phi}}(t_0), S_{t,\Delta s_{\Phi}}(t_0), S_{t,\Delta s_{$

The bit r_0 is affected. This could happen in 3 ways: a) r_0 alone is toggled, b) r_0, r_1 are toggled, c) r_0, r_1, r_2 are toggled. We state the following

Proposition 1. $\Psi^1_{r_{\mathbf{\Phi}}}[0] = 1, \forall \mathbf{\Phi} \text{ such that } 0 \notin \mathbf{\Phi} \text{ but } \Psi^2_{r_{\mathbf{\Phi}}}[0] = 1 \text{ for all } \mathbf{\Phi} \text{ that contain } 0.$

Proof. Since
$$\theta_0$$
 is a function of r_0, s_0 only we will have $z_t + z_{t,\Delta r_{\mathbf{\Phi}}}(t) = \theta_0(R_t, S_t) + \theta_0(R_{t,\Delta r_{\mathbf{\Phi}}}(t), S_{t,\Delta r_{\mathbf{\Phi}}}(t)) = \begin{cases} 0, & \text{if } 0 \notin \mathbf{\Phi}, \\ 1, & \text{if } 0 \in \mathbf{\Phi} \end{cases}$ Hence the result.

This implies that any faulty stream with its first bit different from the faultless first bit must have been produced due to a fault that has affected r_0 and vice versa. Thus 3 out of the 297 faulty streams have this property and they can be identified easily. Furthermore since $\theta_1(R_t, S_t) + \theta_1(R_{t,\Delta r_{\Phi}}(t), S_{t,\Delta r_{\Phi}}(t)) =$ $s_{34}^t + r_{67}^t = CR_t \ \forall \Phi$ containing 0, the second bit in the all these faulty streams are equal and the difference of this bit with the second faultless bit gives us the value of CR_t .

The bits r_{67} and r_{99} are affected. r_{67} could be affected in 6 ways: a) r_{67} alone is toggled, b) r_{66} , r_{67} are toggled, c) r_{67} , r_{68} are toggled, d) r_{65} , r_{66} , r_{67} are toggled, e) r_{66} , r_{67} , r_{68} are toggled and f) r_{67} , r_{68} , r_{69} are toggled. Also note that r_{99} could be affected in 3 ways: a) r_{99} is toggled, b) r_{98} , r_{99} are toggled and c) r_{97} , r_{98} , r_{99} are all toggled. Again we state the following propositions.

Proposition 2. $\Psi^1_{r_{\mathbf{\Phi}}}[0] = \Psi^1_{r_{\mathbf{\Phi}}}[1] = 1, \forall \mathbf{\Phi} \text{ such that } 0, 67, 99 \notin \mathbf{\Phi}.$

Proposition 3. If $99 \in \Phi$ then $\Psi_{r_{\Phi}}^2[1] = 1$. If $67 \in \Phi$ then $\Psi_{r_{\Phi}}^2[1] = 0$.

Proof. Note that θ_0 is a function of only r_0, s_0 and θ_1 is a function of r_0, r_{67}, r_{99} , s_{34}, s_{99} only. Therefore,

$$z_{t+1} + z_{t+1,\Delta r_{\Phi}}(t) = \theta_1(R_t, S_t) + \theta_1(R_{t,\Delta r_{\Phi}}(t), S_{t,\Delta r_{\Phi}}(t))$$

$$= \begin{cases} 0, & \text{if } 0, 67, 99 \notin \mathbf{\Phi}, \\ CR_t, & \text{if } 0 \in \mathbf{\Phi}, \\ r_0^t, & \text{if } 67 \in \mathbf{\Phi}, \\ 1 & \text{if } 99 \in \mathbf{\Phi} \end{cases}$$
(G)

$$\begin{bmatrix} r_0^c, & \text{if } 67 \in \mathbf{\Phi}, \\ 1 & \text{if } 99 \in \mathbf{\Phi} \end{bmatrix} \tag{K}$$

Hence the result.

(G) implies that of the remaining 294 differential streams at least 294 - 6 - 3 =285 satisfy

(P5)
$$\eta_{t,r_{\Phi}}[0] = \eta_{t,r_{\Phi}}[1] = 0.$$

and (L) implies that the number of differential streams with the property

(P6)
$$\eta_{t,r_{\mathbf{\Phi}}}[0] = 0, \eta_{t,r_{\mathbf{\Phi}}}[1] = 1.$$

is at least 3. A direct implication of (K) is that if the number of differential streams satisfying (P5) is 285 and (P6) is 9 then $r_0^t = 1$ and on the other hand if, the number of streams satisfying (P5) is 291 and (P6) is 3 then $r_0^t = 0$. Note that these are exclusive cases i.e the number of streams satisfying (P5) can be either 285 or 291. Since the values of r_0^t , CR_t for all $t \in [0, 100]$ are now known, the attacker can now use the techniques of Section 3.1 and Lemma 1 to calculate the entire initial state R_0 .

The bits s_0 , s_{34} and s_{99} are affected. Following previous descriptions we know that there are respectively 3, 6, 3 possibilities of faults affecting s_0, s_{34}, s_{99} . Again, we present the following propositions before describing the attack.

Proposition 4. $\Psi^1_{s_{\Phi}}[0] = 1, \forall \Phi \text{ such that } 0 \notin \Phi \text{ but } \Psi^2_{s_{\Phi}}[0] = 1 \text{ for all } \Phi \text{ that }$ contain 0.

Proposition 5. $\Psi^1_{s_{\Phi}}[0] = \Psi^1_{s_{\Phi}}[1] = 1, \forall \Phi \text{ such that } 0, 34, 99 \notin \Phi.$

Proposition 6. If
$$99 \in \Phi$$
 then $\Psi_{s_{\Phi}}^2[1] = 1$. If $34 \in \Phi$ then $\Psi_{s_{\Phi}}^2[1] = 0$.

Proof. Proofs are similar to those of previous propositions. Since θ_0 is a function of only r_0 , s_0 and θ_1 is a function of r_0 , r_{67} , r_{99} , s_{34} , s_{99} only, we have

$$z_t + z_{t,\Delta s_{\mathbf{\Phi}}}(t) = \theta_0(R_t, S_t) + \theta_0(R_{t,\Delta s_{\mathbf{\Phi}}}(t), S_{t,\Delta s_{\mathbf{\Phi}}}(t)) = \begin{cases} 0, & \text{if } 0 \notin \mathbf{\Phi}, \\ 1, & \text{if } 0 \in \mathbf{\Phi} \end{cases}$$

$$z_{t+1} + z_{t+1,\Delta s_{\mathbf{\Phi}}}(t) = \theta_{1}(R_{t}, S_{t}) + \theta_{1}(R_{t,\Delta s_{\mathbf{\Phi}}}(t), S_{t,\Delta s_{\mathbf{\Phi}}}(t))$$

$$= \begin{cases} 0, & \text{if } 34, 99 \notin \mathbf{\Phi}, & (M) \\ r_{0}^{t}, & \text{if } 34 \in \mathbf{\Phi}, & (N) \\ 1, & \text{if } 99 \in \mathbf{\Phi}. & (O) \end{cases}$$

Proposition 4 proves that there are 3 differential streams out of 297 which have $\eta_{s_{\Phi}}[0] = 1$. (M) implies that of the remaining 294 streams, at least 294 - 3 - 6 = 285 satisfy

(P7)
$$\eta_{t,s_{\mathbf{\Phi}}}[0] = \eta_{t,s_{\mathbf{\Phi}}}[1] = 0.$$

(O) implies that the number of streams that satisfy

(P8)
$$\eta_{t,s_{\Phi}}[0] = 0, \eta_{t,s_{\Phi}}[1] = 1.$$

is at least 3.

CASE I. If the number of streams that satisfy (P7) is 291 and (P8) is 3 then the streams satisfying (P8) must have been produced due to faults affecting s_{99} . For these streams we have

$$\begin{split} z_{t+2} + z_{t+2,\Delta s_{\mathbf{\Phi}}}(t) = & \theta_2(R_t, S_t) + \theta_2(R_{t,\Delta s_{\mathbf{\Phi}}}(t), S_{t,\Delta s_{\mathbf{\Phi}}}(t)) \\ = & \begin{cases} CS_t, & \text{if } \mathbf{\Phi} = \{99\}, \\ 1 + CS_t, & \text{if } \mathbf{\Phi} = \{98, 99\} \\ 1 + CS_t. & \text{if } \mathbf{\Phi} = \{97, 98, 99\} \end{cases} \end{split}$$

So for 2 of these 3 streams we have $\eta_{s_{\Phi}}[2] = 1 + CS_t$. Hence our strategy will be to look at the bit indexed 2 of these 3 streams. Two of them will be equal and we designate that value as $1 + CS_t$.

CASE II. If the number of streams that satisfy (P7) is 285 and (P8) is 9 then the streams have been produced due to faults that have affected s_{34} and s_{99} . Note the identity

$$\sum_{\Phi: 34 \in \Phi} \eta_{t,s_{\Phi}}[2] = r_0^t \cdot r_{67}^t \cdot s_{34}^t + r_{99}^t \cdot s_{34}^t$$

Therefore the sum of the bits indexed 2 of all the differential streams that satisfy (P8) is

$$\begin{split} \sum_{\Phi: \ 34 \text{ or } 99 \in \Phi} \eta_{t,s_{\Phi}}[2] = & r_0^t \cdot r_{67}^t \cdot s_{34}^t + r_{99}^t \cdot s_{34}^t + CS_t + CS_t + 1 + CS_t + 1 \\ = & CS_t + r_0^t \cdot r_{67}^t \cdot s_{34}^t + r_{99}^t \cdot s_{34}^t. \end{split}$$

At this time the entire initial state of the R register and all values of CR_t for $t \in [0, 100]$ is known to us. Hence by Lemma 2, all values of r_i^t for all t > 0 can be calculated by clocking the register R forward. Also, since $CR_t = r_{67}^t + s_{34}^t$ is known, $s_{34}^t = CR_t + r_{67}^t$ can be calculated easily. Therefore in the previous equation CS_t becomes the only unknown and thus its value can be calculated easily.

At this point of time we have the values of r_0^t , CR_t , CS_t for all values of t = 0, 1, 2, ..., 100. Now by using the techniques of Section 3.1 and Lemma 1, 2 we will be able to determine the entire initial state R_0 , S_0 . Note that using this fault model although the fault requirement increases, the adversary does not have to bear the additional computational burden of guessing γ values of CS_t .

5 Conclusion

A differential fault attack against the stream cipher MICKEY 2.0 is presented. The work is one of the first cryptanalytic attempts against this cipher and requires reasonable computational effort. The attack works due to the simplicity of the output function and certain register update operations of MICKEY 2.0 and would have been thwarted had these been of a more complex nature. It would be interesting to study efficient counter-measures with minimum tweak in the design.

Given our work in this paper, differential fault attacks are now known against all of the three ciphers in the hardware portfolio of eStream. The attacks on all the 3 ciphers use exactly the same fault model that is similar to what described in this paper. Let us now summarize the fault requirements.

Cipher	State size	Average # of Faults
Trivium [15]	288	3.2
Grain v1 [10]	160	$\approx 2^{8.5}$
MICKEY 2.0	200	$\approx 2^{16.7}$

To the best of our knowledge, there was no published fault attack on MICKEY 2.0. prior to our work. We believe that one of the reasons this remained open for such a long time could be that the cipher uses irregular clocking to update its state registers. Hence it becomes difficult to determine the location of a randomly applied fault injected in either the R or S register by simply comparing the faulty and fault-free key-streams. The idea explained in Theorem 1 and its implications are instrumental in mounting the attack. The total number of faults is indeed much higher when we compare it with the other two eStream hardware candidates. However, this seems natural as MICKEY 2.0 has more complex structure than Trivium or Grain v1.

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Appendix A: The functions $\rho_i, \beta_i \ \forall i \in [0, 99]$

i	ρ_i	$ eta_i $
0	$r_0 \cdot r_{67} + r_0 \cdot s_{34} + r_{99}$	s99
1	$r_0 + r_1 \cdot r_{67} + r_1 \cdot s_{34} + r_{99}$	$s_0 + s_1 \cdot s_2 + s_1 + s_{99}$
2	$r_1 + r_2 \cdot r_{67} + r_2 \cdot s_{34}$	$s_1 + s_2 \cdot s_3 + s_{99}$
3	$r_2 + r_3 \cdot r_{67} + r_3 \cdot s_{34} + r_{99}$	$r_{33} \cdot s_{99} + s_2 + s_3 \cdot s_4 + s_3 + s_{67} \cdot s_{99} + s_{99}$
	$r_3 + r_4 \cdot r_{67} + r_4 \cdot s_{34} + r_{99}$	$r_{33} \cdot s_{99} + s_3 + s_4 \cdot s_5 + s_4 + s_5 + s_{67} \cdot s_{99} + 1$
5	$r_4 + r_5 \cdot r_{67} + r_5 \cdot s_{34} + r_{99}$	$s_4 + s_5 \cdot s_6 + s_6 + s_{99}$
	$r_5 + r_6 \cdot r_{67} + r_6 \cdot s_{34} + r_{99}$	$r_{33} \cdot s_{99} + s_5 + s_6 \cdot s_7 + s_{67} \cdot s_{99}$
	$r_6 + r_7 \cdot r_{67} + r_7 \cdot s_{34}$	$r_{33} \cdot s_{99} + s_6 + s_7 \cdot s_8 + s_7 + s_{67} \cdot s_{99} + s_{99}$
	$r_7 + r_8 \cdot r_{67} + r_8 \cdot s_{34}$	$r_{33} \cdot s_{99} + s_7 + s_8 \cdot s_9 + s_{67} \cdot s_{99} + s_{99}$
	$r_8 + r_9 \cdot r_{67} + r_9 \cdot s_{34} + r_{99}$	$r_{33} \cdot s_{99} + s_8 + s_9 \cdot s_{10} + s_9 + s_{10} + s_{67} \cdot s_{99} + s_{99} + 1$
	$r_9 + r_{10} \cdot r_{67} + r_{10} \cdot s_{34}$	$r_{33} \cdot s_{99} + s_9 + s_{10} \cdot s_{11} + s_{10} + s_{67} \cdot s_{99} + s_{99}$
	$r_{10} + r_{11} \cdot r_{67} + r_{11} \cdot s_{34}$	$s_{10} + s_{11} \cdot s_{12} + s_{11} + s_{12} + s_{99} + 1$
12	$r_{11} + r_{12} \cdot r_{67} + r_{12} \cdot s_{34} + r_{99}$	$s_{11} + s_{12} \cdot s_{13} + s_{12} + s_{13} + s_{99} + 1$
	$r_{12} + r_{13} \cdot r_{67} + r_{13} \cdot s_{34} + r_{99}$	$s_{12} + s_{13} \cdot s_{14} + s_{14} + s_{99}$
	$r_{13} + r_{14} \cdot r_{67} + r_{14} \cdot s_{34}$	$r_{33} \cdot s_{99} + s_{13} + s_{14} \cdot s_{15} + s_{15} + s_{67} \cdot s_{99} + s_{99}$
	$r_{14} + r_{15} \cdot r_{67} + r_{15} \cdot s_{34}$	$r_{33} \cdot s_{99} + s_{14} + s_{15} \cdot s_{16} + s_{15} + s_{67} \cdot s_{99}$
16	$r_{15} + r_{16} \cdot r_{67} + r_{16} \cdot s_{34} + r_{99}$	$s_{15} + s_{16} \cdot s_{17} + s_{17}$
	$r_{16} + r_{17} \cdot r_{67} + r_{17} \cdot s_{34}$	$r_{33} \cdot s_{99} + s_{16} + s_{17} \cdot s_{18} + s_{17} + s_{67} \cdot s_{99} + s_{99}$
		$r_{33} \cdot s_{99} + s_{17} + s_{18} \cdot s_{19} + s_{67} \cdot s_{99}$
19	$r_{18} + r_{19} \cdot r_{67} + r_{19} \cdot s_{34} + r_{99}$	$ s_{18} + s_{19} \cdot s_{20} + s_{20} + s_{99} $
20	$ r_{19} + r_{20} \cdot r_{67} + r_{20} \cdot s_{34} + r_{99} $	$r_{33} \cdot s_{99} + s_{19} + s_{20} \cdot s_{21} + s_{67} \cdot s_{99} + s_{99}$

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i \mid \rho_i
r_{25} + r_{26} \cdot r_{67} + r_{26} \cdot s_{34}
                                        r_{27} + r_{28} \cdot r_{67} + r_{28} \cdot s_{34} + r_{99} r_{33} \cdot s_{99} + s_{27} + s_{28} \cdot s_{29} + s_{28} + s_{67} \cdot s_{99} + s_{99}
                                       \begin{array}{c} r_{33} \cdot s_{99} + s_{27} + s_{28} \cdot s_{29} + s_{26} \cdot \cdot \cdot \cdot \\ s_{28} + s_{29} \cdot s_{30} + s_{30} \\ r_{33} \cdot s_{99} + s_{29} + s_{30} \cdot s_{31} + s_{30} + s_{31} + s_{67} \cdot s_{99} + 1 \\ r_{33} \cdot s_{99} + s_{30} + s_{31} \cdot s_{32} + s_{31} + s_{67} \cdot s_{99} + s_{99} \\ s_{51} + s_{32} \cdot s_{33} + s_{32} + s_{33} + s_{99} + 1 \\ r_{33} \cdot s_{99} + s_{32} + s_{33} \cdot s_{34} + s_{33} + s_{67} \cdot s_{99} \\ \end{array}
|s_{33} + s_{34} \cdot s_{35}|
|s_{34} + s_{35} \cdot s_{36} + s_{36}|
||r_{39} + r_{40} \cdot r_{67} + r_{40} \cdot s_{34}||
                                         r_{33} \cdot s_{99} + s_{39} + s_{40} \cdot s_{41} + s_{40} + s_{67} \cdot s_{99} + s_{99}
r_{44} + r_{45} \cdot r_{67} + r_{45} \cdot s_{34} + r_{99} r_{33} \cdot s_{99} + s_{44} + s_{45} \cdot s_{46} + s_{46} + s_{67} \cdot s_{99}
\begin{array}{c} r_{33} \cdot s_{99} + s_{47} + s_{48} \cdot s_{49} + s_{67} \cdot s_{99} \\ r_{33} \cdot s_{99} + s_{48} + s_{49} \cdot s_{50} + s_{49} + s_{50} + s_{67} \cdot s_{99} + s_{99} + 1 \end{array}
52 || r_{51} + r_{52} \cdot r_{67} + r_{52} \cdot s_{34} + r_{99} || r_{33} \cdot s_{99} + s_{51} + s_{52} \cdot s_{53} + s_{67} \cdot s_{99} ||
59 || r_{58} + r_{59} \cdot r_{67} + r_{59} \cdot s_{34}
 \begin{array}{l} s_{72} + s_{73} \cdot s_{74} + s_{74} \\ r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{73} + s_{74} \cdot s_{75} + s_{74} + s_{75} + 1 \\ r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{74} + s_{75} \cdot s_{76} + s_{75} + s_{76} + s_{99} + 1 \\ r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{75} + s_{76} \cdot s_{77} + s_{76} + s_{77} + s_{99} + 1 \\ \end{array} 
\begin{array}{c} 91 \quad r_{67} \cdot r_{91} + r_{90} + r_{91} \cdot s_{34} + r_{99} \quad r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{90} + s_{91} \cdot s_{92} + s_{99} \\ 92 \quad r_{67} \cdot r_{92} + r_{91} + r_{92} \cdot s_{34} + r_{99} \quad r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{91} + s_{92} \cdot s_{93} + s_{92} + s_{99} \\ \end{array}
\frac{96}{97} \left| \frac{r_{67} \cdot r_{96} + r_{95} + r_{96} \cdot s_{34} + r_{99}}{r_{67} \cdot r_{97} + r_{96} + r_{97} \cdot s_{34} + r_{99}} \right| \frac{r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{95} + s_{96} \cdot s_{97} + s_{96} + s_{99}}{s_{96} + s_{97} \cdot s_{98} + s_{98}}
||s_{97} + s_{98} \cdot s_{99} + s_{99}||r_{33} \cdot s_{99} + s_{67} \cdot s_{99} + s_{98}||
```